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# Multi-Task Assignment for CrowdSensing in Mobile Social Networks

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# Outline

- **Background & Motivation**
- **Model & Problem**
- **Solution**
- **Simulation**
- **Conclusion**

# Background

- **Mobile CrowdSensing**

- **Smart devices:**

iPads, smart phones, portable devices, etc.

(light sensor, GPS, camera, digital compass, etc.)

- **A new paradigm:**

mobile users exploit their carried smart devices to conduct complex computation and sensing tasks.

- **Applications:**

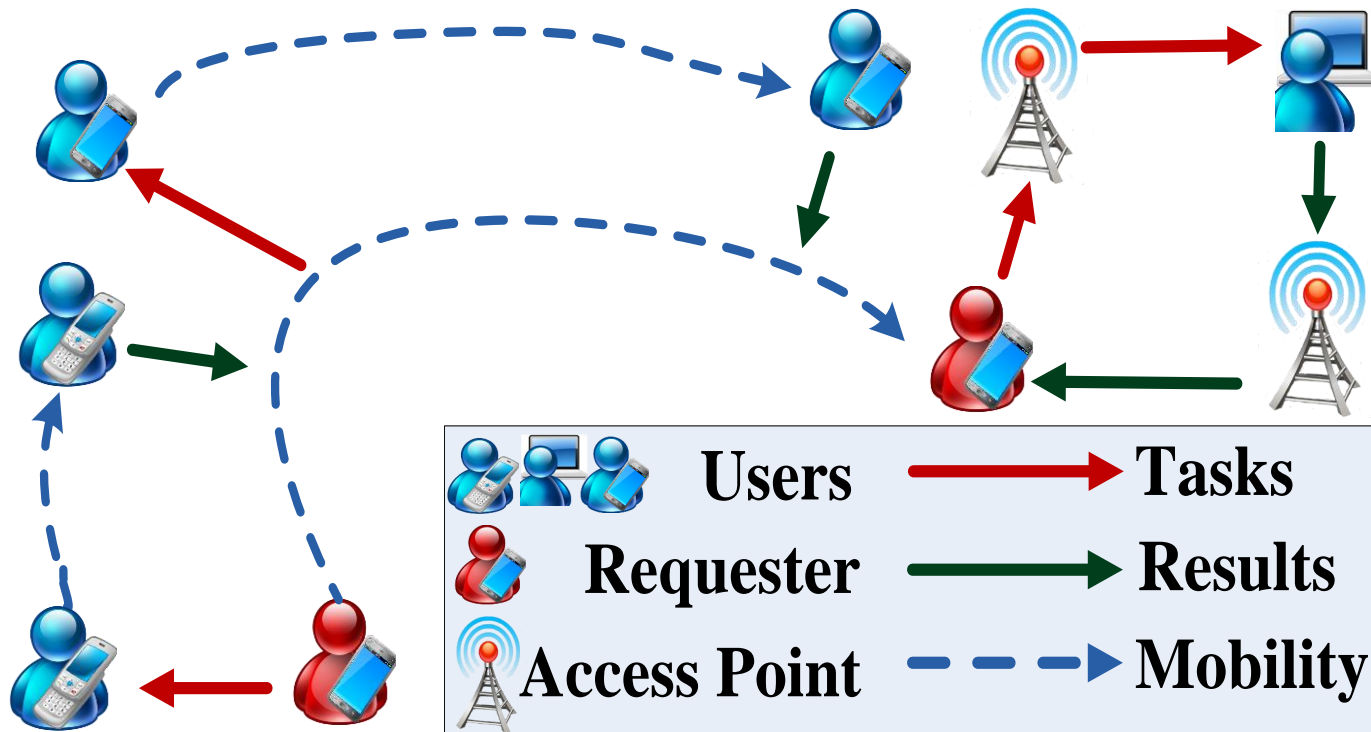
urban WiFi characterization, map labelling, traffic information mapping, etc.

# Motivation

- **CrowdSensing in Mobile Social Networks**
  - **Mobile Social Network (MSN):**
    - 3G/4G communication model
    - Short-distance communication model (WiFi, Bluetooth)
- **Existing CrowdSensing Algorithms**
  - **Task assignment**
    - LRBA [Infocom'14]
    - Fair energy-efficient allocation algorithm [Infocom'14]
  - **Other issues**
    - Incentive mechanisms, Privacy-preserving schemes,...

# Motivation

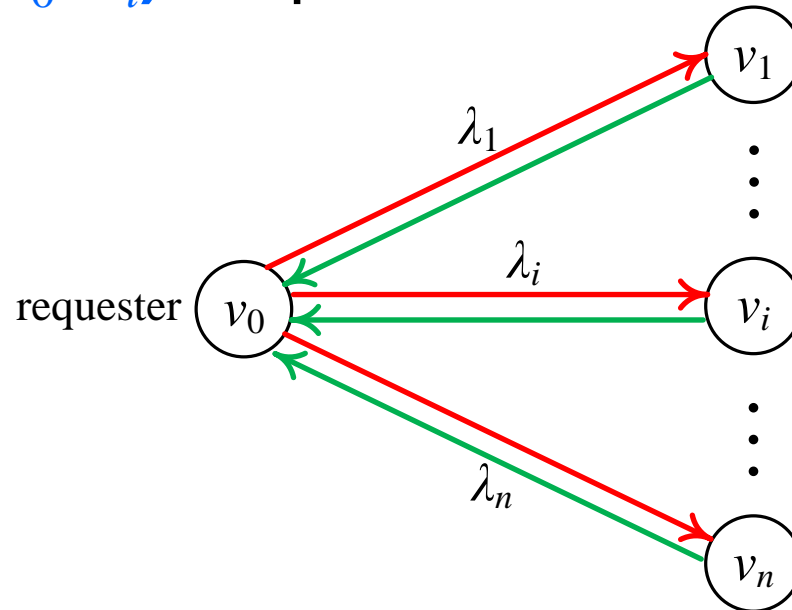
- **Time-sensitive task assignment**



# Model & Problem

- **Network Model**

- **MSN users:**  $V = \{v_0, v_1, \dots, v_n\}$
- **Requester:**  $v_0$
- **Communication model:** WiFi, Bluetooth
- **Contact ( $v_0, v_i$ ):** exponential distribution  $\lambda_i$



# Model & Problem

- **Problem**

- **Tasks:**  $J = \{ j_1, j_2, \dots, j_m \}$

- **Workloads:**  $\tau_1, \tau_2, \dots, \tau_m$

- **Makespan  $M(j)$ :** the time that the requester finally receives the result of the task  $j$ .

- **Task assignment strategy:**

$$\Pi = \{ J_1, J_2, \dots, J_n \}$$

$J_i = \{ \dots, j, \dots, j', \dots \}$  is an ordered subset of  $J$

$j \leq j'$ :  $j$  will be processed prior to  $j'$

$$\sum_{i=1}^n J_i = J, \quad J_i \cap J_{i'} = \emptyset, \quad \forall J_i, J_{i'} \in \Pi$$

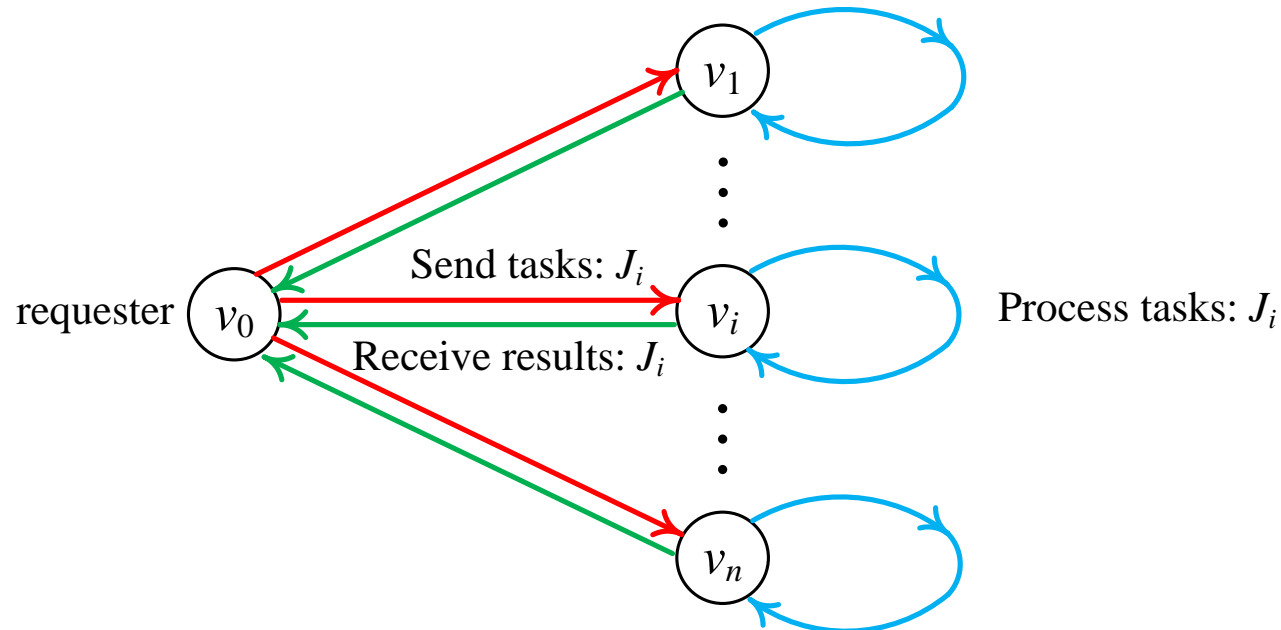
# Model & Problem

- **Problem**

- Average Makespan  $AM(\Pi)$ :

$$AM(\Pi) = \frac{1}{m} \sum_{j \in J} M(j) |_{\Pi}$$

- **Objective: Maximize  $AM(\Pi)$**





# Solution: oFfline Task Assignment

- **FTA: oFfline Task Assignment**

the requester makes the task assignment decision before it encounters any other mobile user

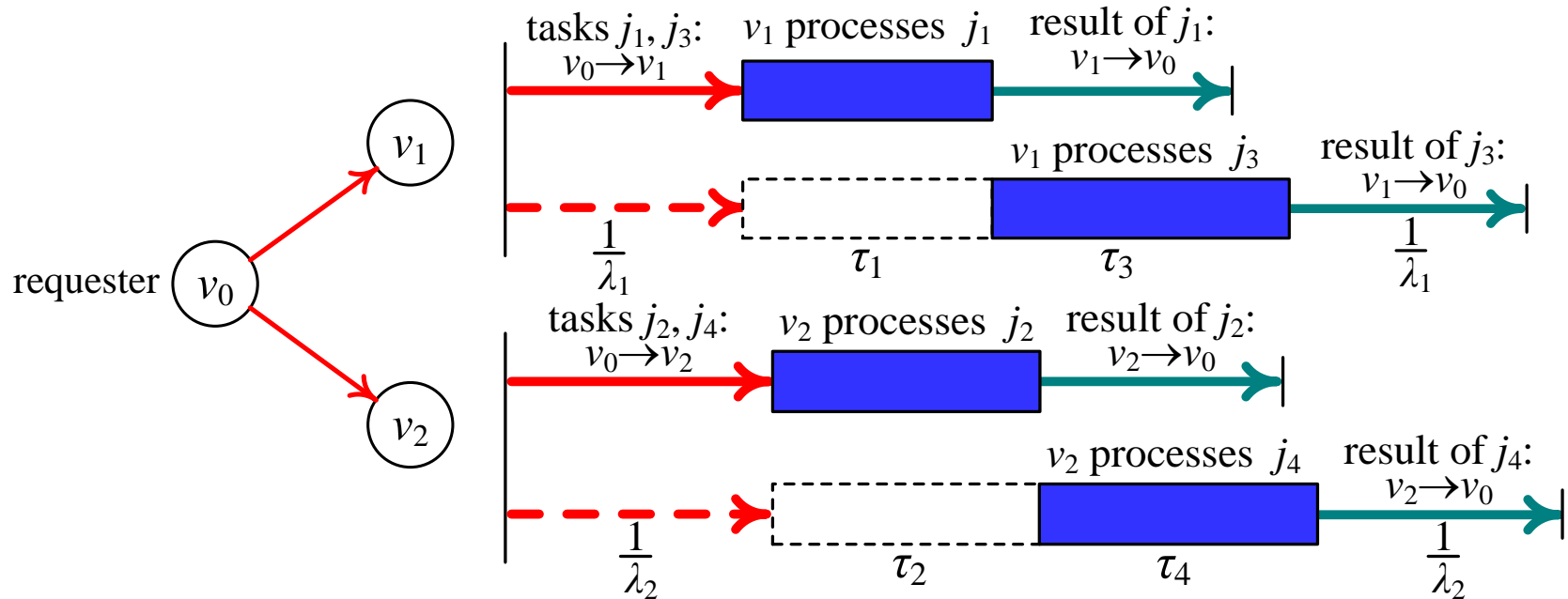
- **Basic Formula**

**Theorem 1:** The average makespan  $AM(\Pi_F)$  for an arbitrary offline task assignment strategy  $\Pi_F = \{J_1, J_2, \dots, J_n\}$  satisfies:

$$AM(\Pi_F) = \frac{1}{m} \sum_{i=1}^n \sum_{j \in J_i} \left( \frac{2}{\lambda_i} + \sum_{j' \in J_i \wedge j' \leq j} \tau_{j'} \right)$$

# Solution: oFfline Task Assignment

- Example:**  $\Pi_F = \{J_1, J_2\}$ ,  $J_1 = \{j_1, j_3\}$ ,  $J_2 = \{j_2, j_4\}$



$$M(j_1) = \frac{2}{\lambda_1} + \tau_1, M(j_2) = \frac{2}{\lambda_1} + \tau_1 + \tau_3, M(j_3) = \frac{2}{\lambda_2} + \tau_2, M(j_4) = \frac{2}{\lambda_2} + \tau_2 + \tau_4$$

$$AM(\Pi_F) = \frac{1}{4}(M(j_1) + M(j_2) + M(j_3) + M(j_4))$$

# Solution: oFfline Task Assignment

- Basic Property of Optimal FTA Solution:  $\Pi^*_F$

**Theorem 2:** Suppose the optimal offline task assignment strategy is  $\Pi^*_F = \{J_1, J_2, \dots, J_n\}$ . Then, the tasks with small workloads will be processed first. More specifically, for  $\forall j, j' \in J_i$  ( $1 \leq i \leq n$ ), if  $\tau_j \leq \tau_{j'}$ , then the order of tasks  $j$  and  $j'$  in  $J_i$  satisfies  $j \leq j'$ .

– In the last example:

$$\tau_1 < \tau_2 < \tau_3 < \tau_4$$

$$j_1 \leq j_3 \quad j_2 \leq j_4$$

# Solution: oFfline Task Assignment

- Basic Property of Optimal FTA Solution:  $\Pi^*_F$ 
  - Expected Processing Time ( $EPT_i$ ):

the expected time for the user  $v_i$  to meet the requester, process the tasks in hand, and return the result.

Example:

user  $v_i$  has tasks  $J_{i_1}, J_{i_2}, \dots, J_{i_k}$

$$EPT_i = \frac{2}{\lambda_i} + \tau_{i_1} + \tau_{i_2} + \dots + \tau_{i_k}$$

# Solution: oFfline Task Assignment

- Basic Property of Optimal FTA Solution:  $\Pi^*_F$

**Theorem 3:** suppose that the workloads of the  $j_1, j_2, \dots, j_m$  satisfy  $\tau_1 \leq \tau_2 \leq \dots \leq \tau_m$ , among which the tasks  $j_1, j_2, \dots, j_{k-1}$  ( $1 \leq k \leq m$ ) have been assigned. Assume that the current expected processing time of user  $v_i$  is  $EPT_i$ . Then, the optimal task assignment strategy  $\Pi^*_F$  satisfies:

the task  $j_k$  will be assigned to the user who currently has the minimum expected processing time, i.e.,

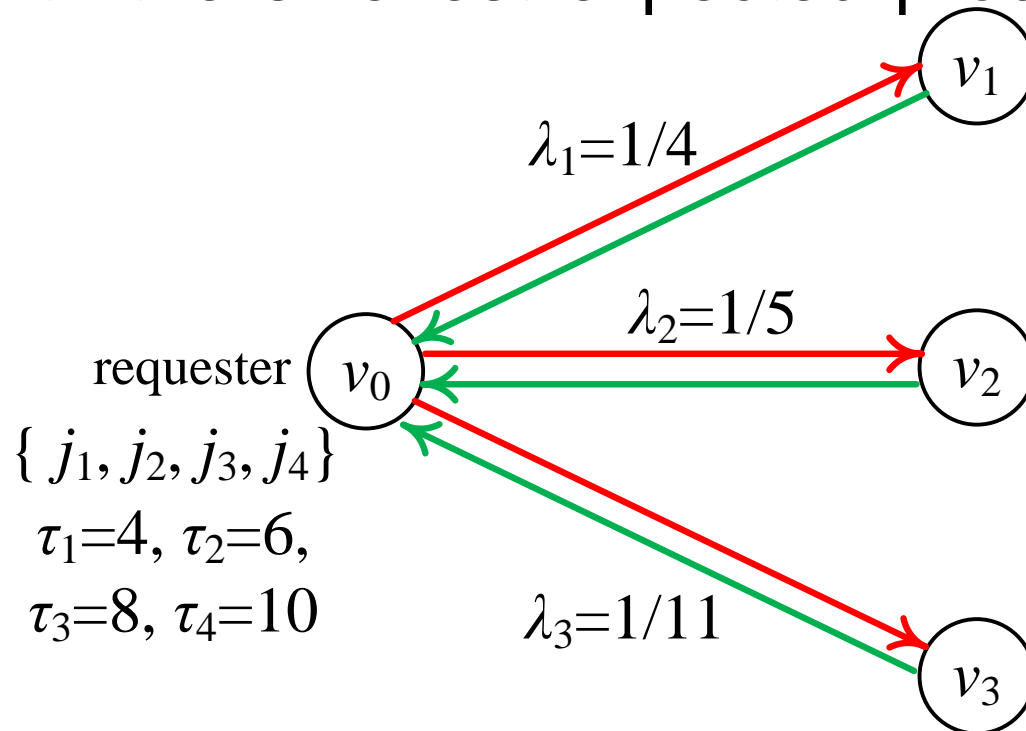
$$EPT_i = \text{Min}\{EPT_1, \dots, EPT_n\} \Rightarrow j_k \in J_i$$

# Solution: oFfline Task Assignment

- **Basic Idea:**

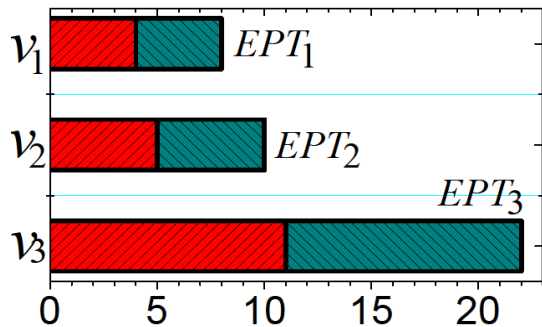
we always assign the minimum workload task among the tasks that have not been assigned to the user with the smallest expected processing time

- **Example:**

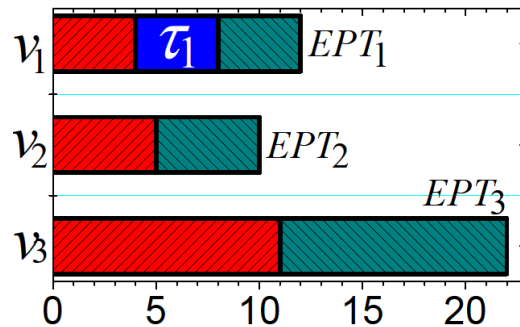


# Solution: oFfline Task Assignment

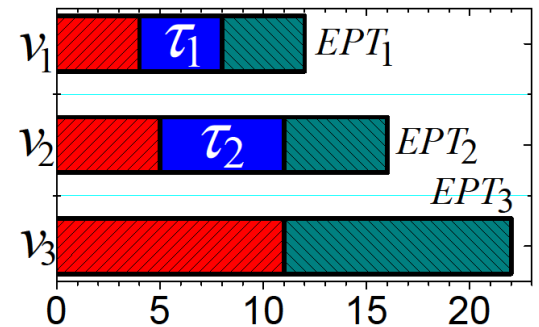
## – Example:



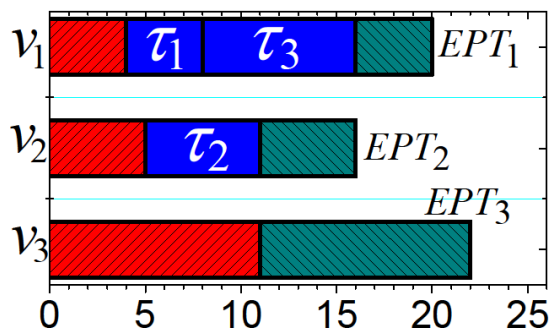
The initial state



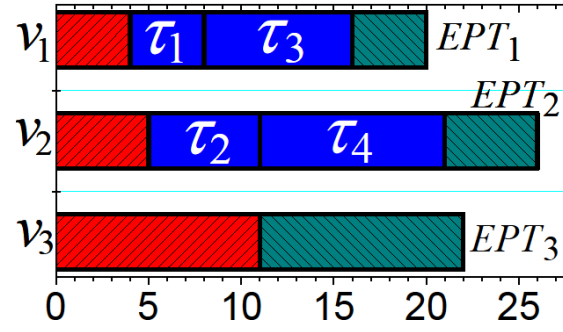
Assign task  $j_1$



Assign task  $j_2$



Assign task  $j_3$



Assign task  $j_4$

# Solution: oFfline Task Assignment

- The Detailed FTA Algorithm:

**Algorithm 1** The FTA Algorithm

**Require:**  $J = \{j_1, j_2, \dots, j_m : \tau_1 \leq \tau_2 \leq \dots \leq \tau_m\}$ ,

$V = \{v_1, v_2, \dots, v_n : \lambda_1, \lambda_2, \dots, \lambda_n\}$ .

**Ensure:**  $\Pi_F = \{J_1, J_2, \dots, J_n\}$

1: **for** each user  $v_i$  **do**

2:    $J_i = \emptyset$ ;

3:    $EPT_i = \frac{2}{\lambda_i}$ ;

4: **for** task  $j$  from  $j_1$  to  $j_m$  **do**

5:    $i_{min} = \operatorname{argmin}\{EPT_1, EPT_2, \dots, EPT_n\}$ ;

6:   Assign task  $j$  to  $v_{i_{min}}$ :  $J_{i_{min}} = J_{i_{min}} + \{j\}$ ;

7:    $EPT_{i_{min}} = EPT_{i_{min}} + \tau_{i_{min}}$ ;

**Corollary 4:** The FTA algorithm can achieve the optimal average makespan for the offline task assignment case.



# Solution: oNline Task Assignment

- **NTA: oNline Task Assignment**

the requester dynamically assigns tasks at each time when it encounters a mobile user

- **Instant Processing Time (IPT)**

the time for a mobile user, who has just encountered and received some tasks from the requester, to process these tasks and return the results

**Example:** user  $v_i$  has tasks  $J_{i_1}, J_{i_2}, \dots, J_{i_k}$

$$IPT_i = \frac{1}{\lambda_i} + \tau_{i_1} + \tau_{i_2} + \dots + \tau_{i_k}$$

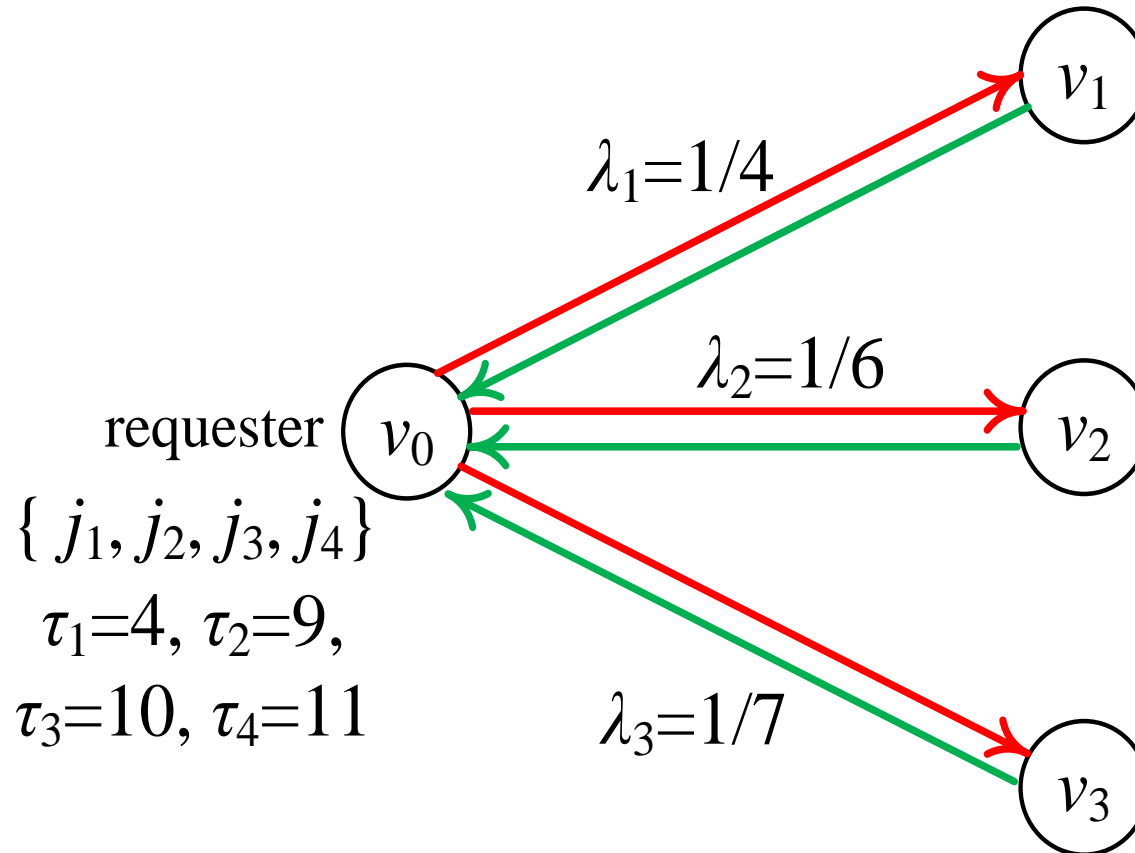
# Solution: oNline Task Assignment

- **Basic idea**

- When the requester encounters a mobile user  $v_i$ , it first computes  $IPT_i$  and  $EPT$  values of other users who have not been met by itself.
- The requester adopts the similar greedy strategy in FTA to assign tasks, while using  $IPT_i$  to replace  $EPT_i$  in FTA.
- The requester will get a result  $\{J_1, \dots, J_i, \dots, J_n\}$ . Then, the requester assigns the tasks in  $J_i$  to user  $v_i$ , while keeping the remaining tasks (i.e., the tasks in  $J - J_i$ ) in hand.

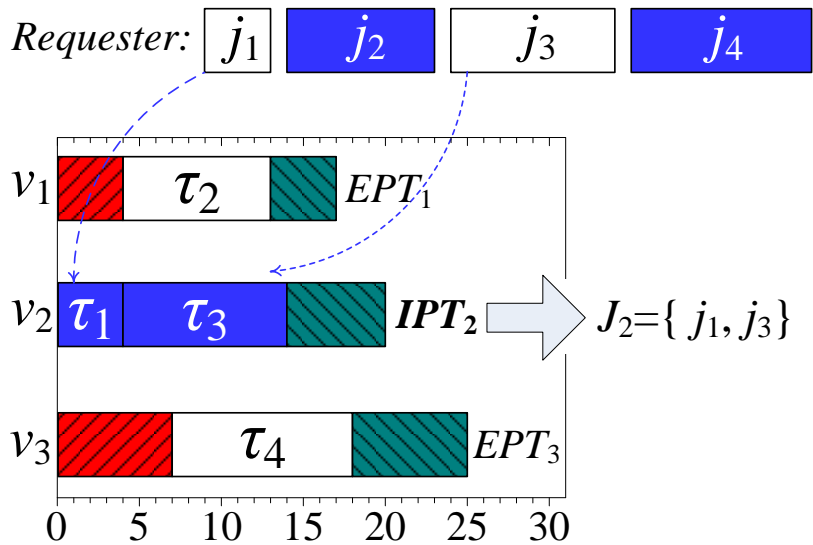
# Solution: oNline Task Assignment

- **Example**

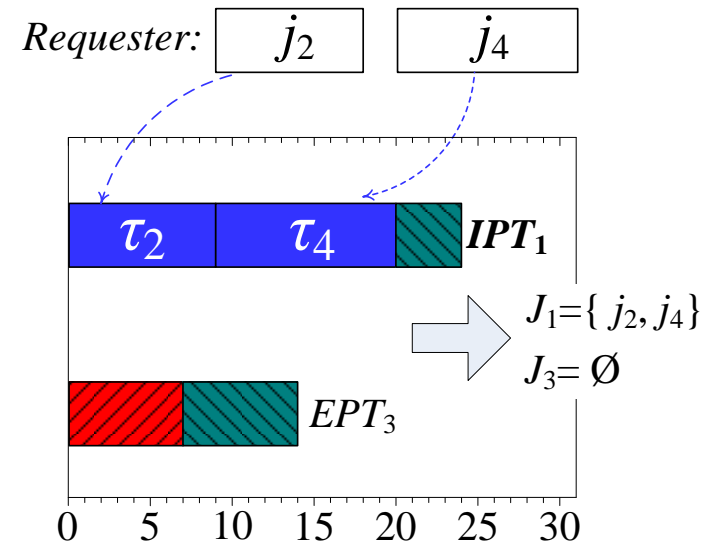


# Solution: oNline Task Assignment

## • Example



the requester determines  $J_2$  when it meets  $v_2$ :  $J_2 = \{j_1, j_3\}$



the requester determines  $J_1$  when it meets  $v_1$ :  $J_1 = \{j_2, j_4\}$

# Solution: oNline Task Assignment

## • The Detailed NTA Algorithm

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### Algorithm 2 The NTA Algorithm

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**Require:**  $J = \{j_1, j_2, \dots, j_m : \tau_1 \leq \tau_2 \leq \dots \leq \tau_m\}$ ,  
 $V = \{v_1, v_2, \dots, v_n : \lambda_1, \lambda_2, \dots, \lambda_n\}$ .

**Ensure:**  $\Pi_N = \{J_1, J_2, \dots, J_n\}$

**When the requester meets user  $v_i$  do**

```
1:  $IPT_i = \frac{1}{\lambda_i}$ ;  
2:  $J_i = \emptyset$ ;  
3:  $V = V - \{v_i\}$ ;  
4: for each other user  $v_l \in V$  do  
5:    $J_l = \emptyset$ ;  
6:    $EPT_l = \frac{2}{\lambda_l}$ ;  
7: for task  $j$  from  $j_1$  to  $j_m$  and  $j \in J$  do  
8:    $i_{min} = \operatorname{argmin}(\{IPT_i\} + \{EPT_l \mid v_l \in V\})$ ;  
9:   if  $i_{min} = i$  then  
10:    Assign task  $j$  to  $v_i$ :  $J_i = J_i + \{j\}$ ;  
11:     $IPT_i = IPT_i + \tau_i$ ;  
12:     $J = J - \{j\}$ ;  
13:   else  
14:     $J_{i_{min}} = J_{i_{min}} + \{j\}$ ;  
15:     $EPT_{i_{min}} = EPT_{i_{min}} + \tau_{i_{min}}$ ;  
16: return  $J_i$ ;
```

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The computation overhead is  $O(mn^2)$

# Solution: oNline Task Assignment

- **Performance analysis**

- **Theorem 5:** The NTA algorithm can achieve a smaller average makespan than FTA, i.e.,

$$AM(\Pi_N) \leq AM(\Pi_F^*)$$

- **Theorem 6:** Assume that there is a god, who can foresee at what time the requester will meet which user. Based on this, it can give an ideal optimal task assignment strategy  $\Pi_{OPT}$ . Then, we have:

$$AM(\Pi_N) - AM(\Pi_{OPT}) \leq \sum_{i=1}^n \frac{2}{\lambda_i} \quad \frac{AM(\Pi_N)}{AM(\Pi_{OPT})} \leq 1 + \frac{m \sum_{i=1}^n \frac{2}{\lambda_i}}{\sum_{j=1}^m \tau_j}$$

# Simulation

- **Algorithms in comparison**
  - *FTA, NTA, OPT*
  - Water Filling (*WF*) [Mobihoc'12]
  - Largest-First (*LF*)
- **Metrics**
  - Average makespan

# Simulation

- **Real Traces**

- **Statistics of traces**

Trace	Contacts	Length (hours)	Requester	Other users
Intel	2,766	99.8	9	128
Cambridge	6,732	145.6	12	223
Infocom	28,216	76.6	41	264
UMassDieselNet	227,657	95.3	4	36

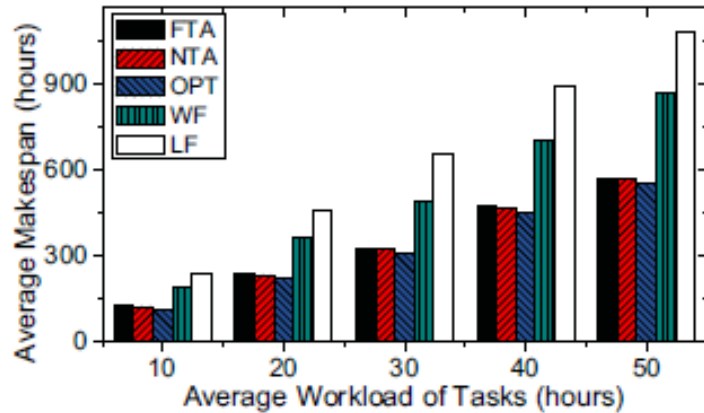
- **Other Settings**

Parameter name	Default value	Range
Number of tasks $m$	300	200-1000
Average workload $\tau$ (hours)	20	10-50

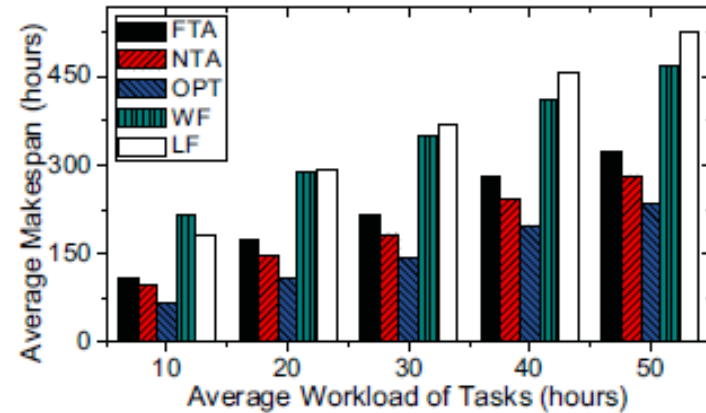


# Simulation

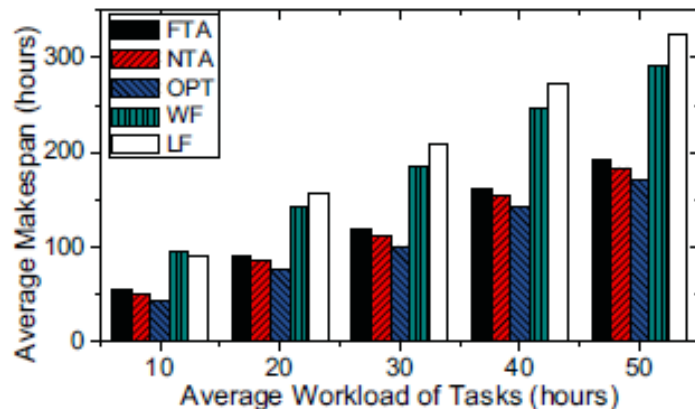
**Results:** average makespan vs. average workload



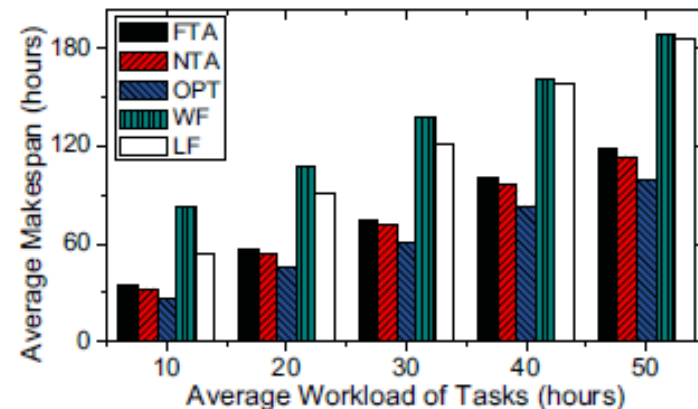
(a) Cambridge Haggles: Intel



(b) Cambridge Haggles: Cambridge



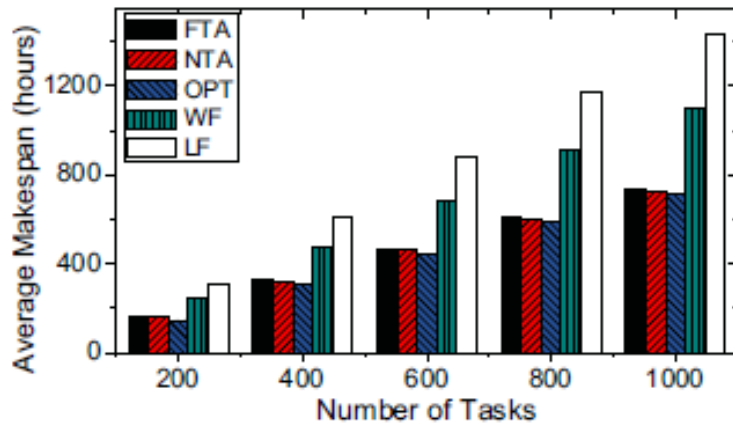
(c) Cambridge Haggles: Infocom



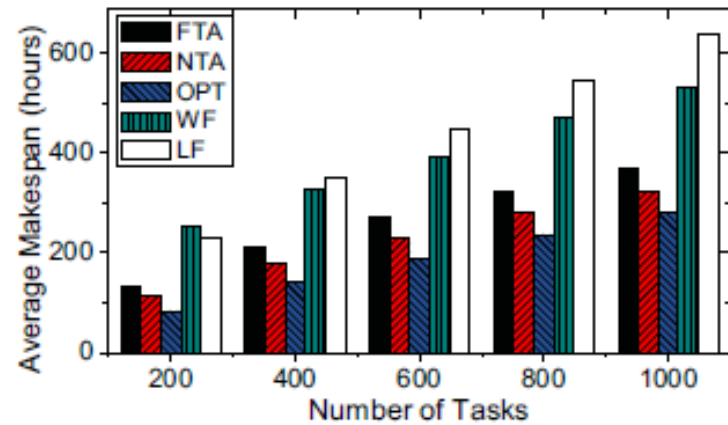
(d) UMassDieselNet

# Simulation

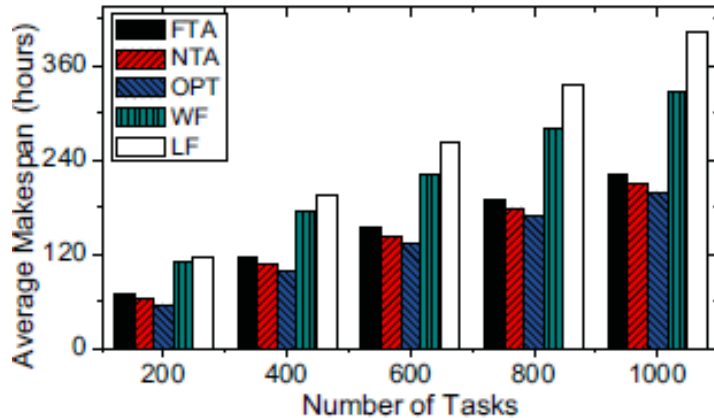
**Results:** average makespan vs. number of tasks



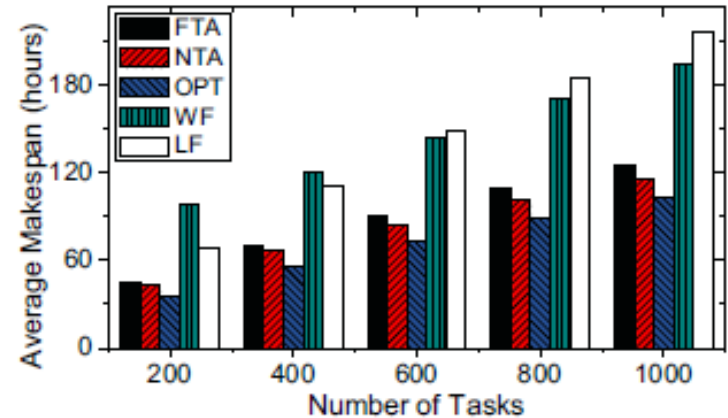
(a) Cambridge Haggles: Intel



(b) Cambridge Haggles: Cambridge



(c) Cambridge Haggles: Infocom



(d) UMassDieselNet

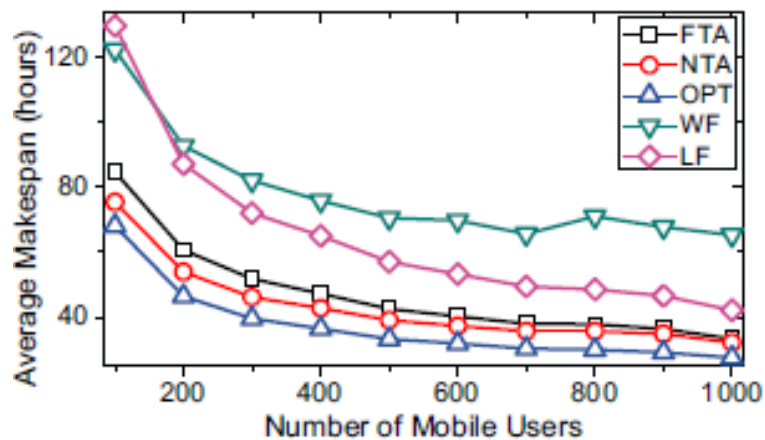
# Simulation

- **Synthetic Traces**

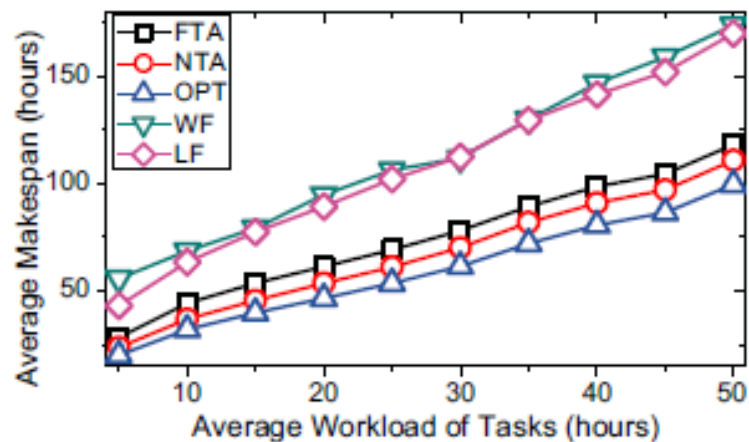
Parameter name	Default value	Range
Number of users $n$	400	100-1000
Number of requesters	5%	5%-10%
The average rate parameter $\lambda$	0.05	0.01-0.1
Number of tasks $m$	300	100-1000
The average workload	10	5 - 50

# Simulation

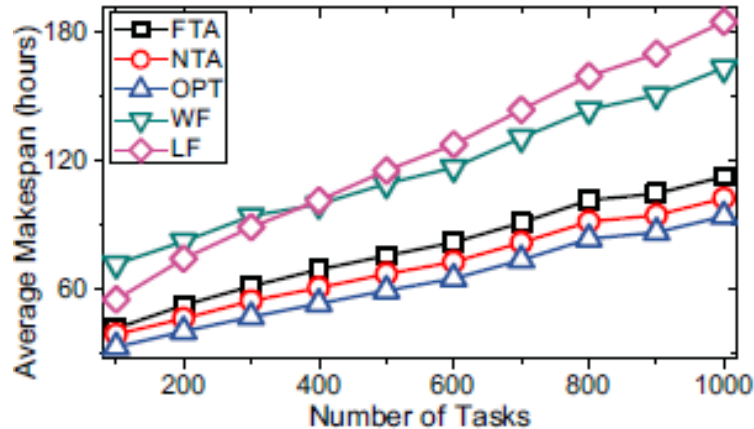
## Results:



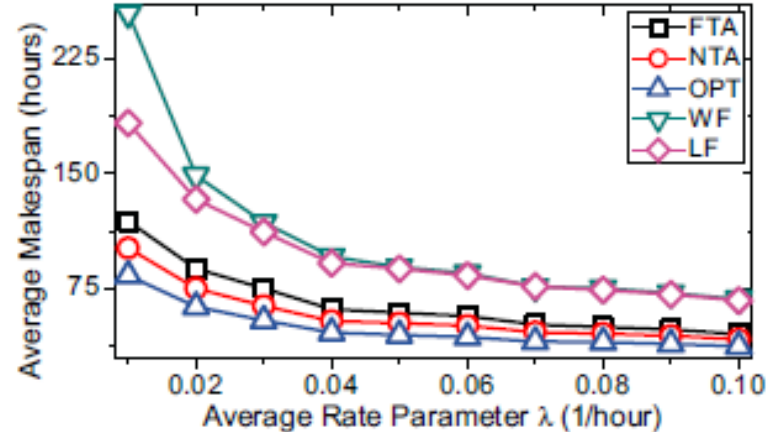
(a) Change the number of users



(b) Change the average workload



(c) Change the number of tasks



(d) Change the average rate parameter

# Conclusion

- FTA is the optimal offline task assignment algorithm
- NTA can achieve a smaller average makespan in the online decision case
- The absolute error of NTA mainly depends on the expected meeting time between the requester and other users. When the average expected meeting time is very small, our algorithm can even achieve the nearly optimal result.

**Thanks!**

**Q&A**