

lecture 20:
Header Space Analysis —
Static Checking For Networks
5590: software defined networking

anduo wang, Temple University
TTLMAN 401B, R 17:30-20:00

HSA

header space

- general and protocol agnostic
 - extend to new protocols and new types of checks (?)

statically check

- reachability properties
 - reachability failures, forwarding loops, traffic isolation and leakage

evaluation

- verify reachability between two subnets in 13 seconds

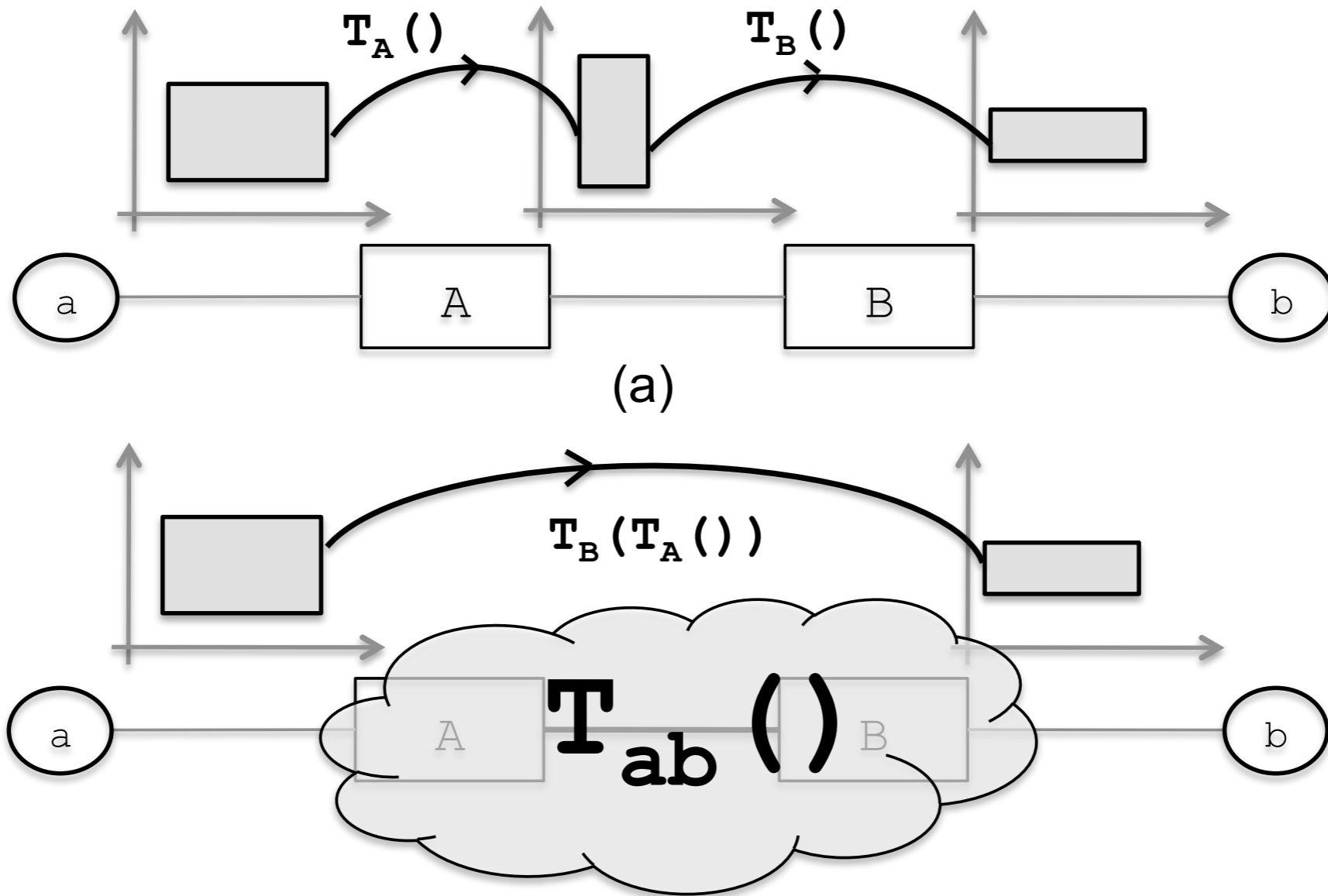
discussion (motivation)

debugging reachability is very time consuming

- complexity of the network state

HSA helps?

header space abstraction



header space abstraction

header space H

- $\{0,1\}^L$, where L is the header length
- a wildcard expression
 - sequence of L bits of $0, 1, \text{or } x$ (wildcard)
 - a region in header space: union of wildcard expressions

network space N

- $\{0,1\}^L \times \{1, \dots, P\}$, where $\{1, \dots, P\}$ is the list of ports

network transfer function

- a node transfer function $T: (h,p) \rightarrow \{(h_1, p_1), (h_2, p_2), \dots\}$

header space abstraction

network transfer function

- a node transfer function $T: (h,p) \rightarrow \{(h_1, p_1), (h_2, p_2), \dots\}$
- network transfer function

$$\Psi(h, p) = \begin{cases} T_1(h, p) & \text{if } p \in \text{switch}_1 \\ \dots & \dots \\ T_n(h, p) & \text{if } p \in \text{switch}_n \end{cases}$$

- topology transfer function

$$\Gamma(h, p) = \begin{cases} \{(h, p^*)\} & \text{if } p \text{ connected to } p^* \\ \{\} & \text{if } p \text{ is not connected.} \end{cases}$$

- multi-hop packet traversal

$$\Psi(\Gamma(\dots(\Psi(\Gamma(h, p)\dots)))$$

using header space abstraction

an IPv4 router that forwards subnet S_1 traffic to port p_1 , S_2 traffic to p_2 , and S_3 traffic to p_3

$$T_r(h, p) = \begin{cases} \{(h, p_1)\} & \text{if } ip_dst(h) \in S_1 \\ \{(h, p_2)\} & \text{if } ip_dst(h) \in S_2 \\ \{(h, p_3)\} & \text{if } ip_dst(h) \in S_3 \\ \{\} & \text{otherwise.} \end{cases}$$

set operation on H

header space algebra

- determine how different spaces overlap
- basic set operation
 - *intersection, union, complementation, difference*

set operation on H — *intersection*

$b_i \backslash b'_i$	0	1	x
0	0	z	0
1	z	1	1
x	0	1	x

examples

$$11000xxx \cap xx00010x = 1100010x$$

$$1100xxxx \cap 111001xx = 11z001xx = \phi$$

set operation on H — *union*

cannot be simplified

example

- $1111xxxx$ and $0000xxxx$

algorithm for logic minimization

- $10xx \cup 011x$ reduced to $b_4\bar{b}_3 \oplus \bar{b}_4b_3b_2$

set operation on H — *complementation*

```
 $h' \leftarrow \phi$   
for bit  $b_i$  in  $h$  do  
  if  $b_i \neq x$  then  
     $h' \leftarrow h' \cup x \dots x \overline{b_i} x \dots x$   
  end if  
end for  
return  $h'$ 
```

set operation on H — *complementation*

algorithm for computing complement for h :

$h' \leftarrow \phi$

for bit b_i in h **do**

if $b_i \neq x$ **then**

$h' \leftarrow h' \cup x \dots x \overline{b_i} x \dots x$

end if

end for

return h'

set operation on H — *complementation*

algorithm for computing complement for h :

$h' \leftarrow \phi$

for bit b_i in h **do**

if $b_i \neq x$ **then**

$h' \leftarrow h' \cup x \dots x \overline{b_i} x \dots x$

end if

end for

return h'

set operation on H — *complementation*

algorithm for computing complement for h :

$h' \leftarrow \phi$

for bit b_i in h **do**

if $b_i \neq x$ **then**

$h' \leftarrow h' \cup x \dots x \overline{b_i} x \dots x$

end if

end for

return h'

set operation on H — *complementation*

algorithm for computing complement for h :

$h' \leftarrow \phi$

for bit b_i in h **do**

if $b_i \neq x$ **then**

$h' \leftarrow h' \cup x \dots x \overline{b_i} x \dots x$

end if

end for

return h'

set operation on H — *complementation*

algorithm for computing complement for h :

$h' \leftarrow \phi$

for bit b_i in h **do**

if $b_i \neq x$ **then**

$h' \leftarrow h' \cup x \dots x \overline{b_i} x \dots x$

end if

end for

return h'

set operation on H — *complementation*

algorithm for computing complement for h :

$h' \leftarrow \phi$

for bit b_i in h **do**

if $b_i \neq x$ **then**

$h' \leftarrow h' \cup x \dots x \overline{b_i} x \dots x$

end if

end for

return h'

set operation on H — *complementation*

algorithm for computing complement for h :

```
 $h' \leftarrow \phi$   
for bit  $b_i$  in  $h$  do  
  if  $b_i \neq x$  then  
     $h' \leftarrow h' \cup x \dots x \overline{b_i} x \dots x$   
  end if  
end for  
return  $h'$ 
```

example

set operation on H — *complementation*

algorithm for computing complement for h :

```
 $h' \leftarrow \phi$   
for bit  $b_i$  in  $h$  do  
  if  $b_i \neq x$  then  
     $h' \leftarrow h' \cup x \dots x \overline{b_i} x \dots x$   
  end if  
end for  
return  $h'$ 
```

example

$$(100xxxx)' = 0xxxxxxx \cup x1xxxxxx \cup xx1xxxxx$$

set operation on H — *difference*

$A - B = A \cap B'$. For example:

$$\begin{aligned} &100xxxx - 10011xxx = \\ &100xxxx \cap (0xxxxxx \cup x1xxxxx \cup xx1xxxx \\ &\cup xxx0xxx \cup xxxx0xxx) \\ &= \phi \cup \phi \cup \phi \cup 1000xxxx \cup 100x0xxx \\ &= 1000xxxx \cup 100x0xxx. \end{aligned}$$

header space analysis — reachability

can packets from host a reach host b

$$R_{a \rightarrow b} = \bigcup_{a \rightarrow b \text{ paths}} \{T_n(\Gamma(T_{n-1}(\dots(\Gamma(T_1(h, p)\dots))))\}$$

header space analysis — reachability

can packets from host a reach host b

$$R_{a \rightarrow b} = \bigcup_{a \rightarrow b \text{ paths}} \{T_n(\Gamma(T_{n-1}(\dots(\Gamma(T_1(h, p)\dots))))\}$$

range reverse

If header $h \in \mathcal{H}$ reached b along the $a \rightarrow S_1 \rightarrow \dots \rightarrow S_{n-1} \rightarrow S_n \rightarrow b$ path, then the original header sent by a is:

$$h_a = T_1^{-1}(\Gamma(\dots(T_{n-1}^{-1}(\Gamma(T_n^{-1}((h, b))\dots))),$$

using the fact that $\Gamma = \Gamma^{-1}$.

header space analysis — reachability

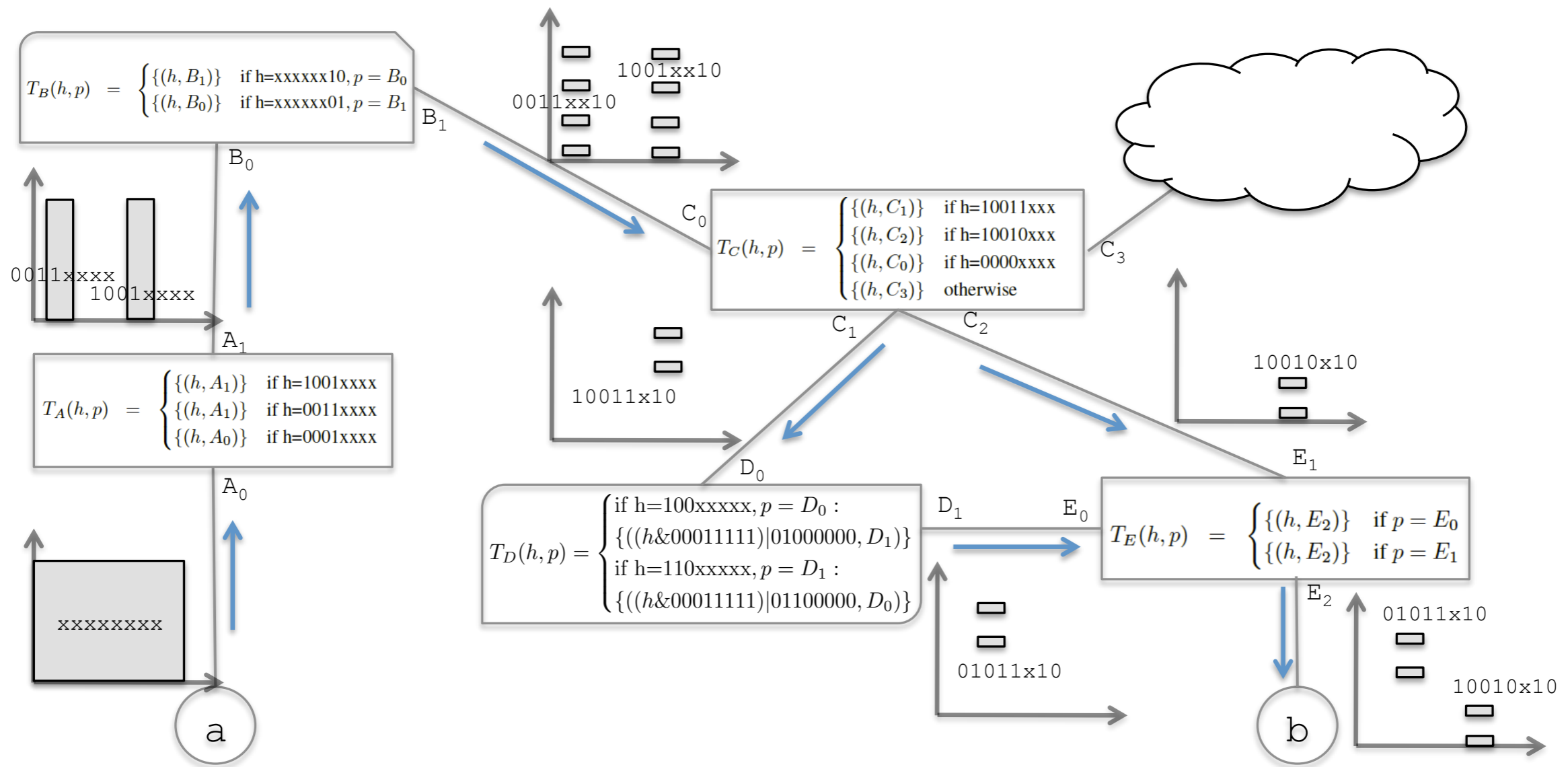


Figure 2: Example for computing reachability function from a to b . For simplicity, we assume a header length of 8 and show the first 4 bits on the x-axis and the last 4 bits on the y-axis. We show the range (output) of each transfer function composition along the paths that connect a to b . At the end, the packet headers that b will see from a are $01011x10 \cup 10010x10$.

header space analysis — reachability

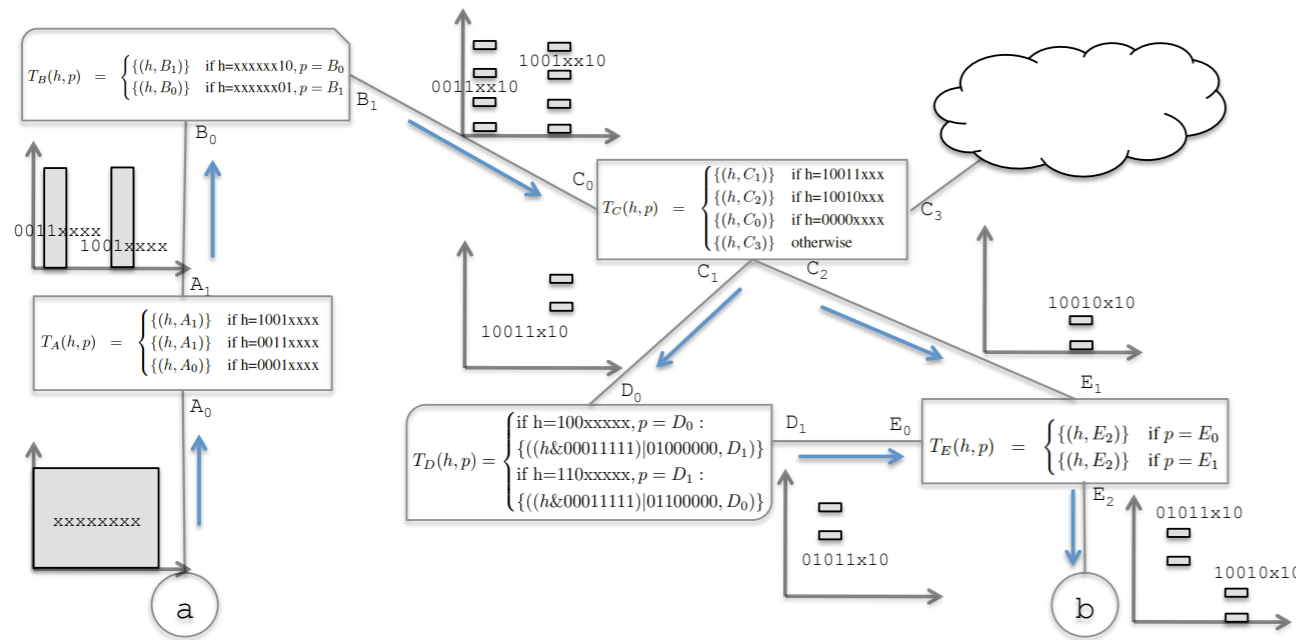


Figure 2: Example for computing reachability function from a to b . For simplicity, we assume a header length of 8 and show the first 4 bits on the x-axis and the last 4 bits on the y-axis. We show the range (output) of each transfer function composition along the paths that connect a to b . At the end, the packet headers that b will see from a are $01011x10 \cup 10010x10$.

$$R_{a \rightarrow b}(h, p) = \begin{cases} \text{if } h=10010x10, p = A_0 : \\ \{(h, E_2)\} \\ \text{if } h=10011x10, p = A_0 : \\ \{((h \& 00011111) | 01000000, E_2)\} \end{cases}$$

header space analysis — reachability

worst case complexity

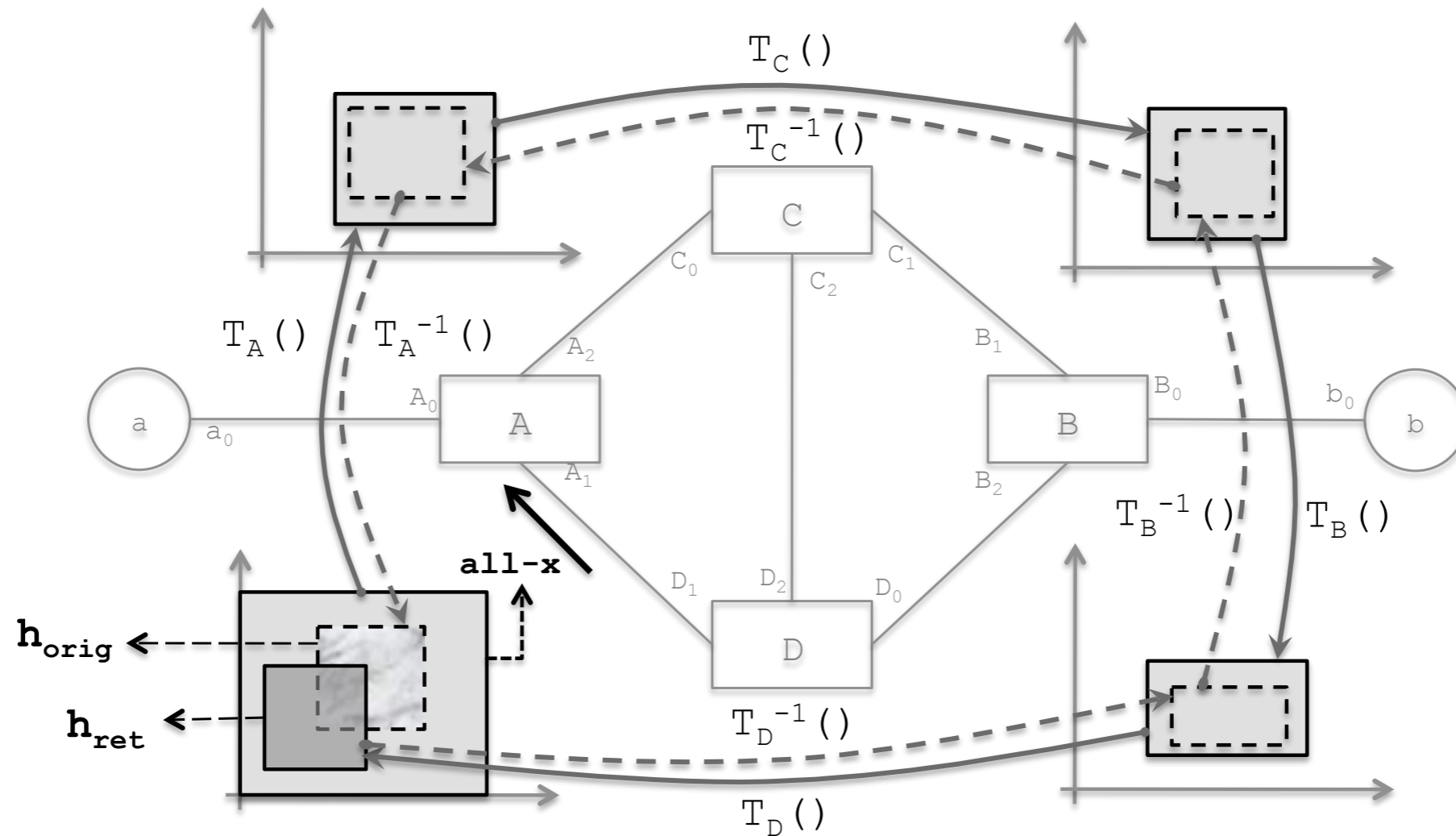
- assume input of
 - R_1 wildcard expressions, R_2 transfer function rules
- output $O(R_1 R_2)$ wildcard expressions

linear fragmentation assumption

- as packet propagates to the core of the network, the match pattern will be less specific
- cR rather than R^2 where $c \ll R$
- running time becomes $O(dR^2)$
 - d is the network diameter
 - R is the maximum number of forwarding rules in a router

brute force: $O(2^L)$

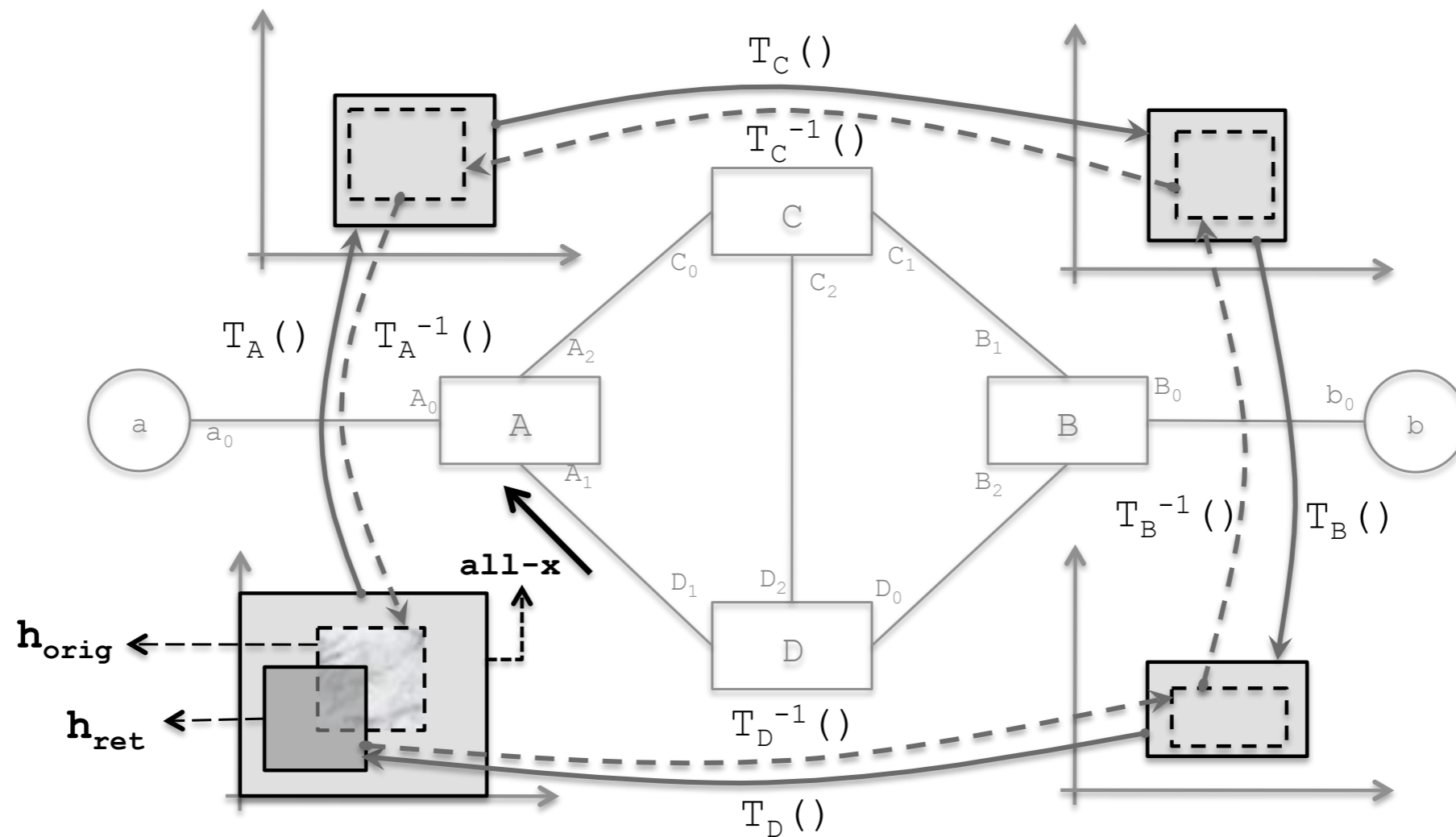
header space analysis — loop



catch loop

- inject an all-x test packet header from each port and track the packet

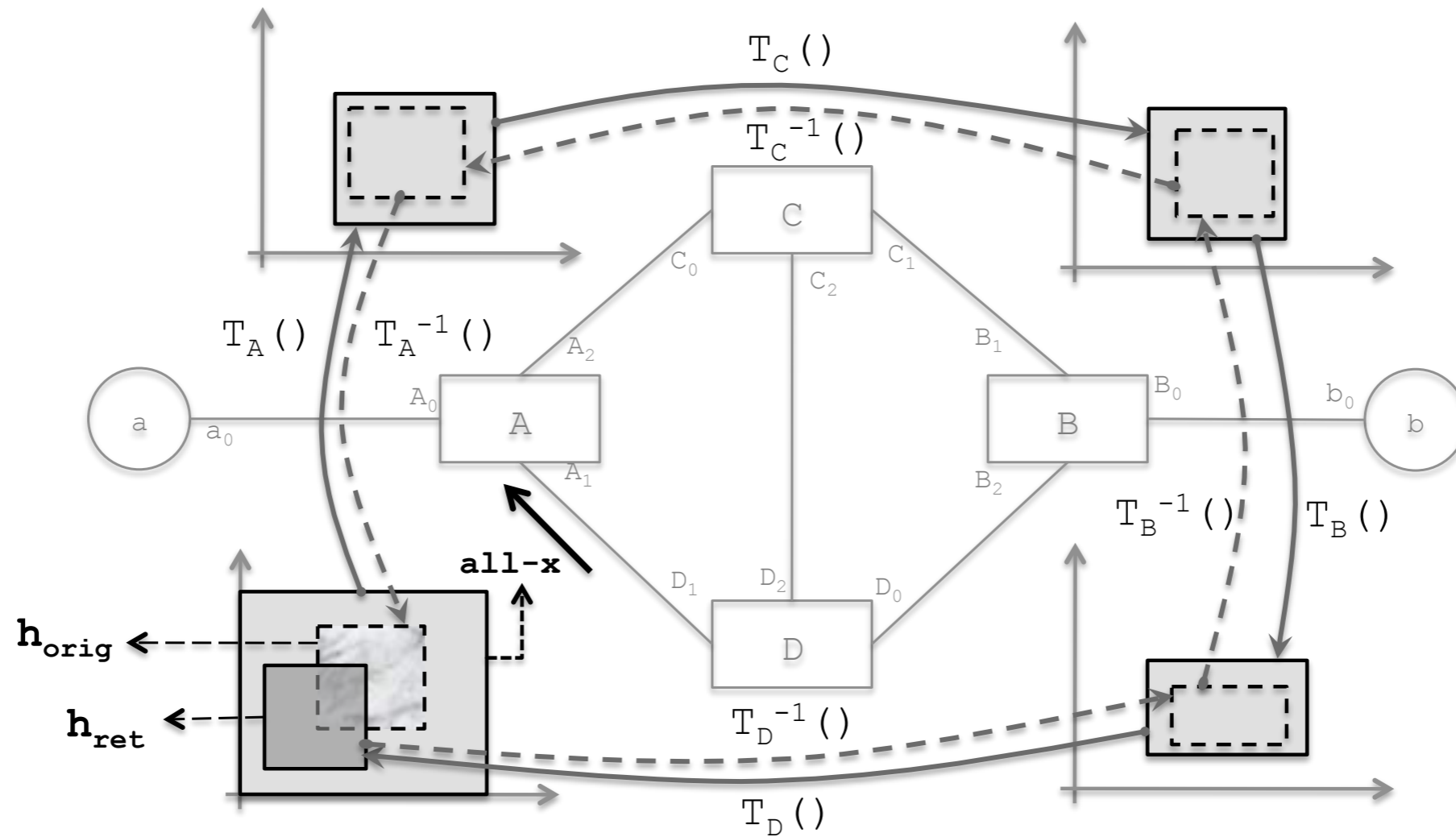
header space analysis — loop



finite loop

- $h_{ret} \cap h_{orig} = \emptyset$

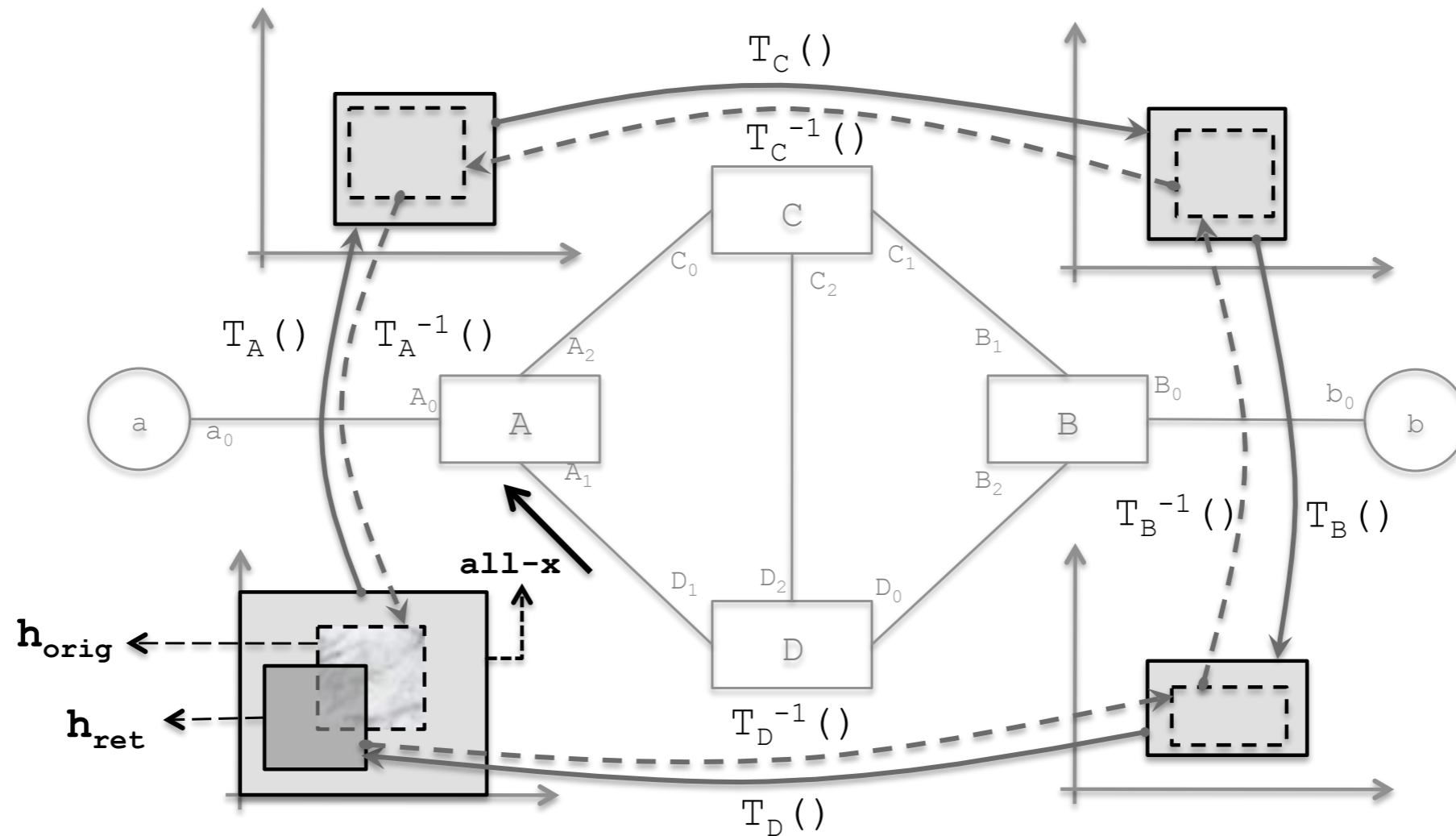
header space analysis — loop



infinite loop

— $h_{ret} \subseteq h_{orig}$

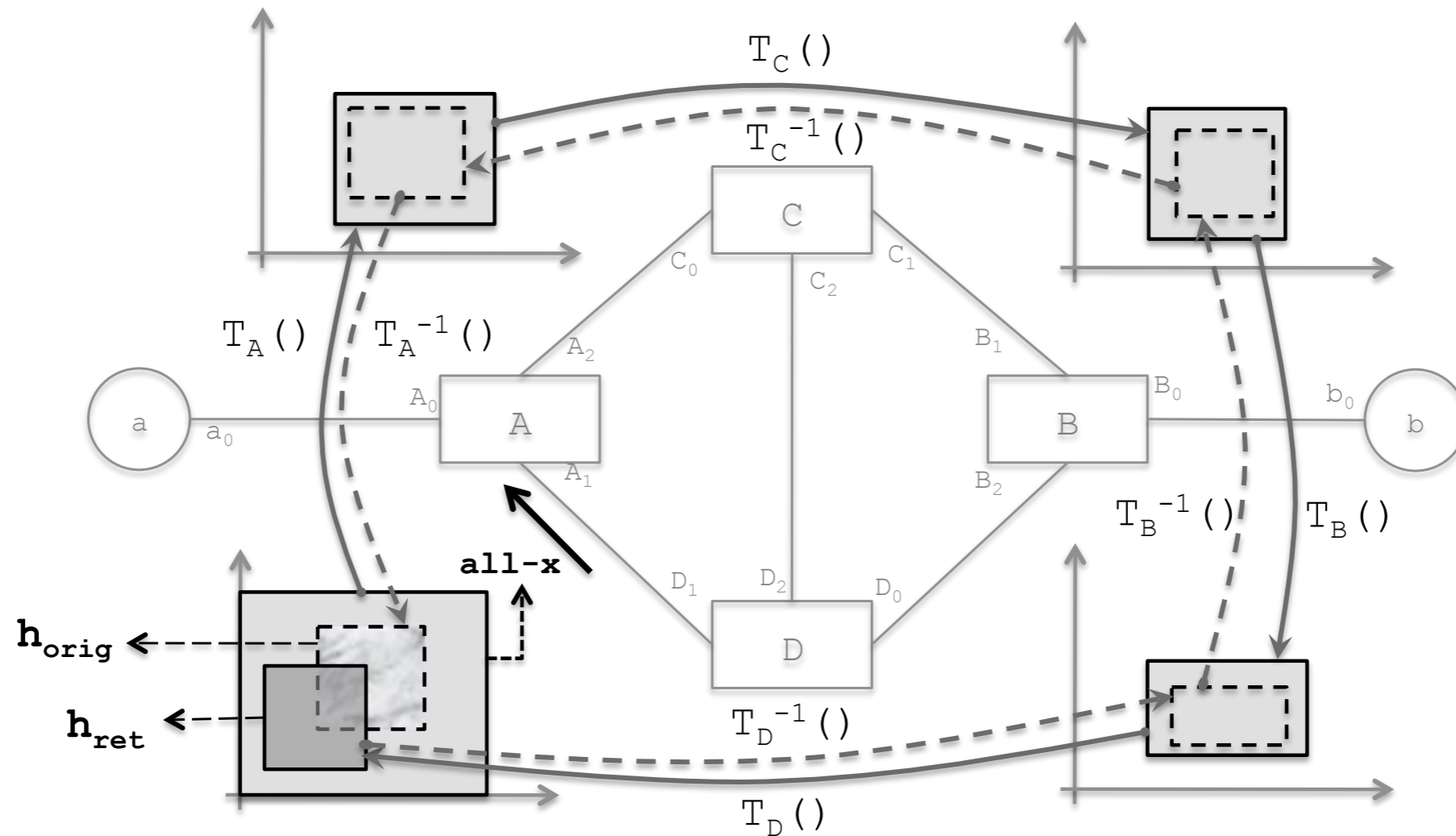
header space analysis — loop



mixed (finite and infinite)

- neither $(h_{ret} \subseteq h_{orig})$ or $h_{ret} \cap h_{orig} = \emptyset$
- $h_{ret} - h_{orig}$ is finite loop
- examine $h_{ret} \cap h_{orig}$

header space analysis — loop



examine $h_{ret} \cap h_{orig}$

- redefine $h_{ret} := h_{ret} \cap h_{orig}$, repeat until either finite or infinite
- at most 2^L iterations

header space analysis — slice isolation

two slices, a and b with regions N_a, N_b

$$N_a = \{(\alpha_i, p_i) \mid p_i \in \mathcal{S}\} \quad , \quad N_b = \{(\beta_i, p_i) \mid p_i \in \mathcal{S}\}$$

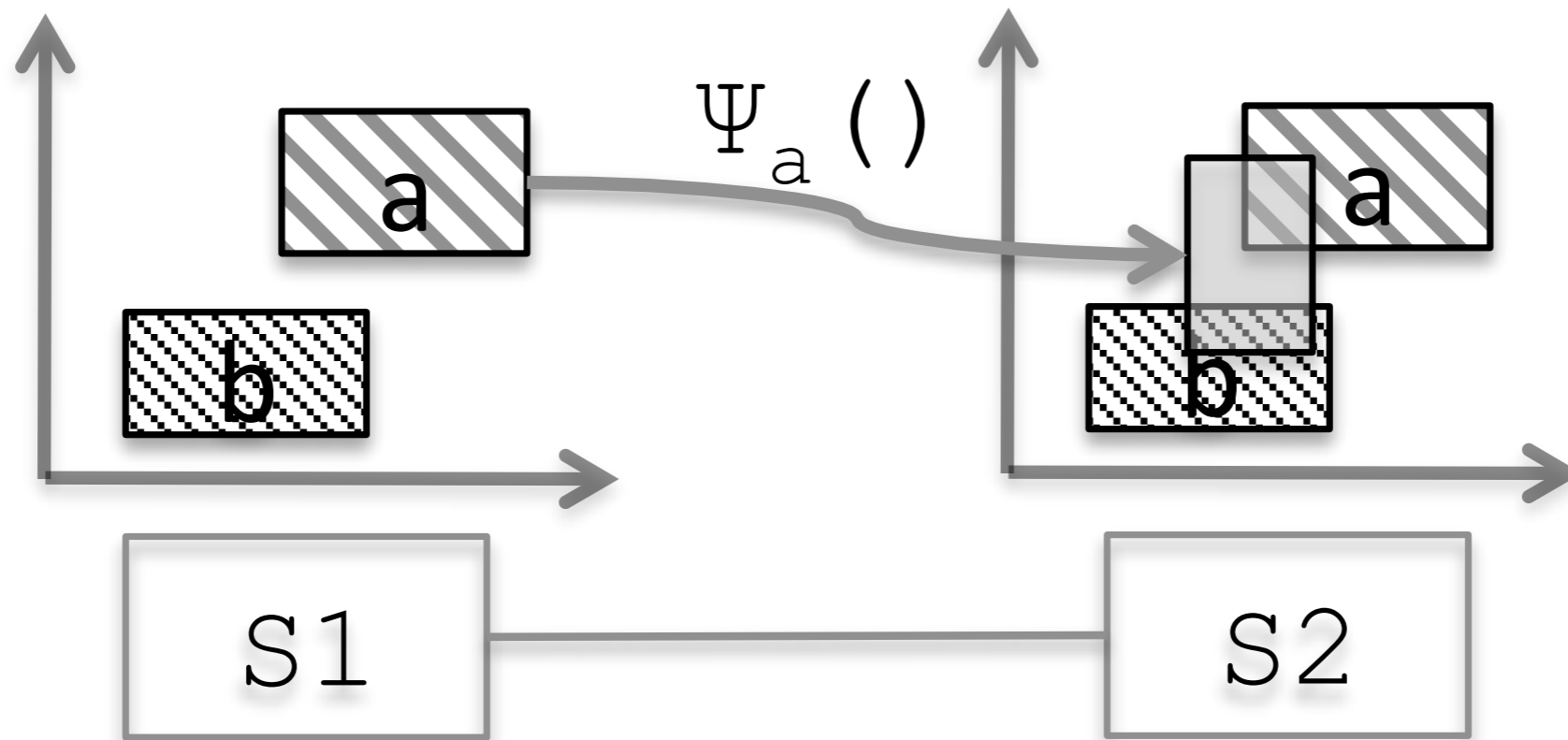
isolated $\alpha_i \cap \beta_i = \phi$

intersection

$$N_a \cap N_b = \{(\alpha_i \cap \beta_i, p_i) \mid p_i \in N_a \& p_i \in N_b\}$$

header space analysis — slice isolation

detecting leakage



discussion

HSA is really just

- simulation + equivalence class optimization

header space analysis — loop

can packets from host a reach host b

$$R_{a \rightarrow b} = \bigcup_{a \rightarrow b \text{ paths}} \{T_n(\Gamma(T_{n-1}(\dots(\Gamma(T_1(h, p)\dots))))\}$$