

## CIS 2166

### HW 2 for Matrix Algebra part 2

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix}, B = \begin{bmatrix} 4 & 3 & 2 \\ 2 & 3 & 4 \end{bmatrix}, C = \begin{bmatrix} 5 \\ 4 \\ 3 \end{bmatrix}, D = \begin{bmatrix} 2 & 1 & 0 \\ 4 & 3 & 3 \\ -6 & 2 & 1 \end{bmatrix}, E = \begin{bmatrix} 2 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{bmatrix}, F = \begin{bmatrix} 2 & 1 & 0 \\ 4 & 3 & 3 \\ -6 & -2 & 3 \end{bmatrix},$$

1. Use method of Gaussian elimination to find  $x$  for the system of linear equations  $E*x=C$ . Solve by hand.
2. Use method of Gaussian elimination to find  $x$  for the system of linear equations  $F*x=C$ . Solve by hand.
3. What is rank of matrices  $A$ ,  $B$ ,  $D$  and  $F$ ? Hint: use Gaussian elimination.
4. Use method of Gaussian elimination to find inverse of matrix  $D$ ,  $E$ ,  $F$ . Solve by hand.
5. Compute  $\text{Tr}(D)$  (trace of matrix  $D$ ),  $\text{Tr}(A)$
6. Find the determinants of  $D$ ,  $E$ ,  $F$  using the Sarrus formula.
7. Use method of Gaussian elimination to find  $\det(D)$ ,  $\det(E)$ ,  $\det(F)$ . Solve by hand.
8. If  $A$  and  $B$  are any symmetric matrices ( $A^T=A$ ,  $B^T=B$ ), show that  $A*B=(B*A)^T$