

CIS 2166

HW 13: Matrix Algebra part 2

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix}, B = \begin{bmatrix} 4 & 3 & 2 \\ 2 & 3 & 4 \end{bmatrix}, C = \begin{bmatrix} 5 \\ 4 \\ 3 \end{bmatrix}, D = \begin{bmatrix} 2 & 1 & 0 \\ 4 & 3 & 3 \\ -6 & 2 & 1 \end{bmatrix}, E = \begin{bmatrix} 2 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{bmatrix}, F = \begin{bmatrix} 2 & 1 & 0 \\ 4 & 3 & 3 \\ -6 & -2 & 3 \end{bmatrix},$$

1. Use method of Gaussian elimination to find x for the system of linear equations $E*x=C$. Solve by hand.
2. Use method of Gaussian elimination to find x for the system of linear equations $F*x=C$. Solve by hand.
3. What is rank of matrices A , B , D and F ? Hint: use Gaussian elimination.
4. Use method of Gaussian elimination to find inverse of matrix D , E , F . Solve by hand.
5. Compute $\text{Tr}(D)$ (trace of matrix D), $\text{Tr}(A)$
6. Find the determinants of D , E , F using the Sarrus formula.
7. Use method of Gaussian elimination to find $\det(D)$, $\det(E)$, $\det(F)$. Solve by hand.
8. If A and B are any symmetric matrices ($A^T=A$, $B^T=B$), show that $A*B=(B*A)^T$