



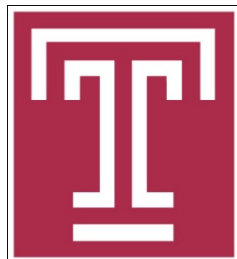
# On Balancing Middlebox Set-up Cost and Bandwidth Consumption in NFV

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# 1. Introduction of Middlebox

- Network Function Virtualization (NFV)
  - Technology of virtualizing network functions into software building blocks
- **Middlebox**: software implementation of network services
  - Improve the network performance:
    - Web proxy and video transcoder, load balancer, ...
  - Enhance the security:
    - Firewall, IDS/IPS, passive network monitor, ...
- Examples



Web Proxy



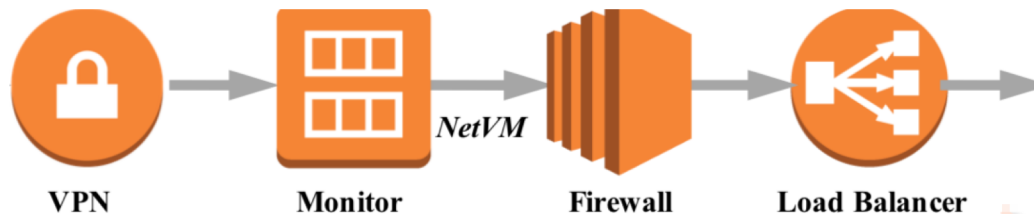
Firewall



NAT

# Middlebox Dependency Relations [1]

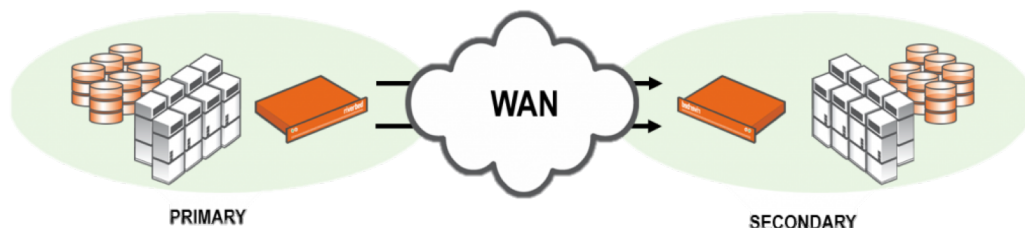
- Multiple middleboxes may/may not have a serving order
  - Examples
    - Firewall usually before Proxy
    - Virus scanner either before or after NAT gateway
- Categories
  - Non-ordered middlebox set
  - Totally-ordered middlebox set (**service chain**)



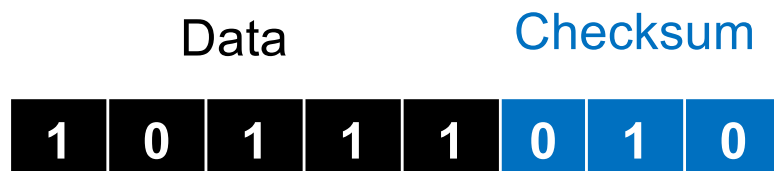
- Partially-ordered middlebox set

# Middlebox Traffic Changing Effects [2]

- Middleboxes may change **flow rates** in different ways
  - Citrix CloudBridge WAN accelerator: 20% (diminishing)



- BCH(63,48) encoder: 130% (expanding)



# Middlebox Placement Overview

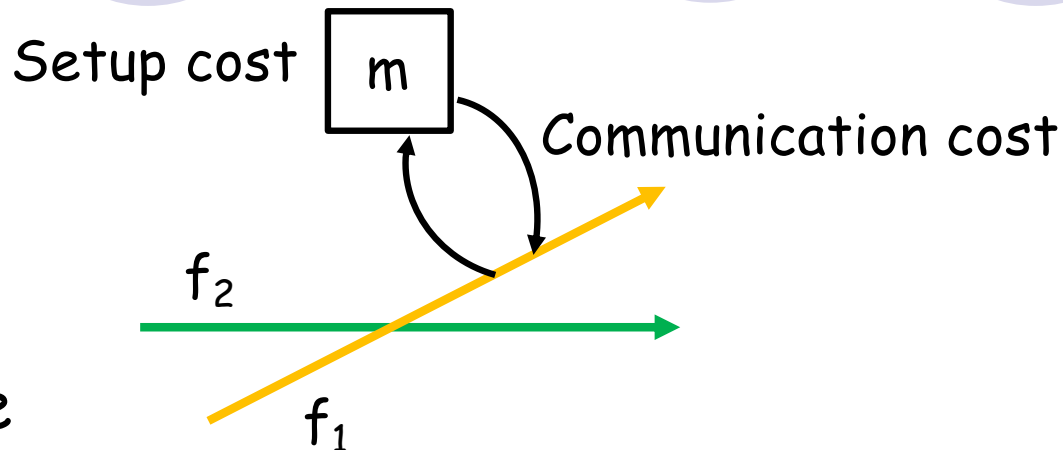
- Problem
  - Placing middleboxes to satisfy all flows' middlebox service requests
- Objectives:
  - Minimizing middlebox setup cost [3]
  - Minimizing bandwidth consumption [2]
- Constraints
  - Dependency relations
  - Traffic-changing effects
  - Vertex capacity and middlebox processing volume

[2] Traffic Aware Placement of Interdependent NFV Middleboxes (INFOCOM '17)

[3] Provably Efficient Algorithms for Joint Placement and Allocation of Virtual Network (INFOCOM '17)

# A Middlebox Placement Model [4]

- Cost



- Objective

- Minimizing sum of middlebox setup cost and communication cost

- Two special cases

- Facility location problem

- Single middlebox placement

- Generalized assignment problem

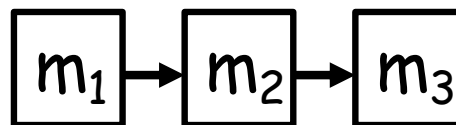
- Each middlebox has a limited processing volume
- Placing middleboxes and assigning to flows

# A Service Chain Model [2]

- Objective
  - Minimizing the total bandwidth consumption
- Solutions
  - Consider traffic-changing effects
  - Place middleboxes for a single flow



Non-ordered  
(Optimal greedy: sort  
traffic-changing ratios  
in increasing order)



Totally-ordered  
(Optimal DP: latter  
middleboxes must be  
after front ones)



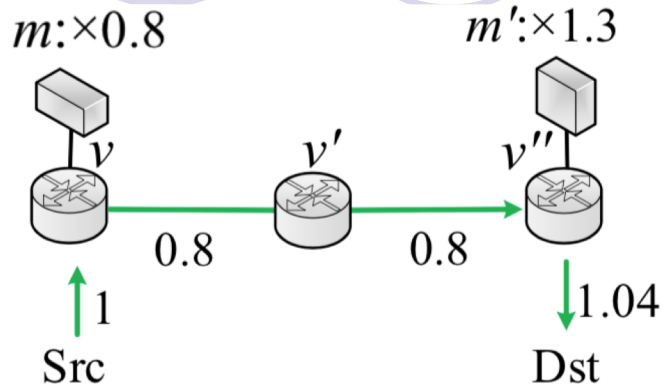
Partially-ordered  
(NP-hard: reduced  
from the Clique Problem)

## 2. Our Model

- Problem
  - Placing middleboxes to satisfy all flows' network service requests
- Network service requests
  - Multiple middleboxes
    - Middlebox set with or without dependency relations
- Cost
  - Middlebox setup
    - Sum of middlebox setup cost
  - Bandwidth consumption
    - Sum of each flow's bandwidth consumption cost on each link
- Objective
  - Minimizing total cost of middlebox setup and bandwidth consumption

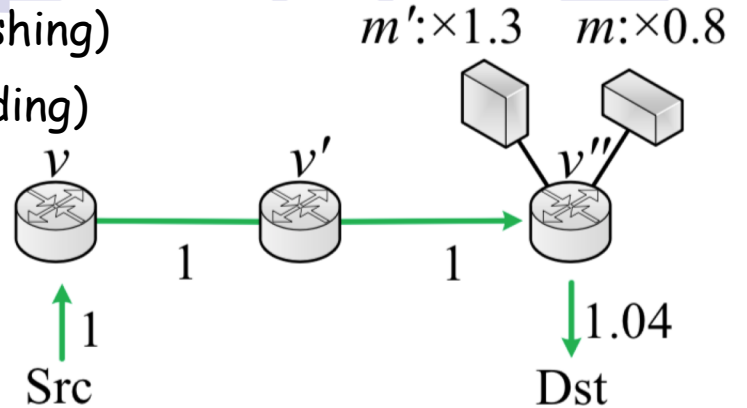


# A Motivating Example

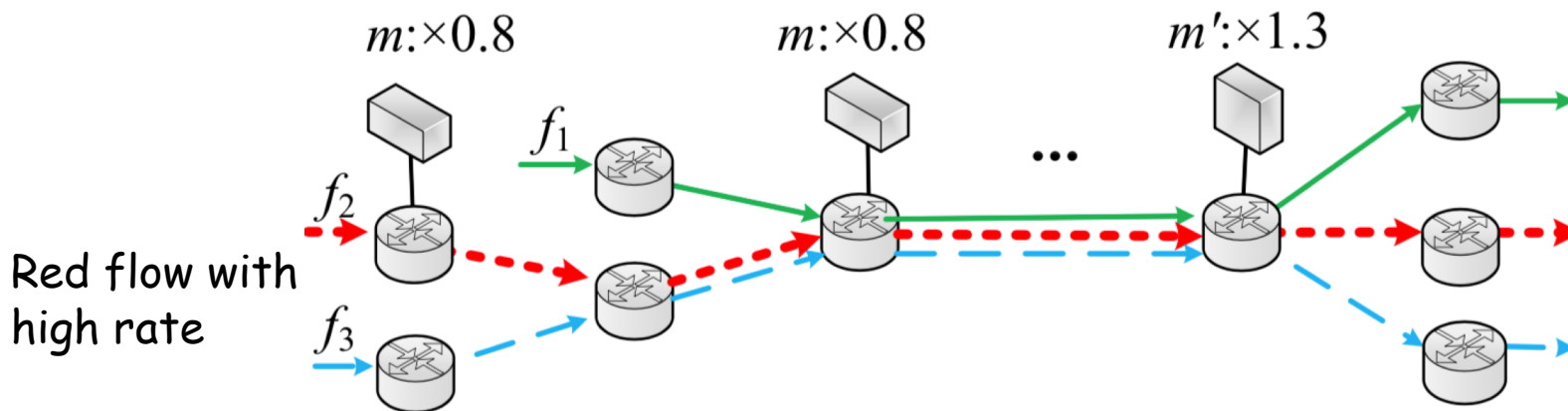


Independent middleboxes

$m: 0.8$  (diminishing)  
 $m': 1.3$  (expanding)



Dependent middleboxes:  $m'$  before  $m$



A flow covered by **multiple middleboxes**

(Multiple coverage: when additional setup cost is less than the reduced bandwidth consumption cost)

# 3. Problem Formulation

- Middlebox setup cost

- $$c_1 = \sum_{m \in M} \sum_{v \in V} c_m$$

- $c_m$ : unit setup cost of middlebox  $m$

- Bandwidth consumption cost

- $$c_2 = \sum_{f \in F} \sum_{e \in p_f} w(b_f^e)$$

- $w(b_f^e)$ : bandwidth cost function of flow  $f$  on link  $e$

- $$b_f^e = r_f \prod_m \lambda_m$$

- $r_f$ : initial traffic rate of flow  $f$
- $\lambda_m$ : traffic-changing ratio of middlebox  $m$

- Objective

- Minimizing  $c_1 + c_2$

# Problem Formulation (cont'd)

- Translog bandwidth cost function on each link

$$w(b_f^e) = \log(b_f^e) = \log(r_f \prod \lambda_m) = \log(r_f) + \sum \log(\lambda_m)$$

- Reasons
  - Widely used in Cisco EIGRP and OSPF protocols
  - Log-linear for easy calculation
- The weight of setup cost and bandwidth consumption
  - Adjusting the traffic-changing ratios and unit setup costs of middleboxes

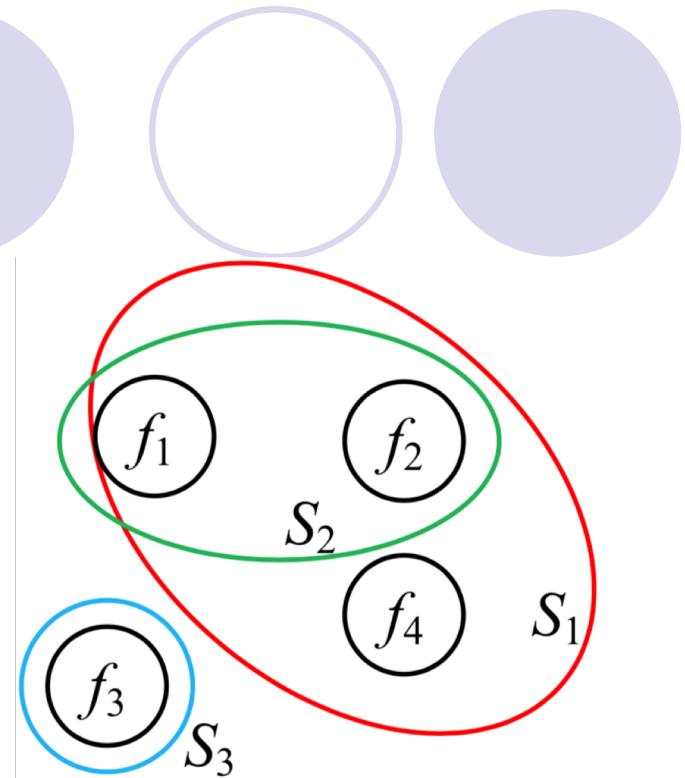
# Problem Complexity

## NP-hard

- Even with no traffic-changing effects
- Even when placing a single middlebox

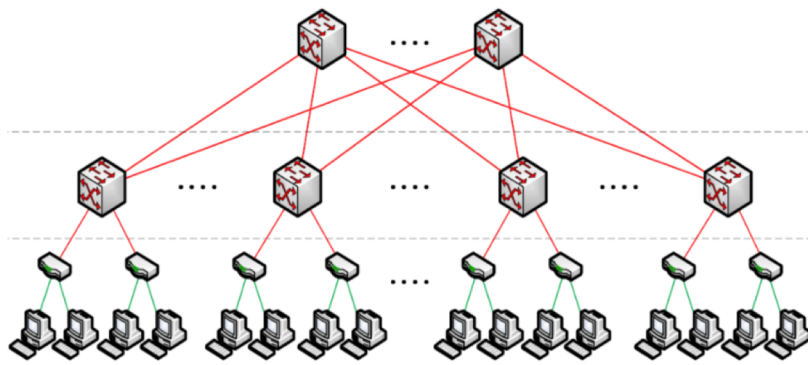
## Proof

- Reduction from set-cover problem
- Use minimum number of middleboxes to "cover" all flows
  - Flows as elements:  $F = \{f_1, f_2, \dots, f_{|F|}\}$
  - Placed middleboxes as sets:  $\{S_1, S_2, \dots\}$
  - $S_1 = \{f_1, f_2, f_4\}$ ,  $S_2 = \{f_1, f_2\}$ ,  $S_3 = \{f_3\}$



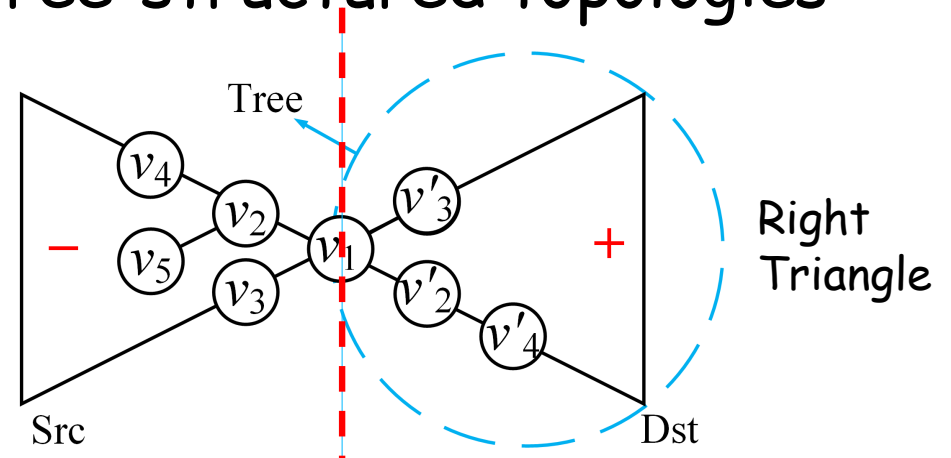
# Problem Complexity (cont'd)

- In this paper, we focus on tree-structured topologies



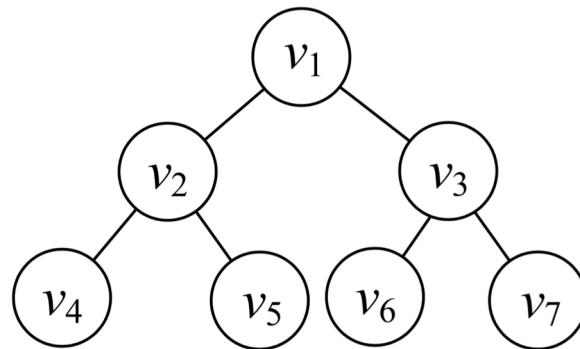
Tree-based data centers

Left Triangle

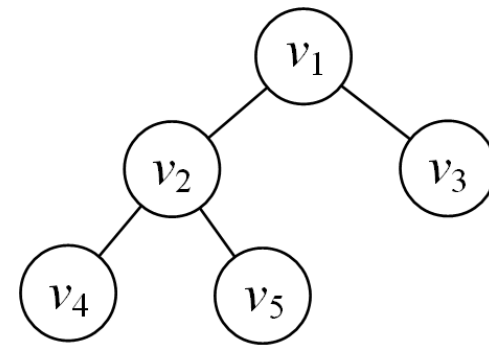


Hierarchical data centers

Each triangle is mostly a perfect or complete tree



Perfect tree



Complete tree

# 4. Placing a Single Middlebox

## Solution

- Local Greedy Algorithm (*LGA*)

## Steps

- Calculate each total cost of placing middleboxes in a whole level
- Select the level with the minimum total cost
- Iterative implementation
  - From top level to bottom, total costs will decrease and then increase
  - Select the level with the local minimum

## 4. Placing a Single Middlebox (cont'd)

Time complexity ( $|V|$ : #node)

- $O(|V|)$

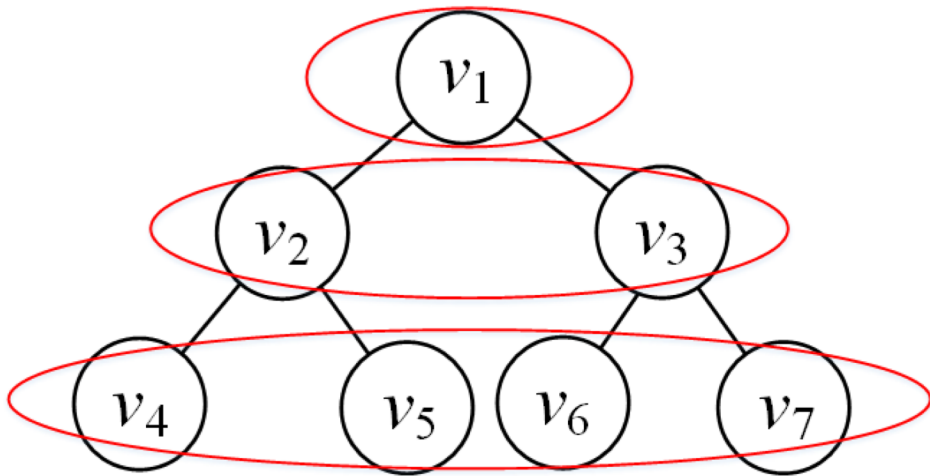
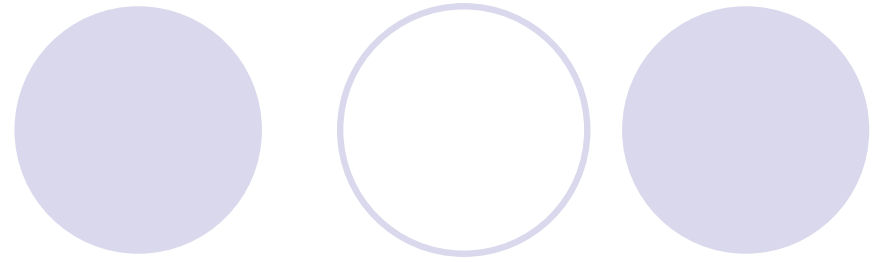
Optimal for perfect tree topologies

- Symmetry of placement
- No multiple "coverage" situation

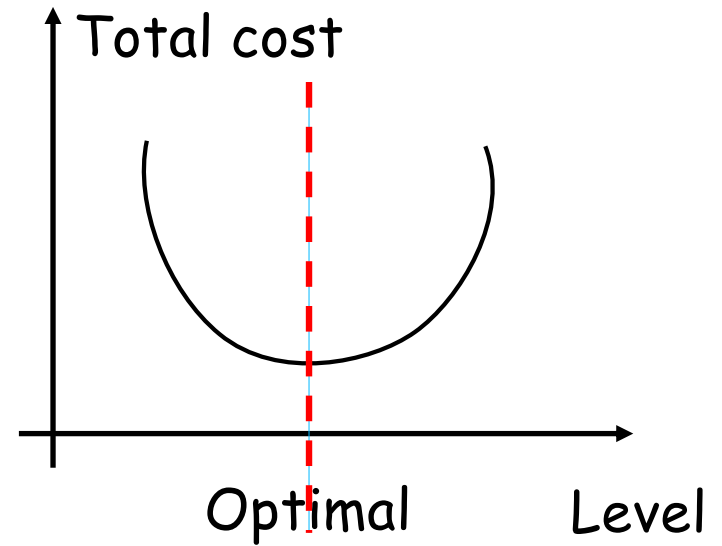
Also optimal for complete tree topologies

- Also multiple "coverage" situation
- The most unbalanced traffic distribution: left and right subtrees of root have a depth difference of 1

# Illustration



Calculate level by level





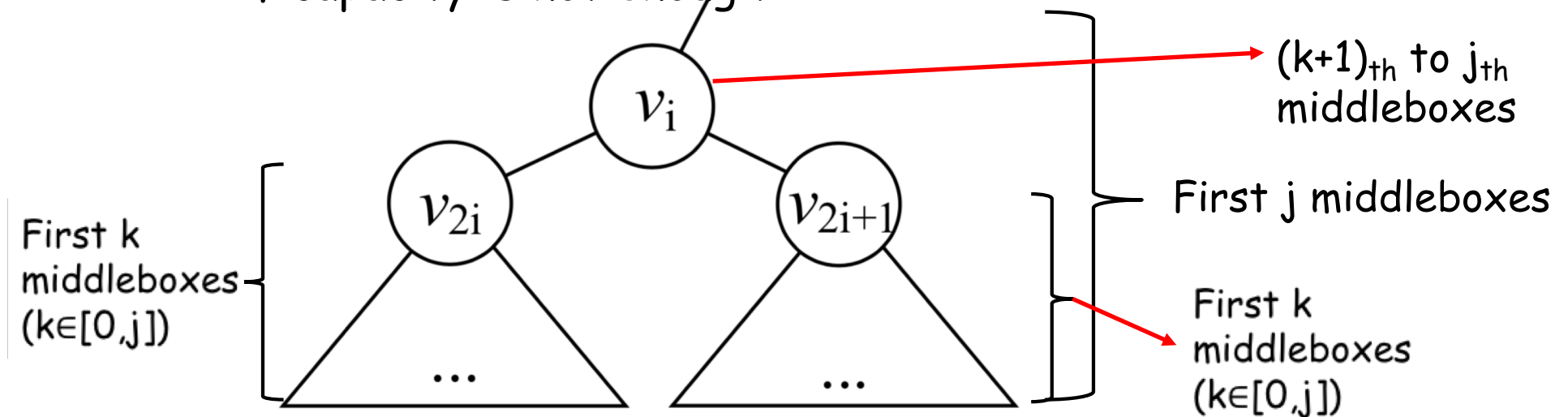
# 5. Placing Multiple Middleboxes

## Non-ordered middlebox set placement

- Solution
  - Combined Local Greedy Algorithm (**CLGA**)
- Insight
  - Place each middlebox independently by applying LGA
- Time complexity ( $|V|$ : #node,  $|M|$ : #middlebox)
  - $O(|V||M|)$
- Optimal for complete trees

# Totally-ordered Middlebox Set Placement

- Solution: Dynamic Programming (DP)
- Works for infinite and finite vertex capacity
- $OPT(i, j)$ 
  - Minimum cost of subtree with root  $v_i$  when placing first  $j$  middleboxes in the set
  - $\infty$  if capacity is not enough



# Dynamic Programming Formulation

- Left triangle

$$\text{OPT}(i, j) = \begin{cases} \min_{0 \leq k \leq j} \{ \text{OPT}(2i, k) + \text{OPT}(2i + 1, k) \\ + \sum_{k < l \leq j} c_l + \lfloor \log i \rfloor \sum_{k < l \leq j} \lambda_l \}, & 1 \leq i \leq \lfloor \frac{n}{2} \rfloor. \\ \sum_{0 \leq l \leq j} c_l + \lfloor \log i \rfloor r_f, & \lfloor \frac{n}{2} \rfloor < i \leq n. \\ \infty & \text{if not enough node capacity.} \\ 0 & \text{otherwise.} \end{cases}$$

The diagram illustrates the components of the DP formulation. Arrows point from the following parts of the equation to callouts:
 

- From  $\text{OPT}(2i, k) + \text{OPT}(2i + 1, k)$  to "Left subtree".
- From  $\sum_{k < l \leq j} c_l + \lfloor \log i \rfloor \sum_{k < l \leq j} \lambda_l$  to "Right subtree".
- From  $\sum_{0 \leq l \leq j} c_l + \lfloor \log i \rfloor r_f$  to "Bandwidth consumption".
- From the "otherwise." case to "Newly placed middleboxes".

- Right triangle

- Similar to the left triangle's formulation

# An Example

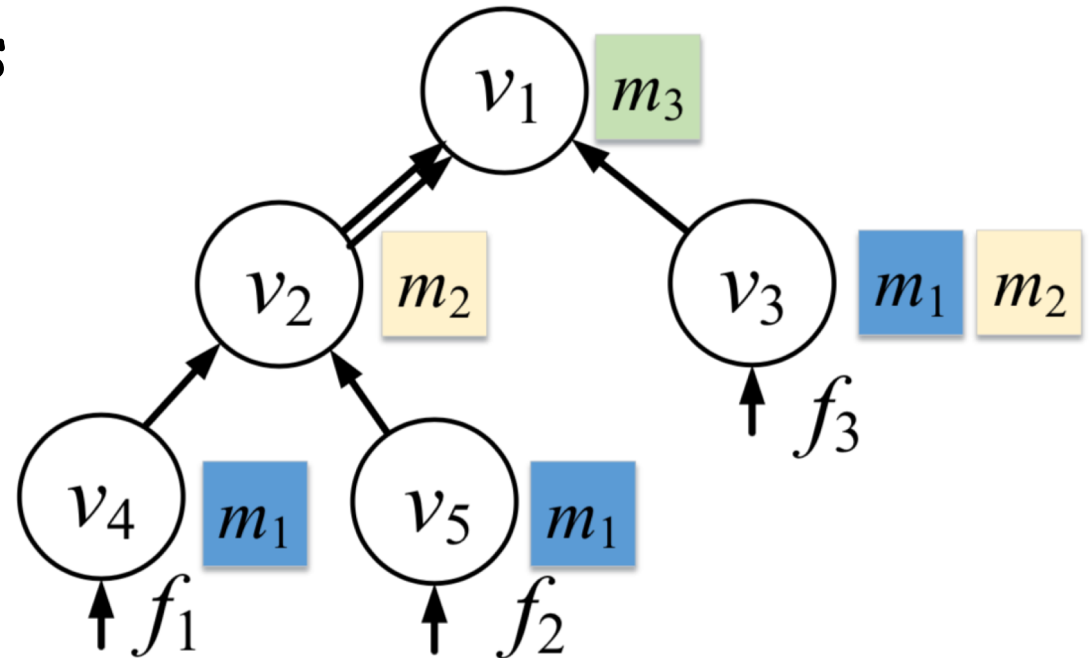
|                        | $m_1$ | $m_2$ | $m_3$ |
|------------------------|-------|-------|-------|
| Traffic-changing ratio | 0.5   | 0.8   | 1.1   |
| Setup cost             | 0.2   | 0.4   | 0.3   |

- Dependency relations

- $m_1 \rightarrow m_2 \rightarrow m_3$

- Initial traffic rate

- $r_1 = r_2 = r_3 = 1$



# Totally-ordered Middlebox Set Placement (cont'd)



## Insights

- The optimal placement with root  $v_i$  by placing first  $j$  and its two subtrees by placing no more than  $j$  middleboxes

## Perfect tree

- Transformed to a line
- Similar to a single flow placement

## Complete tree

- No multiple "coverage" situation

Time complexity ( $|V|$ : #node,  $|M|$ : #middlebox)

- $O(|V||M|^3)$

# Partially-ordered Middlebox Set Placement

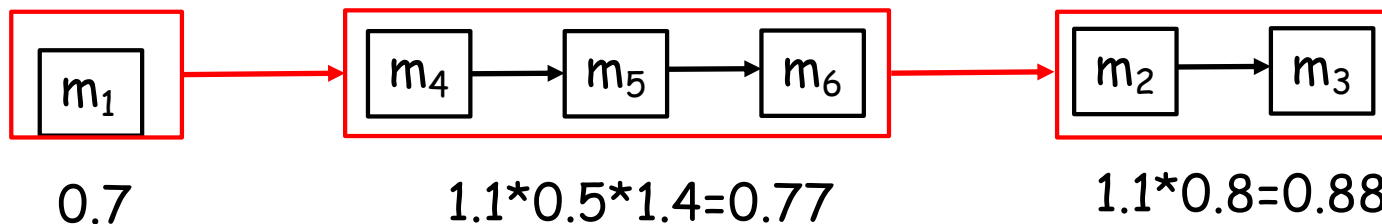
- NP-hard even for a single flow [2]
- One heuristic solution
  - Insight
    - Transform into a totally-ordered middlebox set
  - Steps ( $\lambda$ : traffic-changing ratio)
    - Treat middleboxes with dependencies as a single middlebox
    - Sort middleboxes in increasing order of  $\lambda$

## ○ Example

- Middlebox set

|           | $m_1$ | $m_2$ | $m_3$ | $m_4$ | $m_5$ | $m_6$ |
|-----------|-------|-------|-------|-------|-------|-------|
| $\lambda$ | 0.7   | 1.1   | 0.8   | 1.1   | 0.5   | 1.4   |

- Dependency relationship:  $m_2 \rightarrow m_3, m_4 \rightarrow m_5 \rightarrow m_6$



# Partially-ordered Middlebox Set Placement (cont'd)

- Another heuristic solution

- Insight

- Transform into a non-ordered middlebox set

- Steps

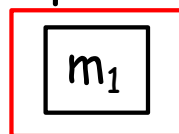
- Treat middleboxes with dependencies as a single middlebox by a topological order
- No dependency relations among new middleboxes

- Example

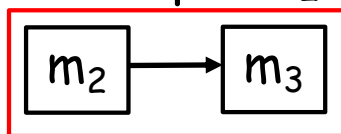
- Middlebox set

|           | $m_1$ | $m_2$ | $m_3$ | $m_4$ | $m_5$ | $m_6$ |
|-----------|-------|-------|-------|-------|-------|-------|
| $\lambda$ | 0.7   | 1.1   | 0.8   | 1.1   | 0.5   | 1.4   |

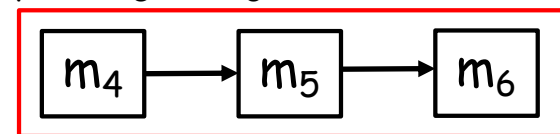
- Dependency relationship:  $m_2 \rightarrow m_3, m_4 \rightarrow m_5 \rightarrow m_6$



0.7



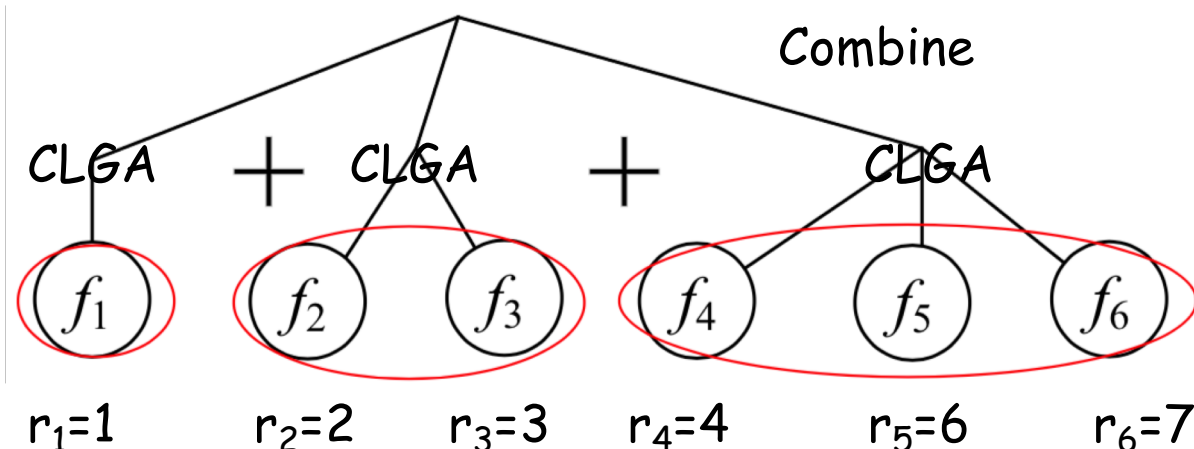
$1.1 * 0.8 = 0.88$



$1.1 * 0.5 * 1.4 = 0.77$

# 6. Handling Heterogeneous flows for Non-ordered Middlebox Set

- Group Flows by Initial Bandwidths (**GFIB**)
  - Group flows by initial traffic rates ( $r_f$ :  $f$ 's traffic rate)
    - #group:  $\lfloor \log_2 \frac{\max r_f}{\min r_f} \rfloor + 1$
    - The traffic rate range of the  $i^{\text{th}}$  group:  $2^{i-1} \times \min r_f \leq r_f < 2^i \times \min r_f$
  - Treat flows in each group as homogeneous
  - Apply CLGA for each group
- An example



$\max r_f = 7$   
 $\min r_f = 1$   
Group 1: [1,2)  
Group 2: [2,4)  
Group 3: [4,8)



## 6. Handling Heterogeneous Flows for Non-ordered Middlebox Set (cont'd)

- Time complexity

$$\max\{O(|V| \log|V|), O(|V|(\left\lceil \log_2 \frac{\max r_f}{\min r_f} \right\rceil + 1))\}$$

- Performance-guaranteed algorithm

- Approximation ratio <sup>[5]</sup>:  $\left\lceil \log_2 \frac{\max r_f}{\min r_f} \right\rceil + 1$

# 7. Simulation

- Our algorithms

- LGA

- Single middlebox
- Select the level with the minimum cost

- CLGA

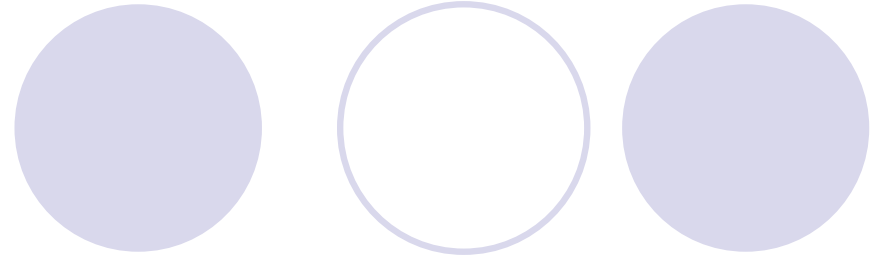
- Non-ordered middlebox set
- Apply LGA independently

- DP

- Totally-ordered middlebox set
- Dynamic programming

- GFIB

- Heterogeneous flows
- Group flows by initial traffic rates
- Combine placement by applying CLGA for each group



# 7. Simulation



- Comparison algorithms

- Random-fit

- Randomly place middleboxes until all flows are satisfied

- NOSP [2]

- Place middleboxes in increasing order of traffic-changing effects for each flow from source to destination independently
- For single middlebox or non-ordered middlebox set

- TOSP [2]

- Dynamic programming based algorithm for each flow independently
- For totally-ordered middlebox set with or without vertex capacity

[2] Traffic aware placement of interdependent NFV middleboxes (INFOCOM '17)

# Settings

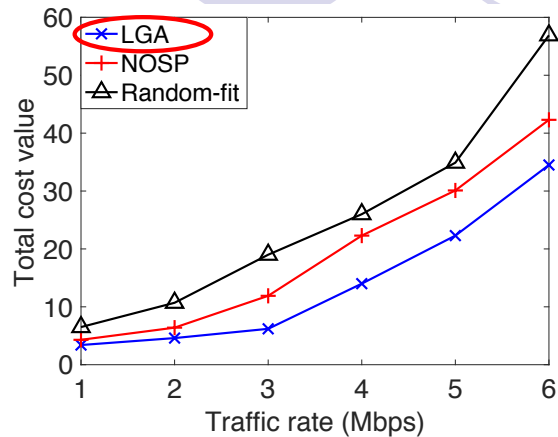


- Topology
  - Perfect 5-layer binary tree for each triangle
- Facebook data center traffic trace
  - Single-flow initial traffic rate: 1~6 Mb
- Middlebox set

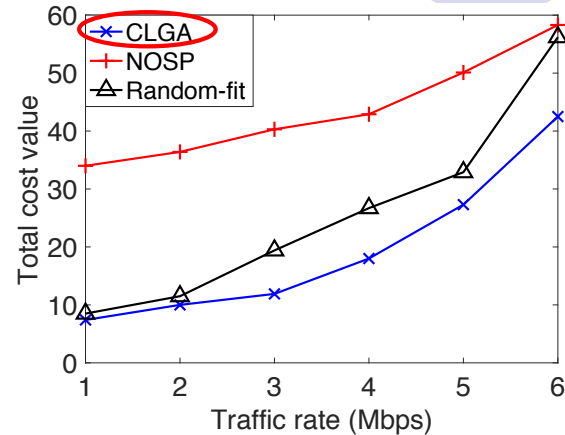
|                        | $m_1$ | $m_2$ | $m_3$ | $m_4$ |
|------------------------|-------|-------|-------|-------|
| Traffic-changing ratio | 0.7   | 0.8   | 1.1   | 1.2   |
| Setup cost             | 0.4   | 0.6   | 0.2   | 0.8   |

- Dependency relationship
  - $m_2 \rightarrow m_3 \rightarrow m_1 \rightarrow m_4$

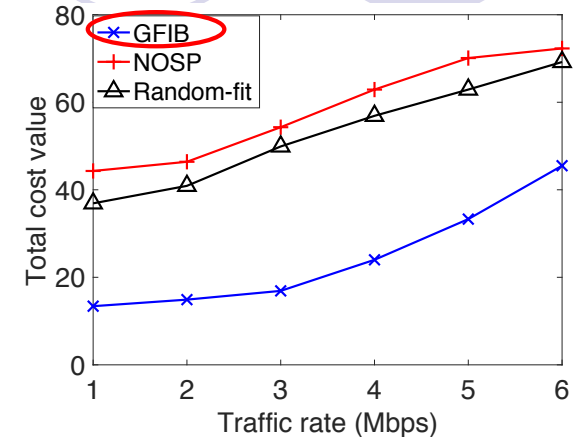
# Simulation Results



Single middlebox  
(LGA)



Non-ordered middlebox set  
(CLGA)

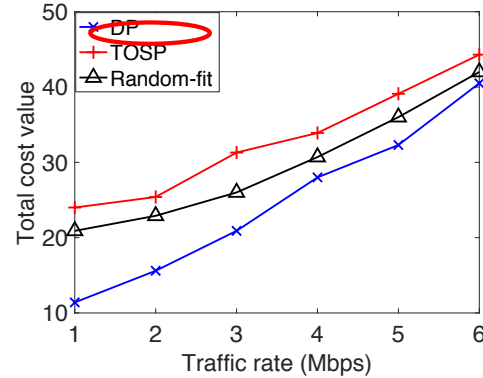
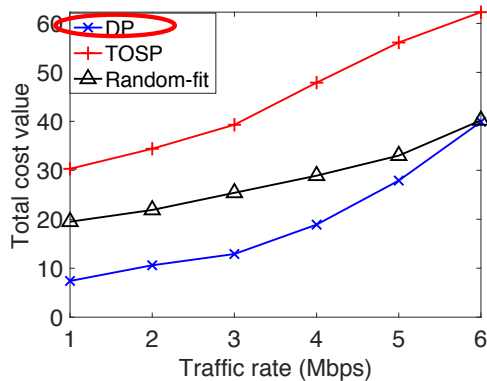


Bandwidth heterogeneity  
(GFIB)

- LGA costs 20.3% less than NOSP and 35.1% less than Random-fit.
- CLGA performs the best even with heavy traffic.
- The performance of Random-fit is not steady.
- For heterogeneous flows, GFIB saves about 36.9% and 34.0% compared to NOSP and Random-fit.

# Simulation Results (cont'd)

## Totally-ordered middlebox set



| Totally-ordered middleboxes                           | Total cost | Set-up cost |
|---|------------|-------------|
| $m_2 \rightarrow m_3 \rightarrow m_1 \rightarrow m_4$ | 20.9       | 10.4        |
| $m_3 \rightarrow m_1 \rightarrow m_2 \rightarrow m_4$ | 23.7       | 12.0        |
| $m_1 \rightarrow m_4 \rightarrow m_3 \rightarrow m_2$ | 22.8       | 9.6         |
| $m_1 \rightarrow m_2 \rightarrow m_3 \rightarrow m_4$ | 11.9       | 4.4         |
| $m_4 \rightarrow m_3 \rightarrow m_2 \rightarrow m_1$ | 24.7       | 10.2        |

Without vertex capacity

With vertex capacity

Middlebox order effect at 3 Mbps (DP)

- The total cost is larger than the non-ordered middlebox set.
- Limited vertex capacity increases the minimum cost.
- The order of a middlebox set matters not only for total cost but also for set-up cost.

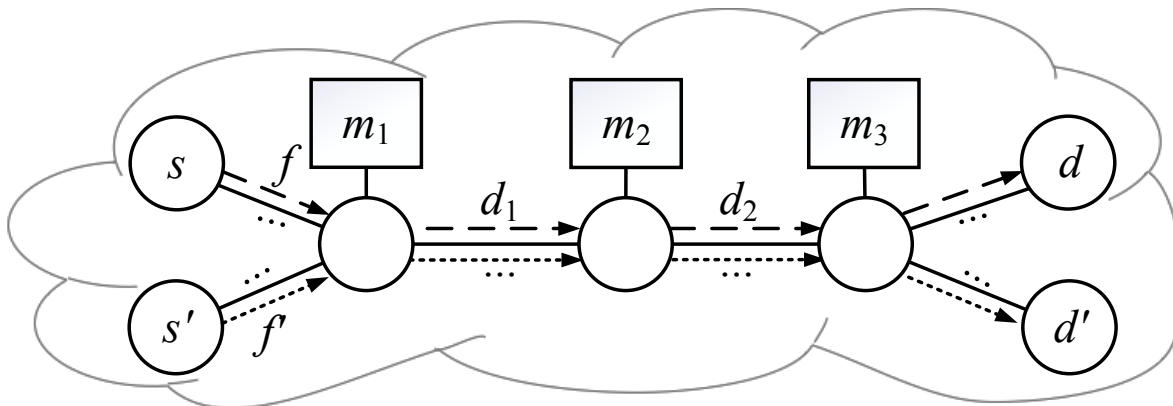
# 8. Conclusion and Future Work

- Middlebox constraints
  - Traffic-changing effects
  - Dependency relations
  - Flow sharing
- Middlebox placement
  - Balancing middlebox set-up cost and bandwidth consumption
- Tree-structured topologies
  - Optimal algorithms for homogeneous flows
  - Performance-guaranteed algorithm for heterogeneous flows
- Future work
  - General tree-structures

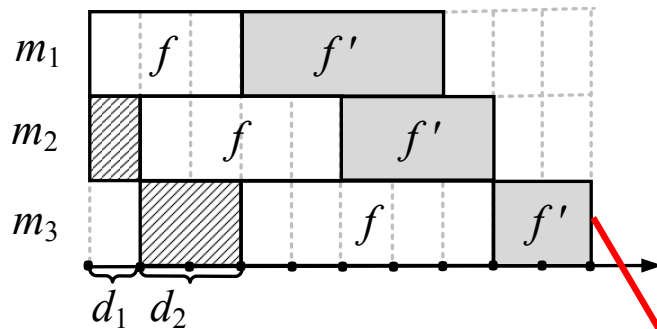
# Other Service Chain Models

$$d_1 = 1 \quad d_2 = 2$$

Processing time

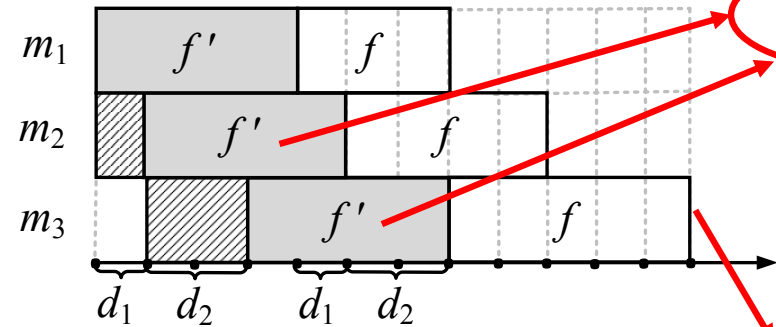


| Flows | Middleboxes |       |       |
|-------|-------------|-------|-------|
|       | $m_1$       | $m_2$ | $m_3$ |
| $f$   | 3           | 4     | 5     |
| $f'$  | 4           | 3     | 2     |



$f$  before  $f'$

$$t = 10$$



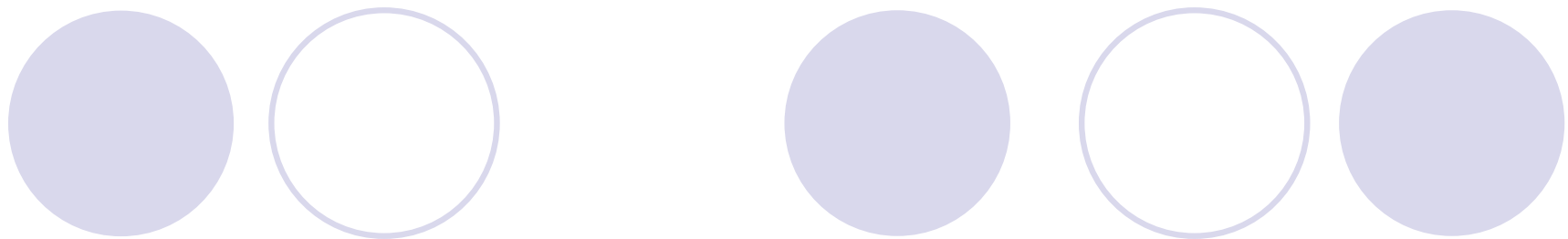
$f'$  before  $f$

$$t' = 12$$

prolong

- Minimizing the makespan
- Minimizing the average completion time





Q & A