



# Fast Interference-Aware Scheduling of Multiple Wireless Chargers

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# Outline

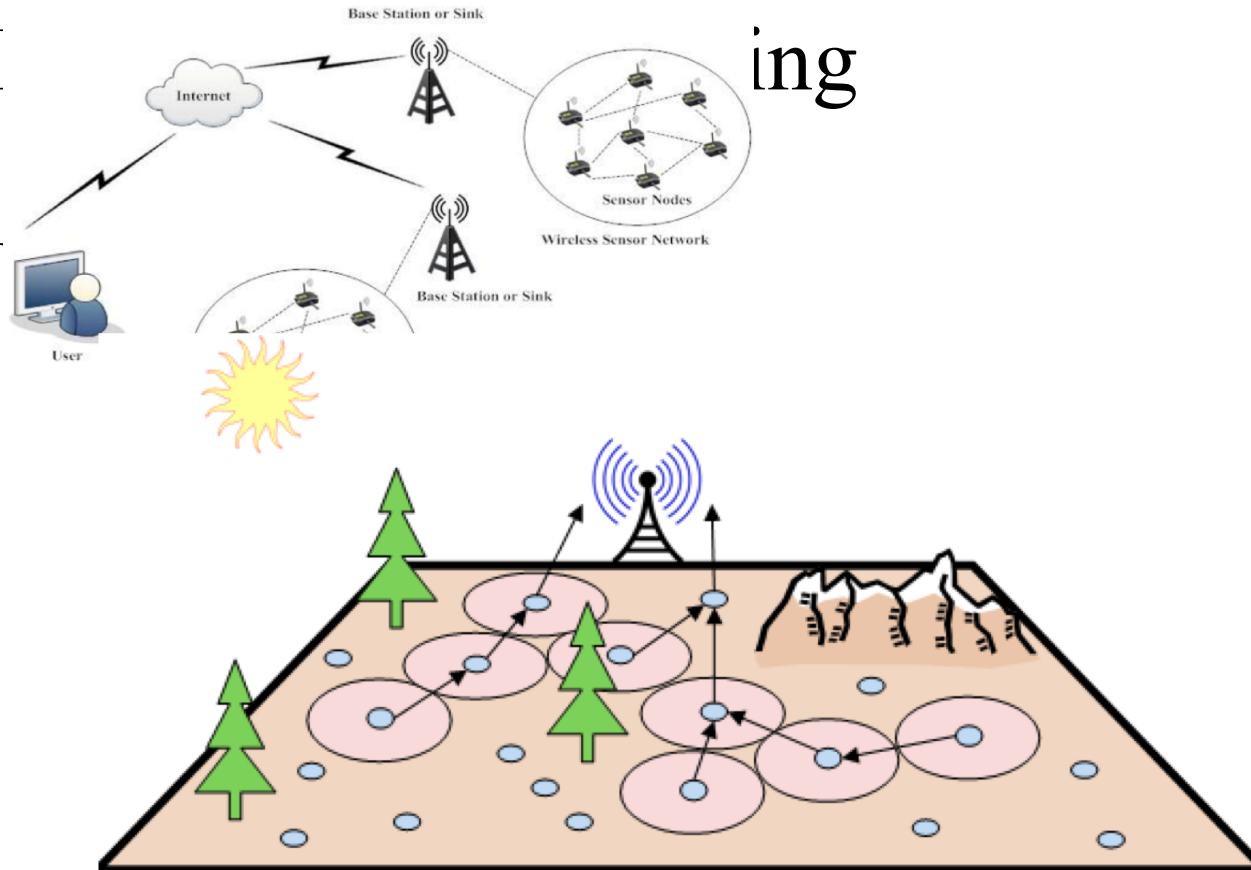
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- Background and contributions
- Model and problem formulation
- Algorithm design
- Performance evaluation
- Conclusion



# Background

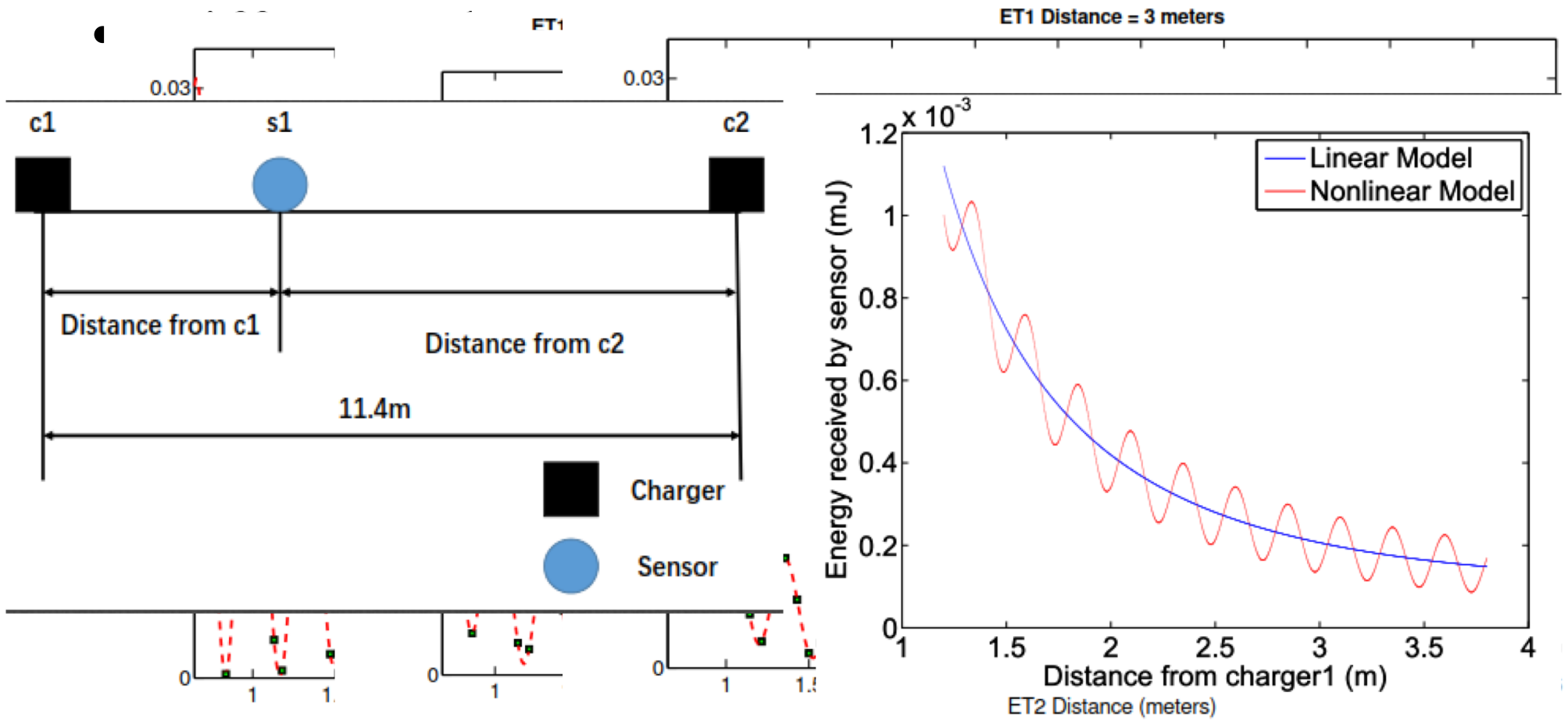
- **Wireless Sensor Network**
  - Sensors are powered by small batteries;





# Background

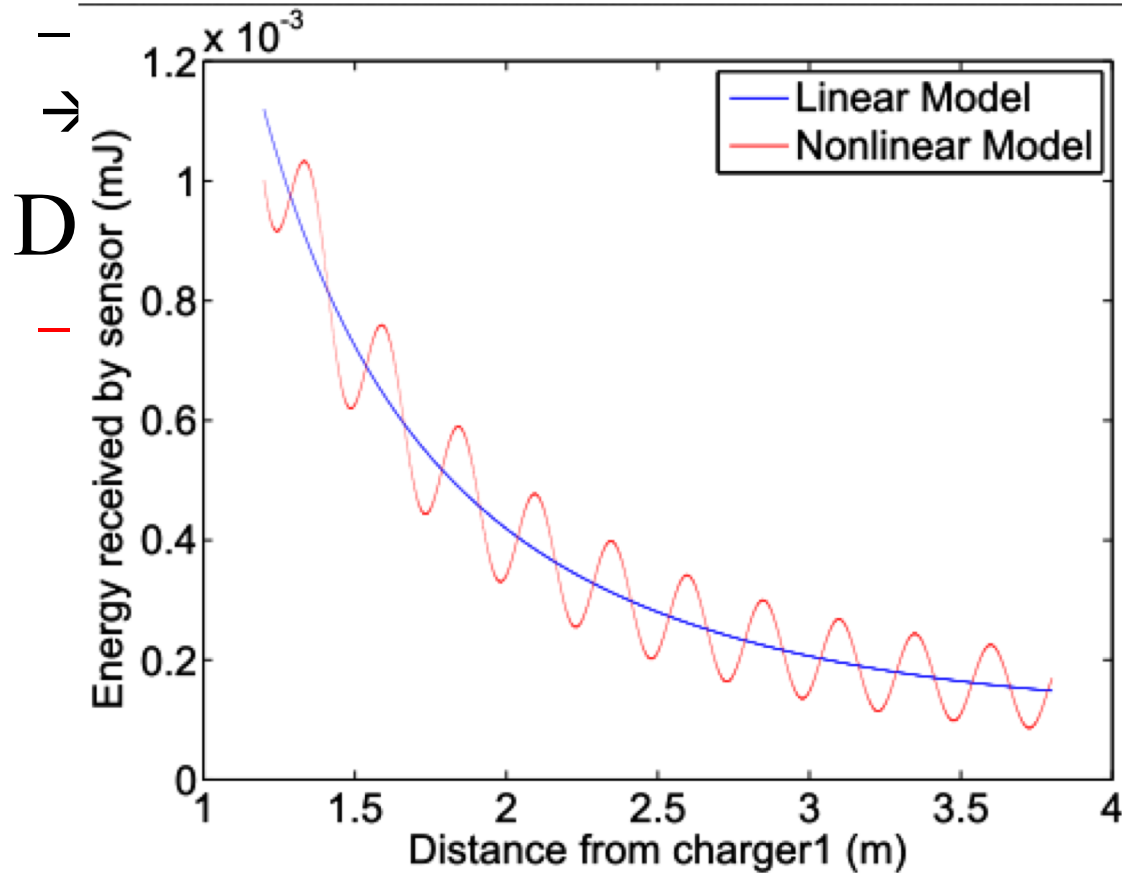
- Combined energy
  - Combined energy is additive?





# Background

- Related work:



er of chargers



# Contributions

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- We apply a new charging model with nonlinear super-position into the FCS problem  $\rightarrow$  **NP-complete**;
- We propose FastPick algorithm in 1D line  $\rightarrow$  bound  $(2-\epsilon)$ ;
- We propose RoundPick algorithm in 2D network  $\rightarrow$  bound;



# Models

- Network model

- N stationary sensor nodes  $\{s_1, s_2, \dots, s_n\}$  and M chargers  $\{c_1, c_2, \dots, c_m\}$

- Charging model

- frequency component  $\omega_0$ , amplitude  $A_0$ , initial phase  $\varphi_0$ , power attenuation factor 2
- Radio signal received by sensor from charger  $c_i$

$$a_{i0}(t) = \frac{A_0}{4\pi d_{ij}/\lambda} \cos(\omega_0 t + \varphi_0 - 2\pi \frac{d_{ij}}{\lambda})$$

- Radio signal received by sensor  $s_j$  from charger set  $C$

$$A_0^j(t) = \sum_{c_i \in C} a_{i0}(t) = \sum_{c_i \in C} \frac{A_0}{4\pi d_{ij}/\lambda} \cos(\omega_0 t + \varphi_0 - 2\pi \frac{d_{ij}}{\lambda})$$



# Models

- Charging model

- Power received by sensor  $s_j$  from charger set  $C$

$$\begin{aligned} P_{j|C} &= \int \overline{[A_0^j(t)]^2} d\omega \\ &= P \sum_{c_i \in C} \frac{1}{d_{ij}^2} + P \sum_{c_i \in C} \sum_{\substack{c_m \in C \\ c_m \neq c_i}} \frac{1}{d_{ij} d_{mj}} \cos(2\pi \frac{d_{ij} - d_{mj}}{\lambda}) \end{aligned}$$

- where  $P = \int p_i d\omega$ ,  $p_i = \frac{A_i^2}{2}$





# Models

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- Harvesting model
  - Threshold of power:  $\epsilon$
  - Energy capacity:  $E$

$$e_j|_{C,t} = \begin{cases} 0 & \text{if } P_j|_C < \epsilon \\ 0 & \text{if } P_j|_C > \epsilon \text{ and } e'_j > E \\ \alpha t(P_j|_C - \epsilon) & \text{otherwise} \end{cases}$$



# Problem Formulation

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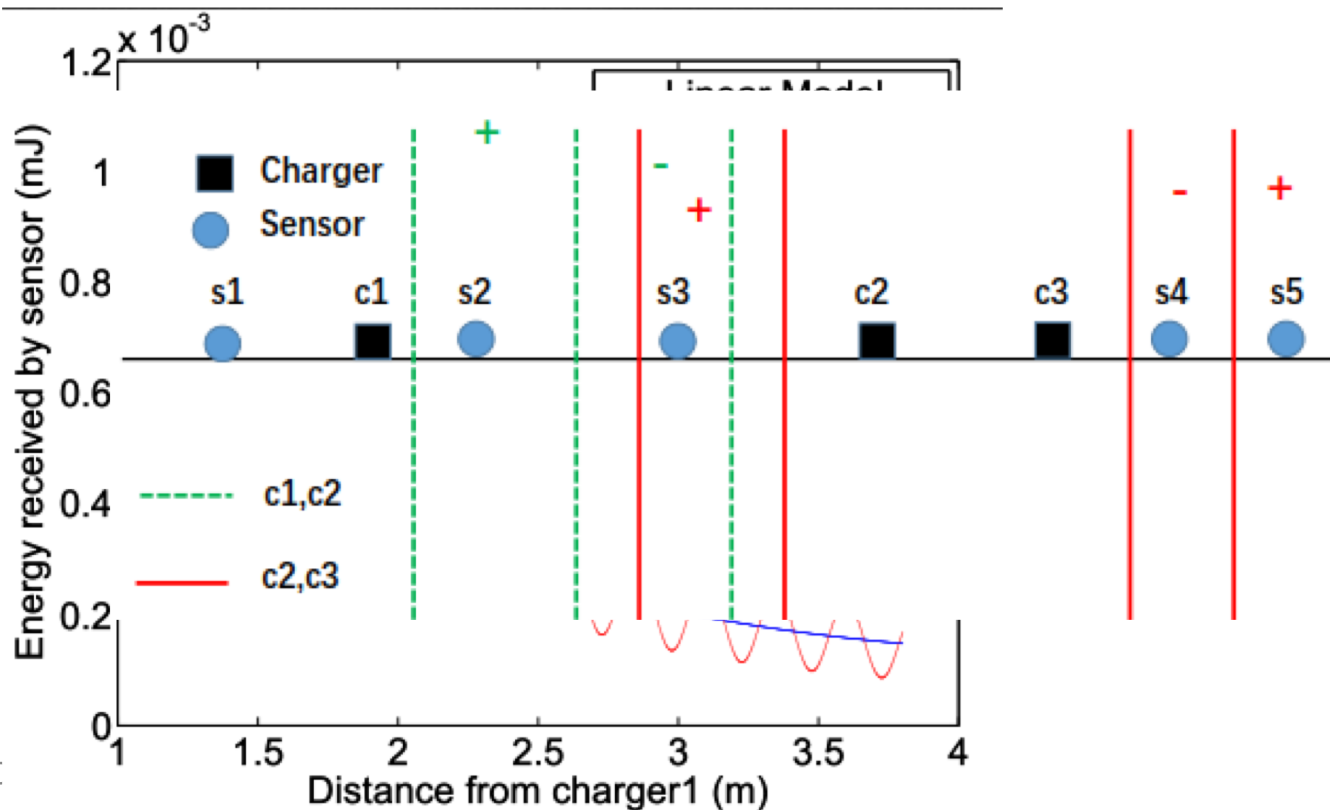
- We use  $H_i$  to denote  $i_{th}$  charging schedule
  - $H_2 = \{1,0,1,0\}$ ;
  - $\Delta$  denotes charging duration.
- Problem:
  - Given a set  $C$  of chargers with fixed position, a set  $S$  of rechargeable sensors, a set  $\{d_{ij} \mid 1 \leq i \leq N, 1 \leq j \leq M\}$  of distance between  $c_i$  and  $s_j$ , and an energy capacity  $E$  of each sensor, FCS is to find a set of multiple charging schedules  $\{H_1, H_2, \dots, H_k\}$ , to charge each sensor with energy no less than  $E$ , and  $k$  is minimized.



# One-Dimension Line

- Rational

- Assumption: all frequency are the same;
- Observation: difference of phases between two chargers





# One-Dimension Line

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- FastPick (Initial phases are adjustable)
  - Choose the sensor with the least energy;
  - Find two chargers that are closest to this sensor;
  - Adjust their initial phases to make most sensors lie in their strong areas;
  - Adjust other chargers' initial phases to make the strong and weak areas are the same;
  - Reverse the original weak and strong areas.



# One-Dimension Line

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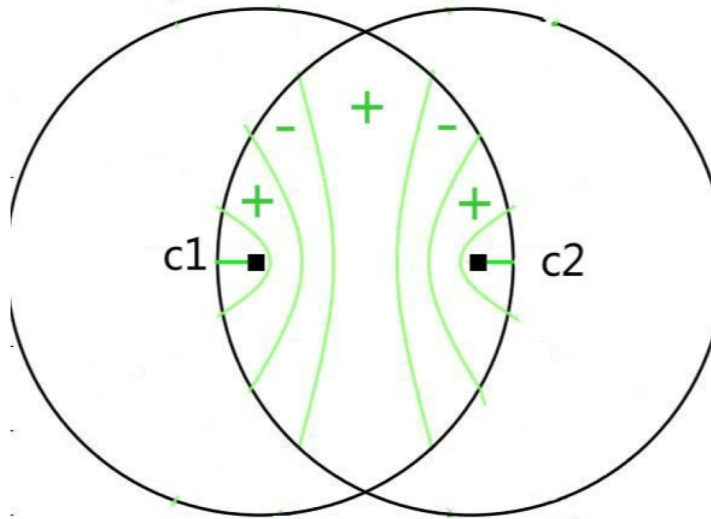
- Approximation Ratio
  - Lower bound:  $T$  (All chargers strengthen each other);
  - FastPick is at most 2 times longer than  $T$ ;
  - $T$  is smaller than  $OPT$ ;
  - FastPick is  $2-\epsilon$  approximate.



# Two-Dimension plane

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- Challenges
  - Irregular;
  - Two directions;
  - Cannot coincide.

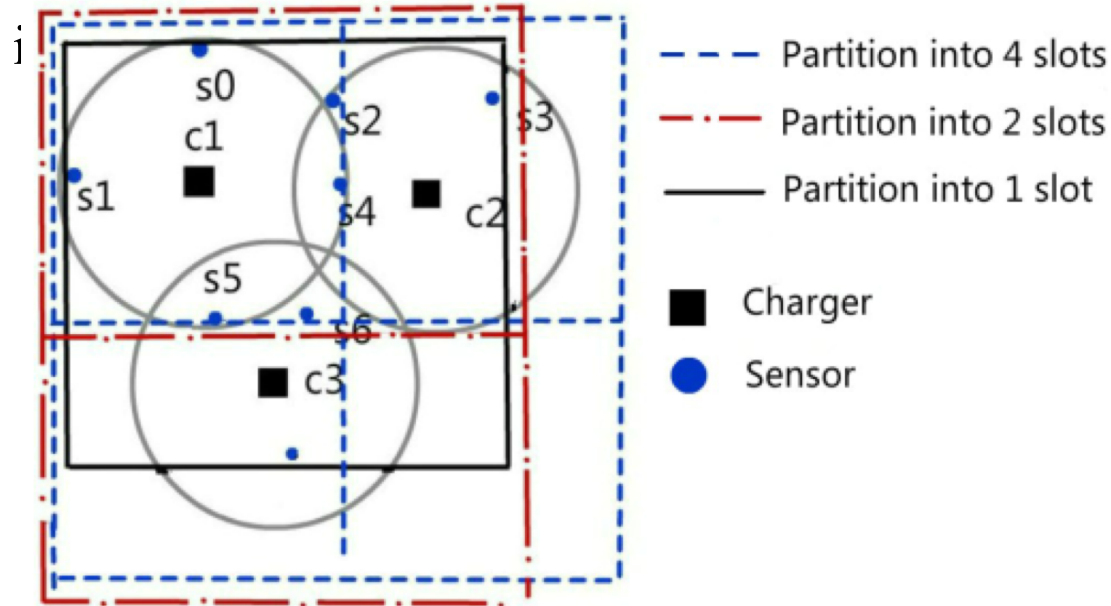




# Two-Dimension Plane

- Partition

- Every sensor in one slot should be covered by chargers in this slot;
- There is at least one charger in a slot;
- The length of slot side should be minimized but no less than  $2 * R$  (R





# Two-Dimension Plane

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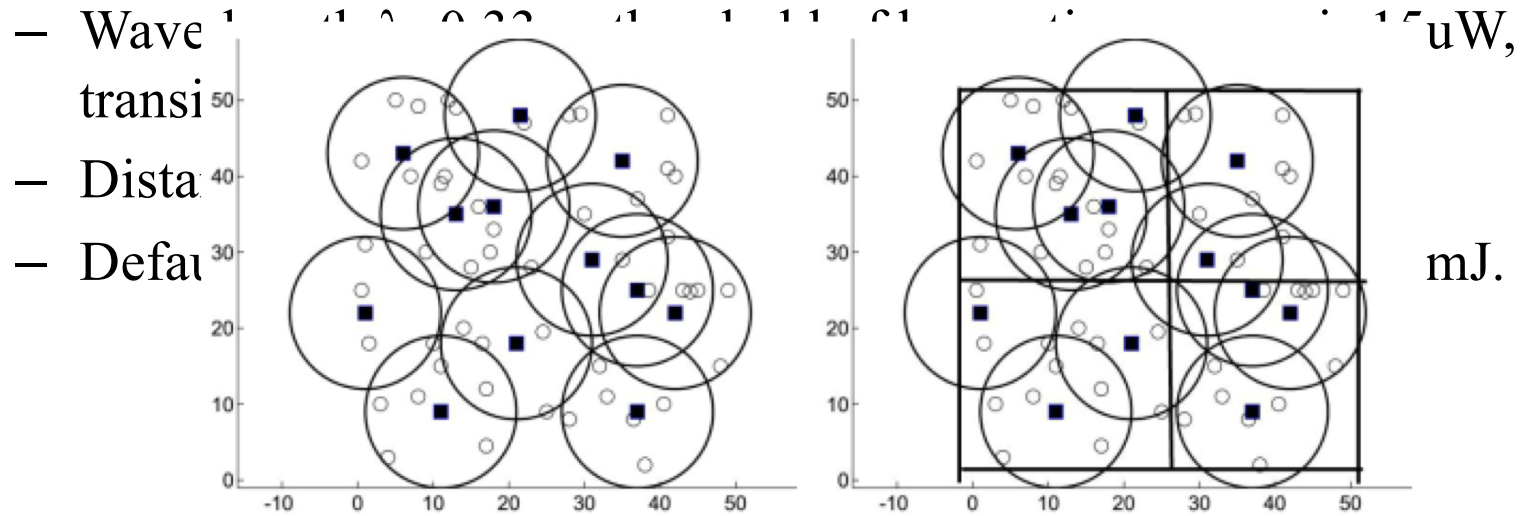
- RoundPick
  - Partition the network;
  - In each iteration, algorithm first computes each two chargers strong areas in each slot, then chooses a sensor with the least energy;
  - Add new chargers if more energy would be received;
  - Move slot.
  
- We also get a bound of  $6-4\varepsilon$





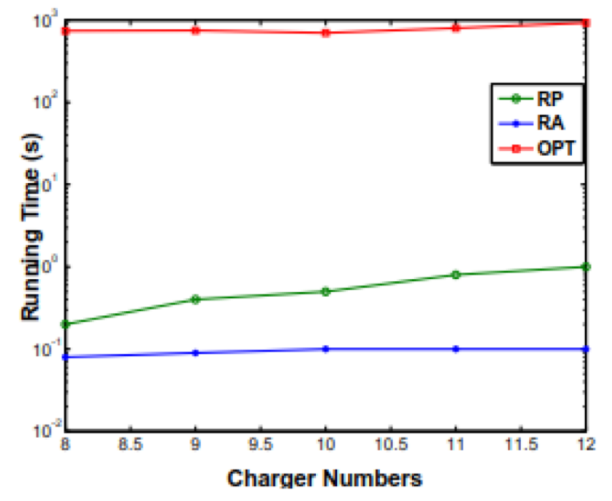
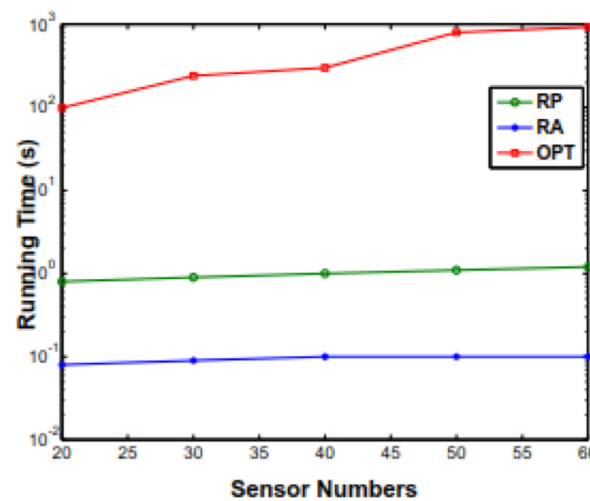
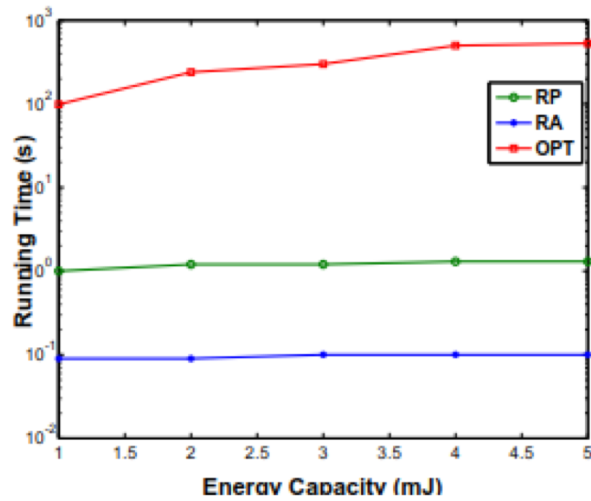
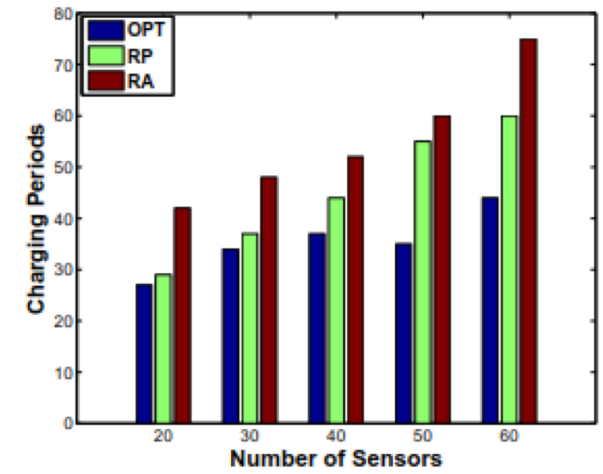
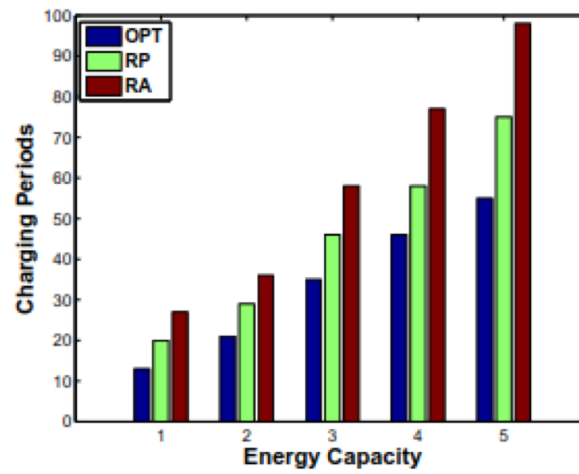
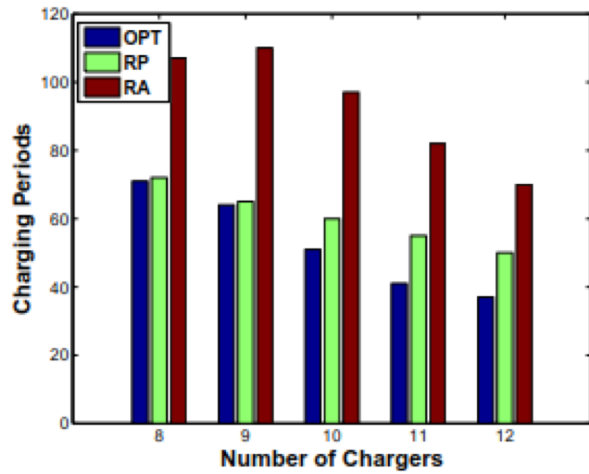
# Evaluations

- Settings





# Evaluations





Thank you  
Q&A