AoI-Aware, Digital Twin-Empowered IoT Query Services in Mobile Edge Computing

Jing Li, Song Guo, *Fellow, IEEE*, Weifa Liang, *Senior Member, IEEE*, Jie Wu, *Fellow, IEEE*,
Quan Chen, *Member, IEEE*, Zichuan Xu, *Member, IEEE*, Wenzheng Xu *Member, IEEE*, and
Jianping Wang, *Fellow, IEEE*

Abstract—The Mobile Edge Computing (MEC) paradigm gives impetus to the vigorous advancement of the Internet of Things (IoT), through provisioning low-latency computing services at network edges. The emerging digital twin technique has been explosively growing in the IoT community, which bridges the gap between physical objects and their digital representations in an MEC network, enabling real-time monitoring and analysis, simulations on the dynamics of systems, accurate predictions on behaviours of objects, and optimization on network resource allocation. In this paper, we consider AoI-aware query services in an MEC network empowered by digital twin technology for diverse IoT applications. We aim to maximize the weighted sum of the accumulative freshness of query results measured by the Age of Information (AoI) and the total query service delay of admitted requests. To this end, we first formulate a novel minimization problem that explores nontrivial trade-offs between the two conflicting optimization objectives: the freshness of query results and service delays, and we show the NP-hardness of the problem. Then, we propose an approximation algorithm with a provable approximation ratio for the problem, at the expense of bounded computing capacity violations. We also develop a heuristic for the problem without any capacity violations. We finally evaluate the performance of the proposed algorithms via simulations. The simulation results demonstrate that the proposed algorithms are promising, and outperform the comparison benchmarks.

Index Terms—Digital twin, mobile edge computing, query services, age of information, IoT applications, service delays, approximation algorithms, resource allocation and optimization

I. INTRODUCTION

The last decade witnessed the unprecedented explosion of Internet of Things (IoT) applications by culminating the proliferation of IoT devices connected with the Internet, thereby permeating the modern-day world and flourishing the potential for brilliant living [27]. However, most IoT devices have limited resources and energy for running IoT applications on themselves, instead, they usually offload computing-intensive tasks to remote clouds that may cause high service costs and prolonged service delays [8]. Such a computing paradigm is inappropriate for many delay-sensitive IoT applications due to stringent end-to-end delay requirements [32]. Moreover, in traditional IoT architectures, IoT devices store data in their backlogs for future diagnosis and improvement, which however may lead to stale feedback, unverified updates, and severe malfunctions [34].

Mobile Edge Computing (MEC) has been envisaged as a promising paradigm to provide computing resource (cloudlets) at the edge of the core network in the proximity of users to mitigate user service delays [4], [16]–[18]. The emerging digital twin technique creates digital avatars for IoT devices in MEC networks catering to massive data continuously generated from IoT devices, through leveraging integrated data and simulations to provide timely data analysis and modeling [23]. The marriage of MEC and digital twin techniques drives new opportunities and challenges for IoT service provisioning, accurate prediction, emulations, optimization, and decision-making, facilitating efficient network management and resource allocations [15], [24].

Motivated by the recent studies in digital twin-empowered service provisioning in MEC [21], [24], [28], [31], [33], [34], the accuracy and fidelity of a service model are determined by how often it is retrained by the update data from its source objects. However, objects are not always accessible by the service model, due to their mobility and intermittent contact with the network. To overcome the unavailability of objects, there is a digital twin for each object in the MEC network, which is a virtual mirror of the object to reflect the status of the object. Thus, the service model always can access its DT status and data instead of the object itself. To maintain the freshness of the DT data of an object, the object needs to upload its update data to its DT quite often. In this study, we consider how to maintain the freshness of query results while minimizing query response delays of IoT applications in an MEC network empowered by digital twins of sensors, where sensors are scattered at diverse geographical locations to provide continuous sensory readings of time-varying environmental parameters (e.g., humidity or temperature). On account of the system dynamics, IoT applications usually rely on real-time and predictive data [9], however, portable sensors have limited computing, storage and communication resources. As a promising cure, the network service provider can create a digital twin for each sensor in a cloudlet to process its generated data and simulate its behaviours in the network [28].

J. Li, W. Liang and J. Wang are with the Department of Computer Science, City University of Hong Kong, Hong Kong, P. R. China. Emails: {jing.li, weifa.liang, jianwang}@cityu.edu.hk

S. Guo is with the Department of Computer Science and Engineering, The Hong Kong University of Science and Technology, Hong Kong, P. R. China. Email: songguo@cse.ust.hk

J. Wu is with the Department of Computer and Information Sciences, Temple University, Philadelphia, USA. Email: jiewu@temple.edu

Q. Chen is with the School of Computer, Guangdong University of Technology, 510006, P. R. China. Email: quan.c@gdut.edu.cn

Z. Xu is with the School of Software, Dalian University of Technology, Dalian 116620, P. R. China. Email: z.xu@dlut.edu.cn

W. Xu is with the College of Computer Science, Sichuan University, Chengdu 610000, P. R. China. Email: wenzheng.xu@scu.edu.cn

For instance, digital twins facilitate an IoT application for forecasting weather and climate patterns, which is beneficial for smart farming.

The digital twin of each sensor contains not only its historical update locations, uploading times, the status of the object but also its update data at each time. We refer to these data as the DT data of the sensor, which can be used for service model training and retraining with the ultimate objective of providing intelligent services by Artificial Intelligence (AI) or Machine Learning (ML) algorithms. To maintain the state freshness of digital twins, it is desirable that each sensor can upload newly collected data to its digital twin on time. However, the volume of data uploaded by each sensor usually is constrained because of the limited energy and cost imposed on the sensor [2]. It thus poses a great challenge for each digital twin to instruct its sensor when performing data uploading, in order to provide the Age of Information (AoI)-aware IoT query services, subject to energy and cost capacities on the sensor, where a common metric to measure the data freshness is the AoI [1], [40], i.e., the duration of the data from its generation to its usage.

Quality of Services (QoS) of user queries on digital twin data usually is measured by two metrics: the freshness of query results and query service delays [2], [31], [34]. Meeting QoS requirements of different users for their IoT applications in MEC poses great challenges. First, the placement of IoT application instances to cloudlets impacts the freshness of query results and query service delays, e.g., a long distance between a cloudlet hosting an IoT application instance and its digital twins leads to a stale query result and a high service delay. How to deploy IoT application instances of users to the MEC network to optimize these two metrics is challenging. Second, it is very difficult to determine whether to utilize the current data at a digital twin for a query to have a lower query service delay, or to wait for the next update data of the digital twin to obtain a lower AoI on the query result. Finally, to provide fresh data for as many queries as possible, it is challenging to determine when scheduling sensors to upload their update data and synchronize with their digital twins over a finite time horizon, considering limited energy and cost budgets on sensors. In this paper, we will address the aforementioned challenges and explore nontrivial trade-offs between the freshness of query results and query service delays.

The novelty of this study lies in IoT service provisioning in a DT-empowered MEC network, by jointly considering the freshness of query results and query service delays, through DT update scheduling and IoT application instance placements. With the aim to minimize the weighted sum of AoIs of query results and service delays of admitted queries for a given time horizon, efficient approximation and heuristic algorithms for the problem are devised.

The main contributions of this paper are as follows.

- We formulate a novel minimization problem that jointly considers the accumulative freshness of query results and the total query service delay of admitted IoT service requests in an MEC network empowered by digital twins, and show the NP-hardness of the problem.

- We devise an approximation algorithm with a provable approximation ratio for the problem at the expense of bounded computing capacity violations. Meanwhile, we also develop an efficient heuristic algorithm for the problem without any capacity violations.
- We evaluate the algorithm performance via simulations. The simulation results demonstrate that the proposed approximation algorithm is promising.

The rest of the paper is arranged as follows. Section II surveyed related works of digital twins in MEC. Section III includes the system model and the problem definition. Section IV proposes an approximation algorithm for the problem with bounded capacity violations. Section V proposes a heuristic algorithm for the problem without any capacity violation. Section VI evaluates the performance of the proposed algorithms, and Section VII concludes the paper and points out a potential research topic from the research in this paper.

II. RELATED WORK

Lots of efforts have been taken in recent years to facilitate delay-sensitive IoT service provisioning in MEC platforms [6], [8], [17], [27], [32], [36], [38]. Gedawy et al. [6] designed heuristic algorithms to optimize the network throughput, as well as the energy consumed by IoT applications. Goudarzi et al. [8] developed an IoT application placement technique in MEC by the Memetic Algorithm (MA) to mitigate the execution time and energy consumption. Li et al. [17] offered approximate and online solutions to handle admitting multi-source IoT applications in MEC environments. Ma et al. [27] considered truthfulness and budget-balance of IoT services, by designing a truthful combinatorial double auction mechanism. Tuli et al. [32] explored the complicated workload dynamics of IoT devices and heterogeneous resources in edge-cloud networks. They outlined a policy gradient-based learning method and captured the temporal patterns to build a framework for resource management in stochastic environments. Wu et al. [36] developed a distributed SDN controller for coordinating mobile IoT devices, enabling efficient location authentication and assignment between IoT devices and access points. These studies however did not consider data freshness of IoT service provisioning.

There are extensive studies on supplying fresh data of the provided IoT services within MEC environments, through minimizing the AoI [1]–[3], [11], [22], [35], [37], [43], [44]. Corneo et al. [2] investigated the problem of prompt dissemination of sensor updates to optimize the AoI of IoT services. Li et al. [11] proposed a heterogeneous federated multi-agent reinforcement learning algorithm to minimize the AoI in an Unmanned Aerial Vehicle (UAV)-assisted MEC system. Liu et al. [22] studied the batch generation and multi-path communication in MEC, and proposed approximation algorithms to minimize the peak and average AoI, while meeting the throughput requirements. Wang et al. [35] devised an offline scheduling algorithm and an online learning-based algorithm for minimizing the average age of critical information. Xu et al. [37] modelled the quality of big data analytic services based on the Age of Data (AoD) for IoT applications, and

developed an online learning method to minimize the AoD in MEC, through leveraging the multi-armed bandit approach. Zhang *et al.* [43] explored a nontrivial trade-off between the AoI and the service delay, and proposed an efficient algorithm to mitigate the average service delay whilst meeting AoI requirements of user requests. Zhou *et al.* [44] addressed the dynamic demands of users with spectral efficiency features, through designing a congestion-based paradigm and an AoI-based paradigm to achieve network stability and maximize the throughput. However, none of these mentioned works incorporated the digital twin technique into their problem formulations.

MEC platforms empowered by the emerging digital twin technique enable the platforms to provide efficient services for various IoT applications [12], [14], [15], [20], [23], [24], [28], [31], [33], [34]. Li *et al.* [14], [15] estimated the reliability of virtual network functions by digital twins, and devised efficient algorithms to provide IoT services enabled by service function chains. Li *et al.* [12], [20] also incorporated the mobility of objects in edge-cloud environments, and proposed approximate and online solutions to provide AoI-aware query services to users built upon the digital twin data. Lin *et al.* [23] proposed a congestion control scheme to meet the dynamic demands of digital twin services by Lyapunov optimization. Lu *et al.* [24] designed a federated learning algorithm built on the blockchain technique to improve security and data privacy in digital twin-assisted MEC networks. Sun *et al.* [31] utilized digital twins to minimize the offloading latency by the Lyapunov optimization, considering user mobility and service migration. Vaezi *et al.* [33] devised approximation algorithms to assign digital twins to execution servers at network edge to minimize the longest request-response delay, considering the data age constraints. Wang *et al.* [34] formulated two problems for managing digital twins to optimize the data fidelity and the reveal delay, respectively, where the data fidelity is the expected time from the production of the data to its delivery, and the reveal delay is defined as the time duration after the production of the latest collected log. They adopted the blockchain technique to design a sustainable digital twin management framework. These mentioned studies however did not investigate the joint optimization of AoIs of query results and query service delays for digital twin-empowered IoT services. Liang *et al.* [21] investigated the relationship between the freshness of a service model and the AoIs of the DT data for the model training. They devised an efficient algorithm for minimizing the cost of various resources consumed to achieve the model freshness. Zhang *et al.* [42] leveraged DT models to optimize device scheduling and MEC resource allocation, aiming to maximize utility across FL services. They developed heuristic and constant approximation algorithms for offline multi-FL services, and a DRL algorithm with dynamic bandwidth and moving client conditions settings.

In contrast to the aforementioned studies, in this paper we study IoT service provisioning in an MEC network empowered by the digital twin technique. We deal with AoI-aware query services with the aim to minimize the weighted sum of the accumulative AoI of query results and the total query delay of admitted queries, by striving for fine trade-offs between these
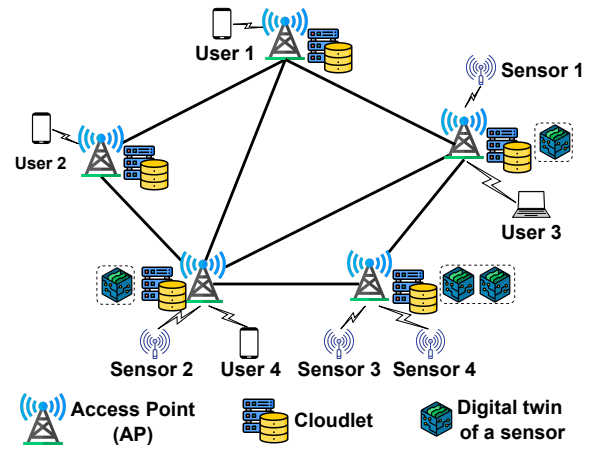

Fig. 1. An MEC network consists of 5 Access Points (APs) and their co-located cloudlets. There are 4 sensors with each having a deployed digital twin, and 4 users requesting query services.

two conflicting optimization objectives. It must be mentioned that part of this paper also appeared in a conference paper [13].

III. PRELIMINARIES

In this section, we introduce the system model and define the problem.

A. System model

An MEC network can be modelled by an undirected graph $G = (V, E)$, where V is the set of Access Points (APs), and E is the set of links connecting APs. Each AP is co-located with a cloudlet that is connected through an optical cable, and the transmission delay between them is negligible [26]. Denote by $v \in V$ a cloudlet or its co-located AP for simplicity, and let C_v be the computing capacity of cloudlet v. Each link $e \in E$ is associated with a transmission delay d_e to transmit one unit data along the link [39].

Let $\mathbb{S}$ be a set of sensors deployed across diverse geographical locations under the coverage of APs. We assume that each sensor $s \in \mathbb{S}$ has a digital twin $DT(s)$ deployed in a cloudlet. Each digital twin $DT(s)$ needs to synchronize with its sensor s often to maintain its state consistency as follows. Sensor s sends its collected data to its nearest AP v_s, assuming that its $DT(s)$ has been placed in cloudlet v_s. Figure. 1 illustrates an example of an MEC network with digital twins deployed in its cloudlets.

B. User queries on digital twin data of sensors

We assume that MEC network G runs in a discrete-time manner, and the monitoring time horizon $\mathbb{T}$ is composed of $|\mathbb{T}|$ equal *time slots*. Denote by U the set of users with different IoT applications requesting data from digital twins of sensors. Assume that each user $u \in U$ deploys an instance for his IoT application in a cloudlet that requires the amount c_u of computing resource in the beginning of time horizon $\mathbb{T}$, and user u issues queries (as his IoT application) for processing data from digital twins of different sensors in the beginning of different time slots.

Denote by $\mathcal{T}_u \subseteq \mathbb{T}$ the set of time slots in which user u will issue his queries of data retrieving and processing, i.e., the deployed IoT application of user u requests the data from the digital twin of a sensor s_u at each time slot $t \in \mathcal{T}_u \subseteq \mathbb{T}$. For example, given $\mathbb{T} = \{1, 2, 3\}$, the IoT application of user u requests data from digital twins of sensors s_1 and s_2 in the beginning of time slots 1 and 3, respectively, with $\mathcal{T}_u = \{1, 3\}$.

C. Updating digital twins of sensors

Given a limited energy budget on each sensor $s \in \mathbb{S}$, we assume that sensor s can deliver at most K_s updates to its digital twin $DT(s)$ within time horizon $\mathbb{T}$. The number of updates of any sensor is no larger than the number of time slots for the given monitoring time horizon, i.e., $K_s \leq |\mathbb{T}|$, $\forall s \in \mathbb{S}$. For example, given $\mathbb{T} = \{1, 2, 3\}$ and $K_s = 2$, sensor s can send its updates at the beginning of time slots 1 and 3, respectively.

The data uploading rate μ_s from sensor s to its allocated AP v_s can be calculated by the Shannon-Hartley theorem [7], where $\mu_s = B_s \cdot \log_2(1 + P_s/(dist_s^\alpha \cdot \eta^2))$, B_s is the bandwidth capacity of AP v_s, P_s is the transmission power of sensor s, $dist_s$ is the distance between sensor s and AP v_s, η^2 is the noise power, and α is the path loss factor, i.e., $\alpha = 2$ or 4 with regard to a short or large distance [4]).

Denote by ρ_s the volume of data per update of sensor s. Let ρ_s/μ_s be the data uploading delay from s to cloudlet v_s in which its digital twin $DT(s)$ is located. Denote by f_s the processing rate of $DT(s)$ in cloudlet v_s. The processing delay of $DT(s)$ thus is ρ_s/f_s.

The update delay t_s^{update} of digital twin $DT(s)$ consists of the data uploading delay from sensor s to cloudlet v_s and the processing delay of $DT(s)$ in cloudlet v_s, i.e.,

$$t_s^{update} = \rho_s/\mu_s + \rho_s/f_s. \tag{1}$$

Suppose the current time slot is t, and the current data of digital twin $DT(s)$ (or the received result of a user) is the last updated one at time slot t_0 with $t_0 \leq t$, *the Age of Information* (AoI) of this generated data is defined as $(t - t_0)$ [40]. It can be seen that t_s^{update} is the minimum AoI of data at $DT(s)$.

We assume that each $DT(s)$ of sensor $s \in \mathbb{S}$ has generated the initial data with the AoI of t_s^{update} in the beginning of time horizon $\mathbb{T}$. In the sequel, the AoI of the data at $DT(s)$ will linearly increase until the next update from sensor s. Assuming that sensor s sends its first update to $DT(s)$ at time slot t, then $DT(s)$ will generate the data that will be available for IoT applications at time $(t + t_s^{update})$, and the AoI of the data at $DT(s)$ decreases to t_s^{update} at time $(t + t_s^{update})$. The AoI of the data of $DT(s)$ then linearly increases again until receiving the next update from s. This procedure continues until the time horizon $\mathbb{T}$ finishes.

D. QoS Model

We introduce a novel metric to measure the Quality of Service (QoS) of query services built upon digital twin data of sensors, which is the weighted sum of AoIs of query results, and query service delays (i.e., the duration between the query issuing time and query result receiving time). Recall that the

IoT application of user $u \in U$ requests data from $DT(s_{u,t})$ of sensor $s_{u,t}$ at each time slot $t \in \mathcal{T}_u \subseteq \mathbb{T}$. In the following, we omit subscripts of $s_{u,t}$ for notation simplicity, i.e., replace $s_{u,t}$ with s. Cloudlet v_s hosts $DT(s)$ of sensor s. We assume cloudlet v_u hosts the IoT application instance of user u. Denote by $d_{s,u}$ the transmission delay of transmitting a unit of data through the shortest path from cloudlet v_s to cloudlet v_u [39]. Let λ_s be the volume of data at $DT(s)$ to be transferred, its transmission delay from $DT(s)$ to the IoT application instance of u is $\lambda_s \cdot d_{s,u}$. With the processing rate f_u of the IoT application instance of user u, the processing delay of the IoT application of user u in v_u is λ_s/f_u.

At each time slot $t \in \mathcal{T}_u$, a user u needs to determine whether to retrieve the current data at $DT(s)$ or wait for its next update. If the user prefers a lower query service delay to a fresher AoI of the data, the user can retrieve the data of $DT(s)$ immediately; otherwise the user can wait for the next update of $DT(s)$ to obtain fresher AoI, at the expense of more query service delays. Note that the volume of a query result usually is small compared with query data, and the transmission delay of the query result between the cloudlet processing the IoT application and the user thus can be negligible [31].

Assume that the IoT application of user u has been deployed in cloudlet v_u and user u issues a query for the data of digital twin $DT(s)$ of sensor s at time slot t. We analyze the freshness of the query result and query service delay of this query by distinguishing the following two cases.

Case 1. User u retrieves the current data at $DT(s)$. Let t_0 be the updating time of sensor s to generate the current data of $DT(s)$. The AoI of query result of user u is $\lambda_s \cdot d_{s,u} + \lambda_s/f_u + t - t_0$, where $\lambda_s \cdot d_{s,u}$ is the transmission delay of transmitting the data from $DT(s)$ in cloudlet v_s to cloudlet v_u hosting the IoT application of user u, λ_s/f_u is the processing delay of the IoT application in cloudlet v_u, and $(t - t_0)$ is the AoI of the generated data at $DT(s)$. The query service delay of user u is $\lambda_s \cdot d_{s,u} + \lambda_s/f_u$.

Case 2. User u will retrieve the newly generated data of $DT(s)$ through waiting for its next update. Because the least AoI of the generated data at $DT(s)$ is t_s^{update} by Eq. (1), the AoI of the query result is $\lambda_s \cdot d_{s,u} + \lambda_s/f_u + t_s^{update}$. Let t and t' be the current time slot and the next update time slot of $DT(s)$. It can be seen that the data generated by the next update of $DT(s)$ will be available for IoT applications at time $(t' + t_s^{update})$. Therefore, the IoT application of u needs to wait for $(t' + t_s^{update} - t)$ time for the next update of $DT(s)$. The query service delay of user u thus is $\lambda_s \cdot d_{s,u} + \lambda_s/f_u + t' + t_s^{update} - t$.

In summary, if user $u \in U$ issues a query at time slot $t \in \mathcal{T}_u \subseteq \mathbb{T}$, then the AoI $W_{AoI}(u, t)$ of the query result is

$$W_{AoI}(u,t) = \begin{cases} \lambda_s \cdot d_{s,u} + \lambda_s/f_u + t - t_0, & \text{Case 1} \\ \lambda_s \cdot d_{s,u} + \lambda_s/f_u + t_s^{update}, & \text{Case 2} \end{cases} \tag{2}$$

and the query service delay $W_{delay}(u, t)$ is

$$W_{delay}(u,t) = \begin{cases} \lambda_s \cdot d_{s,u} + \lambda_s/f_u, & \text{Case 1} \\ \lambda_s \cdot d_{s,u} + \lambda_s/f_u + t' + t_s^{update} - t, & \text{Case 2} \end{cases} \tag{3}$$

Let β be a constant with $0 \leq \beta \leq 1$. We define the

weighted sum $W(u,t)$ of the AoI of the query result and query service delay of a query issued by user u at time t as follows.

$$W(u,t) = \beta \cdot W_{AoI}(u,t) + (1-\beta) \cdot W_{delay}(u,t). \quad (4)$$

E. Problem definition

Definition 1: Given an MEC network $G = (V,E)$, a set $\mathbb{S}$ of sensors with limited energy capacity on each of them, a positive integer K_s for each sensor $s \in \mathbb{S}$, a set U of users issuing queries for IoT applications on sensors, and a finite time horizon $\mathbb{T}$. Assuming digital twins of sensors have already been deployed in cloudlets of V of G. Also, assume that the query profile of each user $u \in U$ for time horizon $\mathbb{T}$ is given (i.e., it is given that user u will retrieve which sensors at which time slots) too, and user u may retrieve data from digital twins of sensors in the beginning of time slots in $\mathcal{T}_u \subseteq \mathbb{T}$. *The minimization problem* of jointly considering the accumulative freshness of query results and the total service delay of admitted queries, by placing IoT application instances of users to cloudlet, such that the average weighted sum of the accumulative AoI of query results and the total query delay of admitted queries for time horizon $\mathbb{T}$ is minimized, i.e.,

$$\text{Minimize} \quad \sum_{u \in U} \sum_{t \in \mathcal{T}_u} W(u,t) / \sum_{u \in U} |\mathcal{T}_u|, \quad (5)$$

subject to computing capacities on cloudlets.

All symbols adopted are listed in Table I.

F. NP-hardness of the defined problem

Theorem 1: The minimization problem is NP-hard.

Proof The NP-hardness of the minimization problem is shown through a reduction from the minimum-cost Generalized Assignment Problem (GAP).

Consider a special case of the problem with a given update scheduling of each sensor over the time horizon, and users can only retrieve the current data at digital twins. Then, we only need to determine the IoT application instance placements of users. Let $W'(u,t,v)$ be the value of $W(u,t)$ by Eq. (4) for the query of user $u \in U$ issuing at time t if his IoT application instance is deployed in cloudlet $v \in V$. We reduce the problem to the minimum-cost GAP as follows.

In a minimum-cost GAP instance, there are $|V|$ bins, and each bin $v \in V$ possesses a capacity C_v, i.e., computing capacity of cloudlet v. There are $|U|$ items and each item $u \in U$ has a size c_u, i.e., the computing resource demand of IoT application instance of user u. Assigning item u to bin v will introduce a cost $\sum_{t \in \mathcal{T}_u} W'(u,t,v)$. The minimum-cost GAP is to minimize the total cost via assigning items to bins.

This minimum-cost GAP is equivalent to a special case of the minimization problem. The minimization problem is NP-hard as the minimum-cost GAP is NP-hard [29]. ∎

IV. APPROXIMATION ALGORITHM WITH BOUNDED CAPACITY VIOLATIONS

In this section, we deal with the minimization problem. Specifically, we decompose the problem into two sub-problems: the update scheduling problem, and the IoT application placement problem. We propose an optimal solution to

the former and an approximate solution for the latter, thereby proposing an approximation algorithm for the minimization problem.

We observe that optimization objective (5) is equivalent to minimizing the total weighted sum of AoIs of query results and the total query service delay of all queries over a given time horizon, i.e.,

$$\text{Minimize} \quad \sum_{u \in U} \sum_{t \in \mathcal{T}_u} W(u,t). \quad (6)$$

Considering a query issued by user u at time slot t for the data at $DT(s)$. Let t_0 be the updating time of sensor s to generate the data at $DT(s)$ at time slot t with $t_0 \leq t$. We distinguish it into two cases: Case 1. There is no further update of sensor s before the time horizon ends. Case 2. The next update of sensor s is sent at time t' with $t_0 < t'$ and $t < t' + t_s^{update}$.

To minimize the optimization objective (6), two functions $W_1(u,t)$ and $W_2(u,t)$ are defined as follows.

$$W_1(u,t) = \begin{cases} \beta \cdot (t-t_0), & \text{if Case 1} \\ \min\{\beta \cdot (t-t_0), \ t_s^{update} + (1-\beta) \cdot (t'-t)\}, & (7) \\ & \text{if Case 2} \end{cases}$$

and

$$W_2(u,t) = \lambda_s \cdot d_{s,u} + \lambda_s / f_u. \quad (8)$$

Especially, if there is no further update, $W_1(u,t)$ is $\beta \cdot (t - t_0)$, with $(t - t_0)$ the AoI of the data at $DT(s)$ when issuing the query. Otherwise, $W_1(u,t)$ is the smaller one between $\beta \cdot (t - t_0)$ and $t_s^{update} + (1-\beta) \cdot (t'-t)$, and $(t'-t)$ is the duration between the query issuing time and the sending time of the next update. $W_2(u,t)$ is the query service delay of user u that consists of the transmission delay of data transfer from $DT(s)$ in cloudlet v_s to cloudlet v_u hosting the IoT application and the processing delay of the IoT application in cloudlet v_u.

We claim that (i) the value of $W_1(u,t)$ is determined by the update scheduling of sensor s, that is whether to retrieve current data at $DT(s)$ or wait for its next update; and (ii) the value of $W_2(u,t)$ is determined by the IoT application placement of user u, as shown in Lemma 2 later.

We now define two sub-problems: the update scheduling problem and the IoT application placement problem, which correspond to the two defined functions $W_1(u,t)$ in Eq. (7) and $W_2(u,t)$ in Eq. (8), respectively.

Definition 2: Given an MEC network $G = (V,E)$, a set $\mathbb{S}$ of sensors, a positive integer K_s for each sensor $s \in \mathbb{S}$, a set U of users with queries for IoT applications on sensors, and time horizon $\mathbb{T}$, assuming digital twins of sensors have already been deployed in cloudlets of V, each user $u \in U$ may retrieve data from digital twins of sensors at the beginning of time slots in $\mathcal{T}_u \subseteq \mathbb{T}$, and we further assume that the query profile of each user u is given (i.e., at which time slot, it will retrieve the data of digital twins of which sensors). *The update scheduling problem* in G is to

$$\text{Minimize} \quad \sum_{u \in U} \sum_{t \in \mathcal{T}_u} W_1(u,t), \quad (9)$$

where $W_1(u,t)$ is defined in Eq. (7), by scheduling the K_s updates for each sensor $s \in \mathbb{S}$ over the time horizon $\mathbb{T}$.

TABLE I
TABLE OF SYMBOLS

Notations	Descriptions
$G = (V, E)$	G is an MEC network, V is the set of APs (cloudlets) and E is the set of links between APs.
C_v	The computing capacity of cloudlet v.
d_e	The transmission delay d_e to transmit one unit data along the link $e \in E$.
$\mathbb{S}$, $DT(s)$, v_s and v_u	A set of sensors, a digital twin of sensor $s \in \mathbb{S}$, the cloudlet holding $DT(s)$, and the cloudlet holding the IoT application of user u.
$\mathbb{T}$	The monitoring time horizon.
U and c_u	A set of users and the amount of computing resource of the IoT application of user u.
$\mathcal{T}_u$	The set of time slots in which user u will issue his queries of data retrieving and processing.
K_s	The number of the updates of sensor s delivered to its digital twin within the time horizon.
μ_s	The data uploading rate from sensor s to its allocated AP v_s.
B_s, P_s, and $dist_s$	The bandwidth of AP v_s, the transmission power P_s of sensor s, the distance between sensor s and AP v_s.
η^2 and α	The noise power and the path loss factor.
ρ_s	The volume of data per update of sensor s.
f_s	The processing rate of $DT(s)$ in cloudlet v_s
t_s^{update}	The update delay of digital twin $DT(s)$ defined by Eq. (1)
$d_{s,u}$	The transmission delay of transmitting a unit of data through the shortest path from cloudlet v_s to cloudlet v_u.
λ_s	The size of provided data at $DT(s)$.
t_0	The update sending time of sensor s to generate the current data at $DT(s)$.
t'	The next update sending time of sensor s.
$W_{AoI}(u, t)$ and $W_{delay}(u, t)$	The AoI of the query result by Eq. (2) and the query service delay by Eq. (3).
β	A constant with $0 \le \beta \le 1$ associated with the AoI of the query result.
$W_1(u, t)$ and $W_2(u, t)$	The functions defined by Eq. (7) and Eq. (8), respectively.
$x_{u,v}$	A binary variable, indicating whether the IoT application instance of user $u \in U$ is deployed in cloudlet $v \in V$.
$W_2'(u, t, v)$	The value of $W_2(u, t)$ for the query of user u issuing at time slot t if the IoT application instance of user u is deployed in cloudlet v.
Q_s	The set of queries of users in U to request data of digital twin $DT(s)$ of sensor s over time horizon $\mathbb{T}$.

Definition 3: Given an MEC network $G = (V, E)$, a set $\mathbb{S}$ of sensors, a positive integer K_s for each $s \in \mathbb{S}$, a set U of users with IoT application queries, and time horizon $\mathbb{T}$, assuming digital twins of sensors have already been deployed in cloudlets of V in G, each user $u \in U$ may retrieve data from digital twins of sensors at the beginning of time slots in $\mathcal{T}_u \subseteq \mathbb{T}$. *The IoT application placement problem* in G is to

$$\text{Minimize} \quad \sum_{u \in U} \sum_{t \in \mathcal{T}_u} W_2(u, t), \quad (10)$$

where $W_2(u, t)$ is defined in Eq. (8), by deploying IoT applications of users in U on cloudlets, subject to computing capacities on cloudlets.

Alternatively, there is an Integer Linear Programming (ILP) formulation for the IoT application placement problem as follows.

Let $x_{u,v}$ be a binary variable, where $x_{u,v} = 1$ means the IoT application instance of user $u \in U$ is deployed in cloudlet $v \in V$, and $x_{u,v} = 0$ otherwise. Let $W_2'(u, t, v)$ be the value of $W_2(u, t)$ by Eq. (8) for the query of user u issuing at time slot t if its IoT application instance is deployed in cloudlet v. An ILP solution for the IoT application placement problem is provided as follows.

$$\text{Minimize} \quad \sum_{u \in U} \sum_{t \in \mathcal{T}_u} \sum_{v \in V} (W_2'(u, t, v) \cdot x_{u,v}) \quad (11)$$

subject to:

$$\sum_{u \in U} c_u \cdot x_{u,v} \le C_v, \qquad \forall v \in V \quad (12)$$

$$\sum_{v \in V} x_{u,v} = 1, \qquad \forall u \in U \quad (13)$$

$$x_{u,v} \in \{0, 1\}, \qquad \forall u \in U, \ \forall v \in V. \quad (14)$$

Constraint (12) ensures that the computing capacity constraints on cloudlets can be met. Constraint (13) ensures that each user deploys an IoT application instance in a cloudlet.

We claim that the optimal value of the optimization objective (6) is the sum of the optimal values of optimization objectives of the update scheduling problem and the IoT application placement problem, which will be shown in Lemma 4. Thus, minimizing the optimization objective (5) of the original problem is equivalent to minimizing the optimization objectives of the two sub-problems independently.

A. Optimal algorithm for the update scheduling problem

We propose an optimal solution for the update scheduling problem. We first propose an optimal solution for the update scheduling of a single sensor s. We then obtain an optimal solution to schedule the updates of all sensors by the extension of the solution for sensor s.

Denote by Q_s the set of queries of users in U to request data of digital twin $DT(s)$ of sensor s over time horizon $\mathbb{T}$. Let $u_q \in U$ be the user who issues a query $q \in Q_s$ at time slot t_q with $1 \le t_q \le |\mathbb{T}|$. We define four subsets of queries of Q_s as follows. (1) $Q_s(0, t_1) \subseteq Q_s$ is the set of queries issued earlier than $(t_1 + t_s^{update})$, where t_s^{update} is the update delay of $DT(s)$ by Eq. (1), i.e., $1 \le t_q < t_1 + t_s^{update}$ with
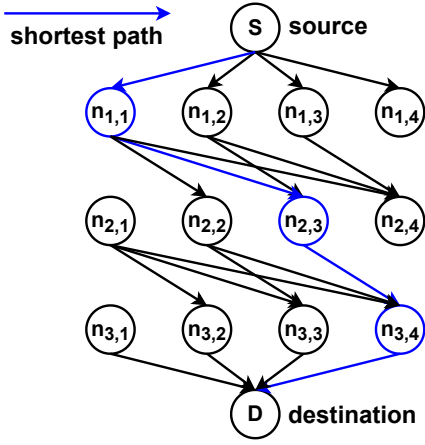
Fig. 2. An example of the auxiliary network $G'_s = (N'_s, E'_s)$ for sensor s, which can send K_s (=3) updates over time horizon $\mathbb{T} = \{1, 2, 3, 4\}$.

Algorithm 1 An optimal algorithm for the update scheduling problem

Input: An MEC network $G = (V, E)$, a set $\mathbb{S}$ of sensors, a positive integer K_s for each $s \in \mathbb{S}$, a set U of users, and time horizon $\mathbb{T}$.

Output: Minimize $\sum_{u \in U} \sum_{t \in \mathcal{T}_u} W_1(u, t)$ by scheduling the updates of sensors in $\mathbb{S}$ over the time horizon $|\mathbb{T}|$.

1: $\mathcal{A}_1 \leftarrow \emptyset$; /* the solution */
2: **for** each sensor $s \in \mathbb{S}$ **do**
3:   Construct an auxiliary graph $G'_s = (N'_s, E'_s)$ for sensor s, and find the shortest path P^*_s in G'_s from source S to destination D, which delivers the optimal solution $\mathcal{A}_{1,s}$ for updating scheduling of sensor s;
4:   $\mathcal{A}_1 \leftarrow \mathcal{A}_1 \cup \{\mathcal{A}_{1,s}\}$;
5: **end for**
6: **return** Solution $\mathcal{A}_1$.

$1 \le t_1 \le |\mathbb{T}|$; (2) $Q_s(t_1, t_2) \subseteq Q_s$ is the set of queries issued no earlier than $(t_1 + t_s^{update})$ but earlier than $(t_2 + t_s^{update})$, i.e., $t_1 + t_s^{update} \le t_q < t_2 + t_s^{update}$ with $1 \le t_1 < t_2 \le |\mathbb{T}|$; (3) $Q_s(t_2, |\mathbb{T}| + 1) \subseteq Q_s$ is the set of queries issued no earlier than $(t_2 + t_s^{update})$, i.e., $t_2 + t_s^{update} \le t_q \le |\mathbb{T}|$ with $1 \le t_2 \le |\mathbb{T}|$; (4) Let $Q_s(0, |\mathbb{T}| + 1) = Q_s$.

Because the queries of all users over the time horizon are the queries requesting data of the digital twins of all sensors over the time horizon, we have $\sum_{s \in \mathbb{S}} \sum_{q \in Q_s} W_1(u_q, t_q) = \sum_{u \in U} \sum_{t \in \mathcal{T}_u} W_1(u, t)$.

To determine whether to utilize the current data at $DT(s)$ or to wait for its next update, we construct an auxiliary graph $G'_s = (N'_s, E'_s)$ with edge weight $w : E'_s \mapsto \mathbb{R}^{\ge 0}$ for sensor $s \in \mathbb{S}$ as follows. The set $N'_s = \{S, D\} \cup \{n_{i,j} \mid 1 \le i \le K_s, \ j \in \mathbb{T}\}$ of nodes and the set $E'_s = \{(S, n_{1,j}) \mid j \in \mathbb{T}\} \cup \{(n_{K_s,j}, D) \mid j \in \mathbb{T}\} \cup \{(n_{i,j}, n_{i+1,j'}) \mid 1 \le i \le K_s - 1, \ 1 \le j < j' \le |\mathbb{T}|\}$ of edges. Especially, we first add virtual nodes S and D as the source and destination, respectively. We also add nodes $n_{i,j}$ with $1 \le i \le K_s$ and $j \in \mathbb{T}$, i.e., the nodes are contained in a K_s-layer structure with $|\mathbb{T}|$ nodes in each layer. We then add edges $(S, n_{1,j})$ in the first layer for each node $n_{1,j}$ with $j \in \mathbb{T}$, and edges $(n_{K_s,j}, D)$ for node $n_{K_s,j}$ with $j \in \mathbb{T}$ in the K_sth layer (the last layer). We add edges $(n_{i,j}, n_{i+1,j'})$ with $1 \le i \le K_s - 1$ and $1 \le j < j' \le |\mathbb{T}|$, i.e., for each $n_{i,j}$ in the ith layer, we add an edge $(n_{i,j}, n_{i+1,j'})$ for each $n_{i+1,j'}$ in the $(i + 1)$th layer. A shortest path in G'_s from source S to destination D will deliver an optimal update scheduling of sensor s, which will be shown later.

The weight assignment of edges in E'_s is given as follows. For each edge $(S, n_{1,j}) \in E'_s$ with $j \in \mathbb{T}$, its weight is $w(S, n_{1,j}) = \sum_{q \in Q_s(0,j)} W_1(u_q, t_q)$, with $W_1(u_q, t_q)$ defined in Eq. (7). If edge $(S, n_{1,j})$ is included in a shortest path in G'_s from S to D, it implies that the first update of sensor s is sent at the beginning of time slot j. For each edge $(n_{i,j}, n_{i+1,j'}) \in E'_s$ with $1 \le i \le K_s - 1$ and $1 \le j < j' \le |\mathbb{T}|$, its weight is $w(n_{i,j}, n_{i+1,j'}) = \sum_{q \in Q_s(j,j')} W_1(u_q, t_q)$. Similarly, if edge $(n_{i,j}, n_{i+1,j'})$ is included in a shortest path in G'_s from S to D, the ith and $(i + 1)$th updates are sent by sensor s at the beginning of time slots j and j', respectively. For each edge $(n_{K_s,j}, D) \in E'_s$ with $j \in \mathbb{T}$, its weight is $w(n_{K_s,j}, D) = \sum_{q \in Q_s(j,|\mathbb{T}|+1)} W_1(u_q, t_q)$. If edge $(n_{K_s,j}, D)$ is included in a shortest path in G'_s from S to D, the K_sth update is sent by sensor s at the beginning of time slot j.

We claim that a shortest path P^*_s in G'_s from S to D corresponds to an optimal solution to the update scheduling of sensor s, i.e., $\sum_{e \in P^*_s} w(e)$ is the minimum value of $\sum_{q \in Q_s} W_1(u_q, t_q)$, which will be shown later in Theorem 2. To this end, we first construct an auxiliary graph G'_s for each sensor $s \in \mathbb{S}$, and find a shortest path P^*_s in each G'_s, and $\sum_{s \in \mathbb{S}} \sum_{e \in P^*_s} w(e)$ is the minimum value of $\sum_{u \in U} \sum_{t \in \mathcal{T}_u} W_1(u, t)$. The found P^*_s is an optimal solution to the update scheduling problem.

An illustrative example of the construction of auxiliary graph G'_s is given in Fig. 2, where sensor s can have K_s (=3) updates over time horizon $\mathbb{T} = \{1, 2, 3, 4\}$. $P^*_s = \{(S, n_{1,1}), (n_{1,1}, n_{2,3}), (n_{2,3}, n_{3,4}), (n_{3,4}, D)\}$ is the shortest path in G'_s from S to D, which implies that K_s (=3) updates of sensor s will be sent to its $DT(s)$ in the beginning of time slot 1, 3, and 4, respectively.

The algorithm for the update scheduling problem is detailed in Algorithm 1.

B. Approximation algorithm for the IoT application placement problem

We propose an approximation algorithm with a provable approximation ratio for the IoT application placement problem, through a reduction to the minimum-cost Generalized Assignment Problem (GAP) [30]. An approximate solution to the minimum-cost GAP will in turn return an approximate solution to the IoT application placement problem.

We reduce the IoT application placement problem to a minimum-cost GAP as follows.

Each IoT application instance of user $u \in U$ is an item u with size c_u, while each cloudlet $v \in V$ is a bin v with capacity C_v. Packing item u to bin v incurs a cost $\sum_{t \in \mathcal{T}_u} W'_2(u, t, v)$. By applying the approximation algorithm [30] for the minimum-cost GAP, an approximation algorithm for the IoT application placement problem then can be derived. Specifically, let $\widetilde{OPT}$ be an optimal fractional solution of the linear relaxation (LP) of the ILP (11) and $\tilde{x}_{u,v} \in [0, 1]$ the fractional value of $x_{u,v}$ by $\widetilde{OPT}$.

Algorithm 2 An approximation algorithm for the IoT application placement problem

---

Input: An MEC network $G = (V, E)$, a set $\mathbb{S}$ of sensors, a positive integer K_s for each $s \in \mathbb{S}$, a set U of users, and time horizon $\mathbb{T}$.

Output: Minimize $\sum_{u \in U} \sum_{t \in \mathcal{T}_u} W_2(u, t)$ by deploying the IoT application instances of users in U on cloudlets in V.

1: $\mathcal{A}_2 \leftarrow \emptyset$; /* the solution */
2: Find a shortest path between each pair of cloudlets;
3: Solve the relaxed LP of the ILP (11);
4: Obtain the optimal solution $\widetilde{OPT}$ of the LP, where $\tilde{x}_{u,v} \in [0, 1]$ is the value of each $x_{u,v}$;
5: Construct a bipartite graph $\mathcal{B} = (\mathcal{R}, \mathcal{V}; \mathcal{E})$ by [30].
6: Identify a minimum-cost matching M in $\mathcal{B}$, where all nodes in $\mathcal{R}$ are matched, via Hungarian algorithm;
7: **for** each edge $(R_u, \gamma_{v,i}) \in M$ **do**
8:     A solution $\mathcal{A}_{2,u}$ for user u is obtained, by deploying the IoT application instance of user u in cloudlet v;
9:     $\mathcal{A}_2 \leftarrow \mathcal{A}_2 \cup \{\mathcal{A}_{2,u}\}$;
10: **end for**
11: **return** Solution $\mathcal{A}_2$.

A bipartite graph $\mathcal{B} = (\mathcal{R}, \mathcal{V}; \mathcal{E})$ is then constructed, by adopting the method in [30], where $\mathcal{R}$ and $\mathcal{V}$ are two disjoint node sets, $\mathcal{R} = \{R_u \mid u \in U\}$, R_u is a node corresponding to the IoT application instance of user $u \in U$, $\mathcal{V} = \{\gamma_{v,i} \mid v \in V, 1 \leq i \leq \eta_v\}$, and $\eta_v = \lceil \sum_{R_u \in \mathcal{R}} \tilde{x}_{u,v} \rceil$ for each cloudlet $v \in V$. The edge set $\mathcal{E}$ of $\mathcal{B}$ consists of edges connecting nodes in $\mathcal{R}$ and $\mathcal{V}$, which is constructed as follows.

Considering each cloudlet $v \in V$, each node in $\{\gamma_{v,i} \mid 1 \leq i \leq \eta_v\}$ is regarded as a bin with capacity 1. Each node $R_u \in \mathcal{R}$ with $\tilde{x}_{u,v} > 0$ is regarded as an item with size of $\tilde{x}_{u,v}$. Sort nodes (items) in $\mathcal{R}$ in non-increasing order of c_u, and let $R_1 \geq R_2 \geq \ldots \geq R_{|U|}$ be the sorted items for notation simplicity. The sorted items then are packed into bins. Specifically, the sorted items are packed to the first bin $\gamma_{v,1}$ one by one until it causes the capacity violation of $\gamma_{v,1}$ by packing an item (e.g., R_u). Then, item R_u is partitioned into two disjoint parts: R_u^1 and R_u^2, such that part R_u^1 packing into bin $\gamma_{v,1}$ makes $\gamma_{v,1}$ have no residual capacity. Part R_u^2 is then packed into the next bin $\gamma_{v,2}$. This procedure repeats until all items in $\mathcal{R}$ are packed. If partial R_u is packed into bin $\gamma_{v,i}$, an edge $(R_u, \gamma_{v,i})$ with cost $\sum_{t \in \mathcal{T}_u} W_2'(u, t, v)$ is added to set $\mathcal{E}$.

Having constructed the bipartite graph $\mathcal{B}$, find a minimum-cost maximum matching M in $\mathcal{B}$, where all nodes in $\mathcal{R}$ are matched. For each edge $(R_u, \gamma_{v,i}) \in M$, the IoT application instance of user u will be deployed in cloudlet v.

The algorithm is detailed in `Algorithm 2`.

C. Approximation algorithm for the minimization problem

We now devise an approximation algorithm for the minimization problem. We decompose the problem into two subproblems - the update scheduling problem, and the IoT application placement problem. We first obtain an optimal solution $\mathcal{A}_1$ to the update scheduling problem by `Algorithm 1`. We then obtain an approximate solution $\mathcal{A}_2$ to the IoT application placement problem by `Algorithm 2`. We finally propose

---

Algorithm 3 An approximation algorithm for the minimization problem

---

Input: An MEC network $G = (V, E)$, a set $\mathbb{S}$ of sensors, a positive integer K_s for each $s \in \mathbb{S}$, a set U of users, and time horizon $\mathbb{T}$.

Output: Minimize $\sum_{u \in U} \sum_{t \in \mathcal{T}_u} W(u, t) / \sum_{u \in U} |\mathcal{T}_u|$, i.e., the average weighted sum of AoIs of query results and query service delays of all queries over $\mathbb{T}$.

1: Formulate the updating scheduling problem, and its solution $\mathcal{A}_1$ is obtained by `Algorithm 1`;
2: Formulate the IoT application placement problem, and its solution $\mathcal{A}_2$ is obtained by `Algorithm 2`;
3: A solution $\mathcal{A}$ is obtained to the minimization problem, by adopting the update scheduling of sensors in $\mathcal{A}_1$ and the IoT application placement of users in $\mathcal{A}_2$;
4: **return** Solution $\mathcal{A}$.

---

an approximation algorithm for the minimization problem, by adopting the update scheduling of sensors in $\mathcal{A}_1$ and the IoT application placement of users in $\mathcal{A}_2$. The algorithm is detailed in `Algorithm 3`.

D. Algorithm analysis

Lemma 1: Let $W^*(u, t)$ be the value of $W(u, t)$ by Eq. (4) in an optimal solution of the minimization problem. Given a query of user u for $DT(s)$ at time slot t, and the update sending time t_0 of sensor s to generate the current data at $DT(s)$, we consider two cases: Case 1. There is no further update of sensor s before time horizon $\mathbb{T}$ ends. User u then can only retrieve the current data of $DT(s)$, and we have $W^*(u, t) = \lambda_s \cdot d_{s,u} + \lambda_s / f_u + \beta \cdot (t - t_0)$. Case 2. Assuming the next update of s is scheduled at time slot t', we have $W^*(u, t) = \lambda_s \cdot d_{s,u} + \lambda_s / f_u + \min\{\beta \cdot (t - t_0), t_s^{update} + (1 - \beta) \cdot (t' - t)\}$, and user u prefers to retrieve the current data of $DT(s)$ to minimize $W(u, t)$, if $\beta \cdot (t - t_0) < t_s^{update} + (1 - \beta) \cdot (t' - t)$; otherwise, user u prefers to wait for the next update of $DT(s)$.

Proof We show the claim by distinguishing the following two cases.

Case 1. Due to no further update on $DT(s)$ from now on until the end of the time horizon, user u cannot wait for the next update of $DT(s)$ anymore. The user can only retrieve the current data of $DT(s)$. From Eq. (2), (3) and (4), we have

$$W^*(u, t) = \lambda_s \cdot d_{s,u} + \lambda_s / f_u + \beta \cdot (t - t_0). \quad (15)$$

Case 2. From Eq. (2), (3) and (4), if user u retrieves the data at $DT(s)$ at time slot t, we have

$$W(u, t) = \lambda_s \cdot d_{s,u} + \lambda_s / f_u + \beta \cdot (t - t_0). \quad (16)$$

Otherwise (i.e., user u waits for the next update of $DT(s)$),

$$W(u, t) = \lambda_s \cdot d_{s,u} + \lambda_s / f_u + t_s^{update} + (1 - \beta) \cdot (t' - t). \quad (17)$$

Therefore, if user u prefers retrieving the current data of $DT(s)$, we have

$$\beta \cdot (t - t_0) < t_s^{update} + (1 - \beta) \cdot (t' - t). \quad (18)$$

Also, $W^*(u,t)$ is the smaller one between Eq. (16) and (17), i.e.,

$$W^*(u,t) = \lambda_s \cdot d_{s,u} + \lambda_s/f_u + \min\{\beta \cdot (t - t_0),\ t_s^{update} + (1 - \beta) \cdot (t' - t)\}. \tag{19}$$

∎

Lemma 2: Given a query of user u at time slot t for data at $DT(s)$, the update sending time t_0 of sensor s to generate the current data at $DT(s)$, and the next update sending time t' of sensor s if available, (i) the value of $W_1(u,t)$ by Eq. (7) is determined by the update scheduling of sensor s, and shows whether to retrieve current data at $DT(s)$ or wait for its next update; and (ii) the value of $W_2(u,t)$ by Eq. (8) is determined by the IoT application instance placement of user u.

Proof (i) Recall that t_s^{update} is a constant, i.e., the update delay of $DT(s)$ by Eq. (1), and β is a constant in Eq. (4). Then $W_1(u,t)$ is determined by the update scheduling of sensor s (i.e., determining values of t_0 and t'). By Lemma 1, the $\min\{\cdot\}$ operation in Eq. (7) for $W_1(u,t)$ shows whether to retrieve the current data at $DT(s)$ or wait for its next update.

(ii) Recall that $d_{s,u}$ is the transmission delay of transmitting a unit of data through the shortest path between cloudlets v_s and v_u, where v_s holds $DT(s)$, and v_u holds the IoT application instance of user u, while λ_s is the size of the generated data at $DT(s)$, and f_u is the processing rate of the IoT application instance of u. As f_u and λ_s are constants, the value of $W_2(u,t)$ is only determined by the IoT application placement of user u (i.e., determining the value of $d_{s,u}$). ∎

Lemma 3: Given a sensor s with K_s updates to be sent over the time horizon $\mathbb{T}$, and the constructed auxiliary graph $G'_s = (N'_s, E'_s)$, (i) each potential update scheduling of s over time horizon $\mathbb{T}$ corresponds to a potential path in G'_s from source S to destination D; and (ii) a potential path in G'_s from source S to destination D corresponds to a feasible update scheduling of s over the time horizon $\mathbb{T}$.

Proof (i) Assume that a potential update scheduling of sensor s is at time slots $t_1, t_2, \ldots, t_{K_s}$, respectively, with $1 \leq t_1 < t_2 < \ldots < t_{K_s} \leq |\mathbb{T}|$. Then we can construct a path P_s in G'_s from S to D with $P_s = \{(S, n_{1,t_1}), (n_{1,t_1}, n_{2,t_2}), \ldots, (n_{K_s-1,t_{K_s-1}}, n_{K_s,t_{K_s}}), (n_{K_s,t_{K_s}}, D)\}$. Now, we show that path P_s is feasible, i.e., all edges in P_s exist in G'_s. We add edges $(S, n_{1,j})$ for each node $n_{1,j}$ with $j \in \mathbb{T}$ in G'_s, so edge (S, n_{1,t_1}) exists in G'_s. Then, edges $\{(n_{1,t_1}, n_{2,t_2}), \ldots, (n_{K_s-1,t_{K_s-1}}, n_{K_s,t_{K_s}})\}$ exist in G'_s, because we also add edges $(n_{i,j}, n_{i+1,j'})$ with $1 \leq i \leq K_s - 1$ and $1 \leq j < j' \leq |\mathbb{T}|$. Edge $(n_{K_s,t_{K_s}}, D)$ exists in G'_s, as we add edges $(n_{K_s,j}, D)$ for each $n_{K_s,j}$ with $j \in \mathbb{T}$. Thus, path P_s is feasible because all edges in P_s exist in G'_s.

(ii) Let P_s be a potential path in G'_s from source S to destination D. Because P_s starts from S and only edges $(S, n_{1,j})$ with $1 \leq j \leq |\mathbb{T}|$ start at S, we assume that the first edge of path P_s is (S, n_{1,t_1}) with $1 \leq t_1 \leq |\mathbb{T}|$. Also, only edges $(n_{1,t_1}, n_{2,j'})$ start from node n_{1,t_1} with $1 \leq t_1 < j' \leq |\mathbb{T}|$, because we add edges $(n_{i,j}, n_{i+1,j'})$ with $1 \leq i \leq K_s - 1$ and $1 \leq j < j' \leq |\mathbb{T}|$. Then

we assume that the second edge of P_s is (n_{1,t_1}, n_{2,t_2}) with $1 \leq t_1 < t_2 \leq |\mathbb{T}|$. Similarly, the first K_s edges of P_s are $(S, n_{1,t_1}), (n_{1,t_1}, n_{2,t_2}), \ldots, (n_{K_s-1,t_{K_s-1}}, n_{K_s,t_{K_s}})$ with $1 \leq t_1 < t_2 < \ldots < t_{K_s} \leq |\mathbb{T}|$. The last edge of P_s is $(n_{K_s,t_{K_s}}, D)$ as only this edge starts from $n_{K_s,t_{K_s}}$ and reaches D. In such a potential path $P_s = \{(S, n_{1,t_1}), (n_{1,t_1}, n_{2,t_2}), \ldots, (n_{K_s-1,t_{K_s-1}}, n_{K_s,t_{K_s}}), (n_{K_s,t_{K_s}}, D)\}$, the derived update scheduling (i.e., send updates at time $t_1, t_2, \ldots, t_{K_s}$) is feasible, because there are K_s updates and $1 \leq t_1 < t_2 < \ldots < t_{K_s} \leq |\mathbb{T}|$. ∎

Theorem 2: Given an MEC network $G = (V, E)$, a set $\mathbb{S}$ of sensors, a positive integer K_s for each sensor $s \in \mathbb{S}$, a set U of users with IoT application queries, and time horizon $\mathbb{T}$, assuming digital twins of sensors have already been deployed in cloudlets of V of G, a user $u \in U$ may retrieve data from digital twins of sensors at the beginning of time slot $t \in \mathcal{T}_u \subseteq \mathbb{T}$. Algorithm 1 delivers an optimal solution to the update scheduling problem, and takes $O(|U| \cdot |\mathbb{T}| + |\mathbb{S}| \cdot K_{max}^2 \cdot |\mathbb{T}|^2)$ time, where $K_{max} = \max\{K_s \mid s \in \mathbb{S}\}$.

Proof By Lemma 3, let P_s be a potential path in G'_s from S to D with $P_s = \{(S, n_{1,t_1}), (n_{1,t_1}, n_{2,t_2}), \ldots, (n_{K_s-1,t_{K_s-1}}, n_{K_s,t_{K_s}}), (n_{K_s,t_{K_s}}, D)\}$, and the derived update scheduling of sensor s is to send its updates at time $t_1, t_2, \ldots, t_{K_s}$, respectively. We have $w(S, n_{1,t_1}) = \sum_{q \in Q_s(0,t_1)} W_1(u_q, t_q)$ with $1 \leq t_q < t_1 + t_s^{update}, \forall q \in Q_s(0, t_1)$. Also, $w(n_{1,t_1}, n_{2,t_2}) = \sum_{q \in Q_s(t_1,t_2)} W_1(u_q, t_q)$, with $t_1 + t_s^{update} \leq t_q < t_2 + t_s^{update}, \forall q \in Q_s(t_1, t_2)$. Then, $w(S, n_{1,t_1}) + w(n_{1,t_1}, n_{2,t_2}) = \sum_{q \in Q_s(0,t_2)} W_1(u_q, t_q)$ with $1 \leq t_q < t_2 + t_s^{update}, \forall q \in Q_s(0, t_2)$. Similarly, $w(S, n_{1,t_1}) + w(n_{1,t_1}, n_{2,t_2}) + \cdots + w(n_{K_s-1,t_{K_s-1}}, n_{K_s,t_{K_s}}) = \sum_{q \in Q_s(0,t_{K_s})} W_1(u_q, t_q)$ with $1 \leq t_q < t_{K_s} + t_s^{update}, \forall q \in Q_s(0, t_{K_s})$. Finally $w(n_{K_s,t_{K_s}}, D) = \sum_{q \in Q_s(t_{K_s},|\mathbb{T}|+1)} W_1(u_q, t_q)$, with $t_{K_s} + t_s^{update} \leq t_q \leq |\mathbb{T}|, \forall q \in Q_s(t_{K_s}, |\mathbb{T}| + 1)$. Therefore, $\sum_{e \in P_s} w(e) = w(S, n_{1,t_1}) + w(n_{1,t_1}, n_{2,t_2}) + \cdots + w(n_{K_s,t_{K_s}}, D) = \sum_{q \in Q_s} W_1(u_q, t_q)$.

The shortest path P_s^* in G'_s corresponds to a feasible update scheduling of sensor s for the given time horizon $\mathbb{T}$ with the minimum $\sum_{q \in Q_s} W_1(u_q, t_q)$ by Lemma 3. Therefore, Algorithm 1 delivers an optimal update scheduling of each $s \in \mathbb{S}$. Because the update scheduling of sensor s does not affect that of another sensor s', Algorithm 1 delivers an optimal solution to the update scheduling problem.

The time complexity of Algorithm 1 is analyzed as follows. For each sensor $s \in \mathbb{S}$, we construct an auxiliary graph $G'_s = (N'_s, E'_s)$, where the cardinality of set N'_s is $O(K_s \cdot |\mathbb{T}|)$. Finding a shortest path in G'_s from S to D takes $O(K_s^2 \cdot |\mathbb{T}|^2)$ time, and there are at most $|U| \cdot |\mathbb{T}|$ queries. Thus, Algorithm 1 takes $O(|U| \cdot |\mathbb{T}| + |\mathbb{S}| \cdot K_{max}^2 \cdot |\mathbb{T}|^2)$ time. ∎

Theorem 3: Given an MEC network $G = (V, E)$, a set $\mathbb{S}$ of sensors, a positive integer K_s for each sensor $s \in \mathbb{S}$, a set U of users, and time horizon $\mathbb{T}$, assuming digital twins of sensors have already been deployed in cloudlets of V in G, a user $u \in U$ may retrieve data from digital twins of sensors at the beginning of time slot $t \in \mathcal{T}_u \subseteq \mathbb{T}$. There is an approximation algorithm, Algorithm 2, for the IoT application placement problem. The solution value by Algorithm 2 is no greater than that of the optimal solution, and the computing resource

consumed in each cloudlet $v \in V$ is no greater than twice its computing capacity. `Algorithm` 2 takes $O(|U|^3 \cdot |V|^3)$ time.

Proof Because we reduce the IoT application placement problem to the minimum-cost GAP, and devise `Algorithm` 2 for the problem by adopting the approximation technique in [30], readers can refer to [30] for more details, which are omitted, due to space limitation. ∎

Lemma 4: Let OPT be the optimal solution to the problem of concern, and let OPT_1 and OPT_2 be the optimal solutions to the update scheduling problem and the IoT application placement problem, respectively. Then, $OPT = \frac{OPT_1 + OPT_2}{\sum_{u \in U} |\mathcal{T}_u|}$.

Proof Let $W^*(u, t)$ be the value of $W(u, t)$ by Eq. (4) in OPT. Let $W_1^*(u, t)$ be the value of $W_1(u, t)$ by Eq. (7) in OPT_1 and $W_2^*(u, t)$ the value of $W_2(u, t)$ by Eq. (8) in OPT_2, respectively. Then, $OPT = \frac{\sum_{u \in U} \sum_{t \in \mathcal{T}_u} W^*(u, t)}{\sum_{u \in U} |\mathcal{T}_u|}$, $OPT_1 = \sum_{u \in U} \sum_{t \in \mathcal{T}_u} W_1^*(u, t)$, and $OPT_2 = \sum_{u \in U} \sum_{t \in \mathcal{T}_u} W_2^*(u, t)$. We show that $\sum_{u \in U} \sum_{t \in \mathcal{T}_u} W^*(u, t) = \sum_{u \in U} \sum_{t \in \mathcal{T}_u} W_1^*(u, t) + \sum_{u \in U} \sum_{t \in \mathcal{T}_u} W_2^*(u, t)$ as follows.

By Lemma 1, Lemma 2, Eq. (7) and Eq. (8), it can be seen that a feasible solution $W'(u, t)$ can be obtained, by combining the optimal solutions $W_1^*(u, t)$ and $W_2^*(u, t)$ for the update scheduling problem and IoT application placement problem, respectively, i.e.,

$$W'(u, t) = W_1^*(u, t) + W_2^*(u, t). \qquad (20)$$

Because of $\sum_{u \in U} \sum_{t \in \mathcal{T}_u} W'(u, t)$ indicating a feasible solution OPT' to the problem, we have $\sum_{u \in U} \sum_{t \in \mathcal{T}_u} W'(u, t) \geq \sum_{u \in U} \sum_{t \in \mathcal{T}_u} W^*(u, t)$.

We then show that $\sum_{u \in U} \sum_{t \in \mathcal{T}_u} W'(u, t) = \sum_{u \in U} \sum_{t \in \mathcal{T}_u} W^*(u, t)$ by contradiction. We assume $OPT' = \frac{\sum_{u \in U} \sum_{t \in \mathcal{T}_u} W'(u, t)}{\sum_{u \in U} |\mathcal{T}_u|} > \frac{\sum_{u \in U} \sum_{t \in \mathcal{T}_u} W^*(u, t)}{\sum_{u \in U} |\mathcal{T}_u|} = OPT$. Because OPT outperforms OPT', OPT must adopt either another update scheduling of sensors (different from OPT_1) or another IoT application placement (different from OPT_2), such that $OPT < OPT'$. However, such an update scheduling of sensors or IoT application placement will lead to a larger objective value of either the update scheduling problem or the IoT application placement problem than OPT_1 and OPT_2, respectively. This contradicts that OPT_1 and OPT_2 are the optimal solutions of the two problems. Therefore, we have $\sum_{u \in U} \sum_{t \in \mathcal{T}_u} W'(u, t) = \sum_{u \in U} \sum_{t \in \mathcal{T}_u} W^*(u, t)$.

By Eq. (20), we have $\sum_{u \in U} \sum_{t \in \mathcal{T}_u} W^*(u, t) = \sum_{u \in U} \sum_{t \in \mathcal{T}_u} W_1^*(u, t) + \sum_{u \in U} \sum_{t \in \mathcal{T}_u} W_2^*(u, t)$. Thus, we have $OPT = \frac{OPT_1 + OPT_2}{\sum_{u \in U} |\mathcal{T}_u|}$. ∎

Theorem 4: Given an MEC network $G = (V, E)$, a set $\mathbb{S}$ of sensors, a positive integer K_s for each sensor $s \in \mathbb{S}$, a set U of users with IoT application queries, and time horizon $\mathbb{T}$, assuming that digital twins of sensors have already been deployed in cloudlets of V in G, a user $u \in U$ may retrieve data from digital twins of sensors at the beginning of time slot $t \in \mathcal{T}_u \subseteq \mathbb{T}$. There is an approximation algorithm, `Algorithm` 3, for the minimization problem. The solution value by `Algorithm` 3 is no greater than that of the optimal solution, and the computing resource consumed in each

---

Algorithm 4 An algorithm for the IoT application placement problem without resource violations

---

Input: An MEC network $G = (V, E)$, a set $\mathbb{S}$ of sensors, a positive integer K_s for each $s \in \mathbb{S}$, a set U of users, and time horizon $\mathbb{T}$.

Output: Minimize $\sum_{u \in U} \sum_{t \in \mathcal{T}_u} W_2(u, t)$ by deploying IoT application instances of queries in U on cloudlets.

1: $\mathcal{A}_2' \leftarrow \emptyset$; /* the solution */
2: $l \leftarrow 1$;
3: $\mathbb{U}^{(l)} \leftarrow U$, $\mathbb{V}^{(l)} \leftarrow V$, and identify $\mathbb{E}^{(l)}$;
4: **while** $\mathbb{E}^{(l)} \neq \emptyset$ **do**
5:    Construct bipartite graph $\mathbb{B}^{(l)} = (\mathbb{U}^{(l)}, \mathbb{V}^{(l)}; \mathbb{E}^{(l)})$;
6:    Find a minimum-cost maximum matching $\mathcal{M}_l$ in $\mathbb{B}^{(l)}$, via the Hungarian algorithm;
7:    **for** each matching edge $e(u, v)$ in $\mathcal{M}_l$ **do**
8:      A solution $\mathcal{A}_{2,u}'$ for user u is obtained, by deploying the IoT application instance of user u in cloudlet v;
9:    **end for**
10:    $\mathcal{A}_2' \leftarrow \mathcal{A}_2' \cup \{\mathcal{A}_{2,u}'\}$;
11:    $l \leftarrow l + 1$;
12:    Update $\mathbb{U}^{(l)}$, $\mathbb{V}^{(l)}$ and $\mathbb{E}^{(l)}$;
13: **end while**
14: **return** Solution $\mathcal{A}_2'$.

---

cloudlet $v \in V$ is no greater than twice its computing capacity. `Algorithm` 3 takes $O(|U| \cdot |\mathbb{T}| + |\mathbb{S}| \cdot K_{max}^2 \cdot |\mathbb{T}|^2 + |U|^3 \cdot |V|^3)$ time with $K_{max} = \max\{K_s \mid s \in \mathbb{S}\}$.

Proof Let OPT, OPT_1, and OPT_2 be the optimal solutions of the minimization problem, the update scheduling problem, and the IoT application placement problem, respectively. Let $\mathcal{A}$, $\mathcal{A}_1$, and $\mathcal{A}_2$ be the values of the solutions by `Algorithm` 3, `Algorithm` 1, and `Algorithm` 2, respectively. We have $\mathcal{A}_1 = OPT_1$ by Theorem 2, $\mathcal{A}_2 \leq OPT_2$ by Theorem 3, and $OPT = \frac{OPT_1 + OPT_2}{\sum_{u \in U} |\mathcal{T}_u|}$ by Lemma 4. From Lemma 1, Eq. (7) and (8), we have $\mathcal{A} = \frac{\mathcal{A}_1 + \mathcal{A}_2}{\sum_{u \in U} |\mathcal{T}_u|} \leq \frac{OPT_1 + OPT_2}{\sum_{u \in U} |\mathcal{T}_u|} = OPT$ with the computing resource consumed of each cloudlet no greater than twice its computing capacity, by Theorem 3.

`Algorithm` 3 takes the time $O(|U| \cdot |\mathbb{T}| + |\mathbb{S}| \cdot K_{max}^2 \cdot |\mathbb{T}|^2 + |U|^3 \cdot |V|^3)$, by time complexity of `Algorithm` 1 and `Algorithm` 2 in Theorem 2 and 3, respectively. ∎

V. HEURISTIC ALGORITHM WITHOUT COMPUTING CAPACITY VIOLATIONS

In the previous section, we developed an approximate solution for the minimization problem at the expense of bounded computing capacity violations. In this section we devise an efficient heuristic algorithm for the problem without computing capacity violation as follows.

A. Algorithm for the IoT application placement problem

The proposed algorithm is based on a series of minimum-cost maximum matchings on their corresponding auxiliary graphs. Specifically, the algorithm proceeds iteratively. Within iteration l, we build a bipartite graph $\mathbb{B}^{(l)} = (\mathbb{U}^{(l)}, \mathbb{V}^{(l)}; \mathbb{E}^{(l)})$, where $\mathbb{U}^{(l)}$ is the set of users, and their IoT applications

Algorithm 5 An algorithm for the minimization problem
___
Input: An MEC network $G = (V, E)$, a set $\mathbb{S}$ of sensors, a positive integer K_s for each $s \in \mathbb{S}$, a set U of users, and time horizon $\mathbb{T}$.

Output: Minimize $\sum_{u \in U} \sum_{t \in \mathcal{T}_u} W(u, t) / \sum_{u \in U} |\mathcal{T}_u|$, i.e., the average weighted sum of AoIs of query results and query service delays of all queries over $\mathbb{T}$.

1: Formulate an updating scheduling problem and obtain its solution $\mathcal{A}_1$ by `Algorithm 1`;

2: Formulate an IoT application placement problem and obtain its solution $\mathcal{A}'_2$ by `Algorithm 4`;

3: A solution $\mathcal{A}'$ to the problem is obtained by adopting the update scheduling of sensors in $\mathcal{A}_1$ and the IoT application placement of users in $\mathcal{A}'_2$;

4: **return** Solution $\mathcal{A}'$.
___

have not been placed before iteration l. $\mathbb{V}^{(l)}$ is the set of cloudlets possessing residual computing resource in iteration l. We have $\mathbb{U}^{(1)} = U$, and $\mathbb{V}^{(1)} = V$ initially. $\mathbb{E}^{(l)}$ is a set of edges in iteration l, and there exists an edge $e(u, v)$ in $\mathbb{E}^{(l)}$ between a user $u \in \mathbb{U}^{(l)}$ and a cloudlet $v \in \mathbb{V}^{(l)}$ with weight $\sum_{t \in \mathcal{T}_u} W'_2(u, t, v)$ if cloudlet v has sufficient residual resource to establish an IoT application instance for user u.

Denote by $\mathcal{M}_l$ a minimum-cost maximum matching in $\mathbb{B}^{(l)}$. For each matching edge $e(u, v) \in \mathcal{M}_l$, we deploy the IoT application of user u in cloudlet v, and the computing resource c_u is subtracted from cloudlet v. Then, the subsequent auxiliary bipartite graph is built. This process continues until the instances of IoT applications of all users are deployed. Let L be the number of iterations of the proposed algorithm. Then, the solution delivered by the algorithm is $\cup_{l=1}^{L} \mathcal{M}_l$. Let $c(\mathcal{M}_l)$ be the weighted sum of edges in $\mathcal{M}_l$. Then, $\sum_{l=1}^{L} c(\mathcal{M}_l)$.

The heuristic algorithm is detailed in `Algorithm 4`.

B. Heuristic algorithm for the minimization problem

In the following we devise an algorithm for the minimization problem. Following the spirit of `Algorithm 3`, we decompose the problem into two sub-problems: the update scheduling problem, and the IoT application placement problem. We obtain an optimal solution $\mathcal{A}_1$ for the update scheduling problem, by invoking `Algorithm 1`, and a feasible solution $\mathcal{A}'_2$ to the IoT application placement problem by `Algorithm 4`, via adopting the update scheduling of sensors in $\mathcal{A}_1$ and the IoT application placement of users in $\mathcal{A}'_2$. The detailed algorithm is presented in `Algorithm 5`.

C. Algorithm analysis

Theorem 5: Given an MEC network $G = (V, E)$, a set $\mathbb{S}$ of sensors, a positive integer K_s for each sensor $s \in \mathbb{S}$, a set U of users, and a finite time horizon $\mathbb{T}$, assuming that digital twins of sensors have already been deployed in cloudlets of V, each user $u \in U$ may retrieve data from digital twins of sensors in the beginning of time slot $t \in \mathcal{T}_u \subseteq \mathbb{T}$. There is an algorithm, `Algorithm 4`, for the IoT application placement problem, which takes $O(|U| \cdot (|U| + |V|)^3)$ time and delivers a feasible solution.

Proof `Algorithm 4` delivers a feasible solution for the IoT application placement problem, because there are no violations on any constraints. The time complexity of `Algorithm 4` is analyzed as follows. It takes $O((|U| + |V|)^3)$ time to find the minimum-cost maximum matching in the bipartite graph $\mathbb{B}^{(l)}$, and there are at most $|U|$ iterations in the proposed algorithm, because at least an IoT application of one user is deployed in each iteration. Thus, the time complexity of `Algorithm 4` is $O(|U| \cdot (|U| + |V|)^3)$. ∎

Theorem 6: Given an MEC network $G = (V, E)$, a set $\mathbb{S}$ of sensors, a positive integer K_s for each sensor $s \in \mathbb{S}$, a set U of users with IoT application queries, and a finite time horizon $\mathbb{T}$, assuming that digital twins of sensors have already been deployed in cloudlets of V, each user $u \in U$ may retrieve data from digital twins of sensors at the beginning of time slot $t \in \mathcal{T}_u \subseteq \mathbb{T}$. There is an algorithm, `Algorithm 5`, for the minimization problem, which takes $O(|U| \cdot |\mathbb{T}| + |\mathbb{S}| \cdot K_{max}^2 \cdot |\mathbb{T}|^2 + |U| \cdot (|U| + |V|)^3)$ time, where $K_{max} = \max\{K_s \mid s \in \mathbb{S}\}$.

Proof `Algorithm 5` delivers a feasible solution for the minimization problem, as invoking `Algorithm 1` or `Algorithm 4` does not cause any resource capacity violations. Also, `Algorithm 5` takes time $O(|U| \cdot |\mathbb{T}| + |\mathbb{S}| \cdot K_{max}^2 \cdot |\mathbb{T}|^2 + |U| \cdot (|U| + |V|)^3)$, due to the time complexities of `Algorithm 1` and `Algorithm 4` by Theorem 2 and Theorem 5, respectively. ∎

VI. PERFORMANCE EVALUATION

In this section, we evaluated the algorithm performance via simulations.

A. Experimental environment settings

Consider an MEC network, in which the number of APs ranges from 50 to 250, and there is a co-located cloudlet with each AP. We leverage GT-ITM [5] to construct different topologies of MEC networks. The capacity on a cloudlet ranges from $10,000$ MHz to $20,000$ MHz [39], and bandwidth capacity on each AP is set within $[5, 20]$ MHz [31]. The transmission delay of one unit data (one MB) along a link ranges from 0.2 ms to 1 ms [39]. There are 500 sensors, and each of them is in the proximity of an AP randomly with a distance from 10 meters to 50 meters. The number of updates K_s of each sensor s ranges from 10 to 30 for a given finite time horizon. The transmission power P_s of each sensor s ranges from 0.1 Watt to 0.5 Watt [4], while the path loss factor α and the noise power η^2 are set as 4 [4] and 1×10^{-10} Watt [19], respectively. There are $1,000$ users, while the computing resource demanded by an IoT application instance or a digital twin is set within $[300, 600]$ MHz [25]. The number of CPU cycles required for 1-bit task calculation is set within $[200, 400]$ cycles/bit [23]. There are 100 time slots with each lasting 50 ms. Each user issues a query for a sensor randomly at each time slot. The volume of the update data of a sensor ranges from 1 MB to 5 MB [35], and the volume of data generated at a digital twin per update is set within $[2, 10]$ MB. Parameter β in Eq. (4) is set as 0.5. The value in

(a) The performance   (b) The running time   (c) Utilization ratio of cloudlets of algorithm Appro
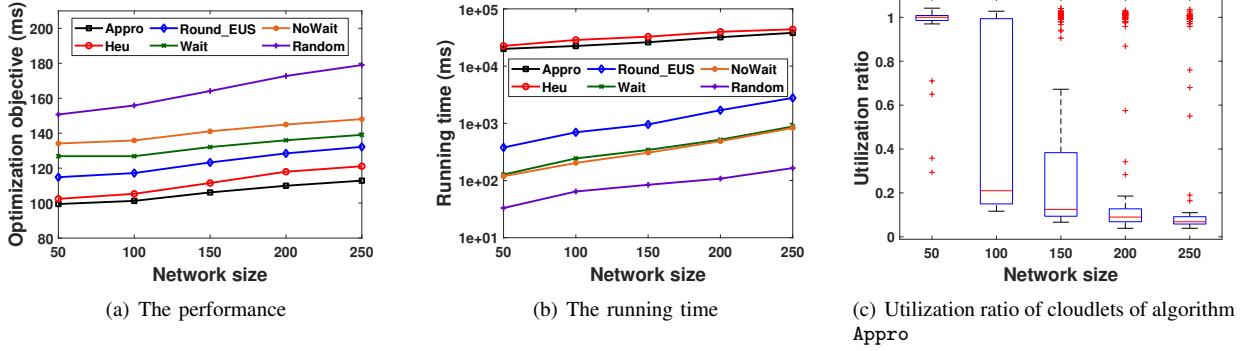
Fig. 3. Performance of different algorithms for the minimization problem by varying network size.

each figure represents the mean based on 30 MEC instances of the same size. The actual running time of each algorithm is obtained by a desktop with 3.60GHz Intel 8-Core i7 CPU and 16GB RAM. Unless otherwise specified, these parameters are adopted by default.

We refer to Algorithm 3 and Algorithm 5 for the minimization problem as Appro and Heu, respectively, and we evaluated their performance against the following three benchmarks.

- Algorithm Round_EUS: It invokes a randomized rounding algorithm from [41] for IoT application placements, through the LP relaxation of the ILP (11). Each sensor adopts an Exact Uniform Scheduler (EUS) [10], i.e., each sensor delivers its updates evenly over the given time horizon. Each query is admitted through minimizing its weighted sum of the AoI of its query result and its query service delay, by determining whether to utilize the current data at $DT(s)$ or to wait for the next update of sensor s.
- Algorithm Wait: each user deploys his IoT application instance in a cloudlet such that the average transmission delay from the requested digital twin to the IoT application instance per query is minimized. Each sensor delivers its updates evenly over the given time horizon by adopting EUSs [10], and each query waits for the next update of its requested digital twin.
- Algorithm NoWait: similar to algorithm Wait, but queries retrieve the current data at their digital twins immediately.
- Algorithm Random: IoT application instances are deployed in cloudlets randomly. Sensors randomly send their updates to their digital twins, while queries can either retrieve the current data of digital twins or wait for their updates, and such actions are randomly chosen.

B. Performance evaluation of different algorithms

We first studied the performance of Appro and Heu against benchmarks Round_EUS, Wait, NoWait and Random, by varying the network size from 50 to 250, where the utilization ratio of cloudlet v is the ratio of the amount of computing resource consumed to its capacity. Fig. 3 plots the performance (the optimization objective (5)) and running times

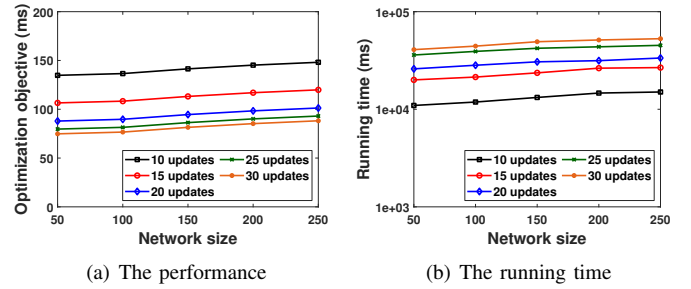(a) The performance   (b) The running time

Fig. 4. Impact of the number of updates of each sensor for the given time horizon on the performance of algorithm Appro.

of different algorithms, and the utilization ratios of cloudlets by algorithm Appro. Shown in Fig. 3(a), with the network size of 250, Appro outperforms Heu by 6.8%, while Heu outperforms Round_EUS, Wait, NoWait and Random by 8.4%, 12.9%, 18.2% and 32.4%, respectively. It can be seen from Fig. 3(b) that algorithm Random takes the least running time, because it makes decisions randomly. Meanwhile, algorithm Heu takes the longest running time, because it takes time to find a shortest path in the auxiliary graph for each sensor to schedule the updates of the sensor, and then to find a series of minimum-cost maximum matchings in corresponding bipartite graphs for IoT application instance placements. Fig. 3(c) shows that the computing capacity violation on any cloudlet by algorithm Appro is no greater than 4.1%. Fig. 3 demonstrates algorithms Appro and Heu outperform algorithms Round_EUS, Wait, NoWait and Random. The rationale behind is that both Appro and Heu can jointly optimize the freshness of query results and query service delays of all queries efficiently.

C. Impact of important parameters on the performance of approximation algorithm Appro

We then investigated the impact of the number of updates of each sensor on the performance of Appro, by varying the number of updates per sensor from 10 to 30. It can be seen from Fig. 4(a) that the performance of Appro with 30 updates within the given time horizon is 40.5% higher than that of itself with 10 updates in the same period when network size is set at 250. This indicates that the use of digital twins can deliver much fresher data through frequent updates of sensors. In Fig. 4(b), algorithm Appro with 30 updates takes the longest time because a large number of updates from a sensor leads to
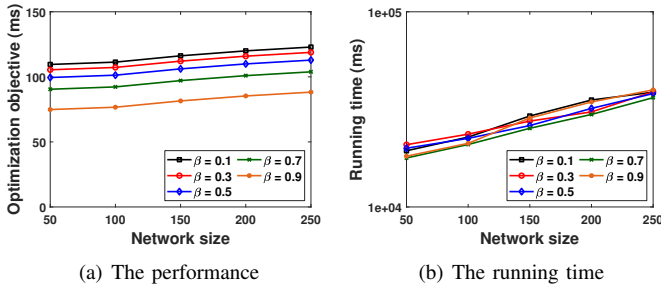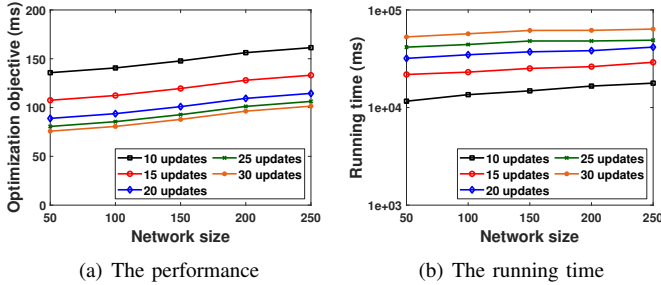
(a) The performance

(b) The running time

Fig. 5. Impact of parameter β on the performance of algorithm Appro.

(a) The performance

(b) The running time

Fig. 6. Impact of the number of updates of each sensor for the given time horizon on the performance of algorithm Heu.

a large auxiliary graph for the updating scheduling, as shown in Section IV-A. We also evaluated the impact of parameter β on the performance of Appro, where β is a coefficient of the AoI of query results in Eq. (4). Fig. 5 plots the performance curves of Appro. When the network size is fixed at 250, the performance of Appro with $\beta = 0.9$ is 28.2% higher than its performance with $\beta = 0.1$, as demonstrated in Fig. 5(a). A larger β represents a larger weight assigned to the average AoI of query results, and meanwhile, a smaller weight $(1 - \beta)$ is assigned to the average query service delay, too. It can be seen from Fig. 5(b) that the impact of different values of β on the running time of Appro is negligible.

D. Impact of important parameters on the performance of heuristic algorithm Heu

We finally studied the impact of the number of update scheduling per sensor on the performance of algorithm Heu, by varying the number of updates from 10 to 30, respectively. Similar to Fig. 4(a), it can be seen from Fig. 6(a) that algorithm Heu with 30 updates outperforms itself with 10 updates by 37.1% when the network size is 250, because more updates for each sensor are scheduled for the given time horizon in order to deliver fresher digital twin data. Meanwhile, Fig. 6(b)

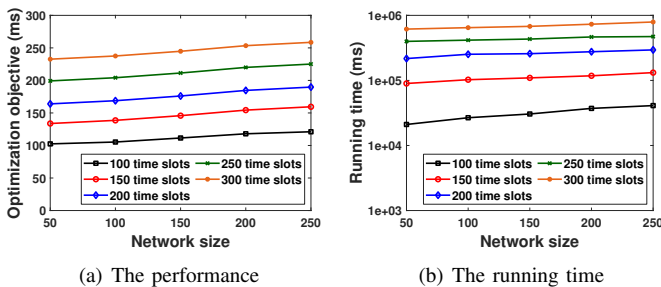(a) The performance

(b) The running time

Fig. 7. Impact of time horizon length on the performance of algorithm Heu.

shows that algorithm Heu with 10 updates takes the least running time among the comparison algorithms. The rest is to study the impact of length $|\mathbb{T}|$ of the finite time horizon on the performance of algorithm Heu. Fig. 7 plots the performance curve of Heu by varying the value of $|\mathbb{T}|$ from 100 to 300. When the network size reaches 250, Fig. 7(a) indicates that algorithm Heu with $|\mathbb{T}| = 100$ outperforms itself with $|\mathbb{T}| = 300$ by 53.2%, since sensors can provide fresher digital twin data for queries, through more frequent updates. Fig. 7(b) indicates that Heu with $|\mathbb{T}| = 300$ takes the longest running time, due to that it takes much more time to find a shortest path in a larger auxiliary graph for each sensor.

VII. CONCLUSION AND FUTURE WORK

In this paper, we investigated AoI-aware IoT query service provisioning in an MEC network empowered by the digital twin technology. We first formulated a novel minimization problem of jointly considering the accumulative freshness of query results and the total query service delay of admitted queries of IoT services, with the aim to minimize the weighted sum of AoIs of query results and query service delays of admitted queries, and we showed the NP-hardness of the defined problem. We then devised a performance-guaranteed approximation algorithm for the problem, at the expense of bounded computing capacity violations. Also, We proposed an efficient heuristic for the problem without computing capacity violations. We finally evaluated the performance of the proposed algorithms via simulations. The simulation results indicated that the proposed algorithms are promising, and outperform the comparison baseline algorithms.

In our future work, we intend to establish an optimization framework for AoI-aware IoT query service provisioning in an MEC empowered by digital twin technology, which enables to accurately predict network dynamics and provide real-time system information such as user query pattern changes and dynamic resource utilization, and so on. An efficient prediction mechanism based on deep reinforcement learning will be developed that will help to pre-allocate network resources for service provisions and improve the quality of services.

REFERENCES

[1] M. Bastopcu and S. Ulukus. Age of information for updates with distortion: constant and age-dependent distortion constraints. *IEEE/ACM Transactions on Networking*, vol. 29, no. 6, pp. 2425 – 2438, 2021.

[2] L. Corneo, C. Rohner, and P. Gunningberg. Age of information-aware scheduling for timely and scalable internet of things applications. *Proc. of INFOCOM'19*, IEEE, pp. 2476 – 2484, 2019.

[3] Q. Chen, Z. Cai, L. Cheng, F. Wang, and H. Gao. Joint near-optimal age-based data transmission and energy replenishment scheduling at wireless-powered network edge. *Proc. of INFOCOM'22*, IEEE, pp. 770 – 779, 2022.

[4] X. Chen, L. Jiao, W. Li, and X. Fu. Efficient multi-user computation offloading for mobile-edge cloud computing. *IEEE/ACM Transactions on Networking*, vol. 24, no. 5, pp. 2795 – 2808, 2016.

[5] GT-ITM. http://www.cc.gatech.edu/projects/gtitm/, 2019.

[6] H. Gedawy, K. Habak, K. A. Harras, and M. Hamdi. RAMOS: a resource-aware multi-objective system for edge computing. *IEEE Transactions on Mobile Computing*, vol. 20, no. 8, pp. 2654 – 2670, 2021.

[7] A. Goldsmith. *Wireless communications*. Cambridge University Press, 2005.

[8] M. Goudarzi, H. Wu, M. Palaniswami, and R. Buyya. An application placement technique for concurrent IoT applications in edge and fog computing environments. *IEEE Transactions on Mobile Computing*, vol. 20, no. 4, pp. 1298 – 1311, 2021.

[9] A. Hameed, J. Violos, A. Leivadeas, N. Santi, R. Grünblatt, and N. Mitton. Toward QoS prediction based on temporal transformers for IoT Applications. *IEEE Transactions on Network and Service Management*, vol. 19, no. 4, pp. 4010 – 4027, 2022.

[10] C. Li, S. Li, Q. Liu, Y. T. Hou, W. Lou, and S. Kompella. Eywa: a general approach for scheduler design in AoI optimization. *Proc of INFOCOM'23*, IEEE, 2023.

[11] H. Li, J. Zhang, H. Zhao, Y. Ni, J. Xiong, and J. Wei. Joint optimization on trajectory, computation and communication resources in information freshness sensitive MEC system. *IEEE Transactions on Vehicular Technology*, vol. 73, no. 3, pp. 4162 – 4177, 2024.

[12] J. Li, S. Guo, W. Liang, J. Wang, Q. Chen, Z. Xu, and W. Xu. AoI-aware user service satisfaction enhancement in digital twin-empowered edge computing. *IEEE/ACM Transactions on Networking*, vol. 32, no. 2, pp. 1677 –-1690, 2024.

[13] J. Li, S. Guo, W. Liang, J. Wu, Q. Chen, Z. Xu, W. Xu, and J. Wang. Wait for fresh data? digital twin empowered IoT services in edge computing. *Proc of MASS'23*, IEEE, 2023.

[14] J. Li, S. Guo, W. Liang, Q. Chen, Z. Xu, and W. Xu. SFC-enabled reliable service provisioning in mobile edge computing via digital twins. *Proc of MASS'22*, IEEE, pp. 311 – 317, 2022.

[15] J. Li, S. Guo, W. Liang, Q. Chen, Z. Xu, W. Xu, and A. Y. Zomaya. Digital twin-assisted, SFC-enabled service provisioning in mobile edge computing. *IEEE Transactions on Mobile Computing*, vol. 23, no. 1, pp.393 – 408, 2024.

[16] J. Li, W. Liang, W. Xu, Z. Xu, X. Jia, A. Zomaya, and S. Guo. Budget-aware user satisfaction maximization on service provisioning in mobile edge computing. *IEEE Transactions on Mobile Computing*, vol. 22, no. 12, pp. 7057 – 7069, 2023.

[17] J. Li, W. Liang, W. Xu, Z. Xu, Y. Li, and X. Jia. Service home identification of multiple-source IoT applications in edge computing. *IEEE Transactions on Services Computing*, vol. 16, no. 2, pp. 1417 – 1430, 2023.

[18] J. Li, W. Liang, W. Xu, Z. Xu, X. Jia, W. Zhou, and J. Zhao. Maximizing user service satisfaction for delay-sensitive IoT applications in edge computing. *IEEE Transactions on Parallel and Distributed Systems*, vol. 33, no. 5, pp. 1199– 1212, 2022.

[19] J. Li, W. Liang, Y. Li, Z. Xu, X. Jia, and S. Guo. Throughput maximization of delay-aware DNN inference in edge computing by exploring DNN model partitioning and inference parallelism. *IEEE Transactions on Mobile Computing*, vol. 22, no. 5, pp. 3017 – 3030, 2023.

[20] J. Li, J. Wang, Q. Chen, Y. Li, and A. Zomaya. Digital twin-enabled service satisfaction enhancement in edge computing. *Proc of INFOCOM'23*, IEEE, 2023.

[21] X. Liang, W. Liang, Z. Xu, Y. Zhang, and X. Jia. Multiple service model refreshments in digital twin-empowered edge computing. *IEEE Transactions on Services Computing*, to be published, 2023, doi: 10.1109/TSC.2023.3341988.

[22] Q. Liu, H. Zeng, and M. Chen. Minimizing AoI with throughput requirements in multi-path network communication. *IEEE/ACM Transactions on Networking*, vol. 30, no. 3, pp. 1203 – 1216, 2022.

[23] X. Lin, J. Wu, J. Li, W. Yang, and M. Guizani. Stochastic digital-twin service demand with edge response: an incentive-based congestion control approach. *IEEE Transactions on Mobile Computing*, vol. 22, no. 4, pp. 2402 – 2416, 2023.

[24] Y. Lu, X. Huang, K. Zhang, S. Maharjan, and Y. Zhang. Communication-efficient federated learning and permissioned blockchain for digital twin edge networks. *IEEE Internet of Things Journal*, vol. 8, no. 4, pp. 2276 – 2288, 2021.

[25] Y. Ma, W. Liang, M. Huang, W. Xu, and S. Guo. Virtual network function service provisioning in MEC via trading off the usages between computing and communication resources. *IEEE Transactions on Cloud Computing*, vol. 10, no. 4, pp. 2949 – 2963, 2022.

[26] Y. Ma, W. Liang, J. Li, X. Jia, and S. Guo. Mobility-aware and delay-sensitive service provisioning in mobile edge-cloud networks. *IEEE Transactions on Mobile Computing*, vol. 21, no, 1, pp. 196 – 210, 2022.

[27] L. Ma, X. Wang, X. Wang, L. Wang, Y. Shi, and M. Huang. TCDA: truthful combinatorial double auctions for mobile edge computing in industrial internet of things. *IEEE Transactions on Mobile Computing*, vol. 21, no. 11, pp. 4125 – 4138, 2022.

[28] R. Minerva, G. M. Lee, and N. Crespi. Digital twin in the IoT context: a survey on technical features, scenarios, and architectural models. *Proceedings of the IEEE*, vol. 108, no. 10, pp. 1785 – 1824, 2020.

[29] R. M. Nauss. Solving the generalized assignment problem: an optimizing and heuristic approach. *INFORMS Journal of Computing*, vol. 15, no. 3, pp. 249 – 266, 2003.

[30] D. Shomys and E. Tardos. An approximation algorithm for the generalized assignment problem. *Mathematical Programming*, vol. 62, pp. 461 – 474, 1993.

[31] W. Sun, H. Zhang, R. Wang, and Y. Zhang. Reducing offloading latency for digital twin edge networks in 6G. *IEEE Transactions on Vehicular Technology*, vol. 69, no. 10, pp. 12240 – 12251, 2020.

[32] S. Tuli, S. Ilager, K. Ramamohanarao, and R. Buyya. Dynamic scheduling for stochastic edge-cloud computing environments using A3C learning and residual recurrent neural networks. *IEEE Transactions on Mobile Computing*, vol. 21, no. 3, pp. 940 – 954, 2022.

[33] M. Vaezi, K. Noroozi, T. D. Todd, D. Zhao, and G. Karakostas. Digital twin placement for minimum application request delay with data age targets. *IEEE Internet of Things Journal*, vol. 10, no. 13, pp. 11547 – 11557, 2023.

[34] C. Wang, Z. Cai, and Y. Li. Sustainable blockchain-based digital twin management architecture for IoT devices. *IEEE Internet of Things Journal*, vol. 10, no. 8, pp. 6535 – 6548, 2023.

[35] X. Wang, Z. Ning, S. Guo, M. Wen, and V. Poor. Minimizing the age-of-critical-information: an imitation learning-based scheduling approach under partial observations. *IEEE Transactions on Mobile Computing*, vol. 21, no. 9, pp. 3225 – 3238, 2022.

[36] D. Wu, X. Huang, X. Xie, X. Nie, L. Bao, and Z. Qin. LEDGE: leveraging edge computing for resilient access management of mobile IoT. *IEEE Transactions on Mobile Computing*, vol. 20, no. 3, pp. 1110 – 1125, 2021.

[37] Z. Xu, W. Ren, W. Liang, W. Xu, Q. Xia, P. Zhou, and M. Li. Schedule or wait: age-minimization for IoT big data processing in MEC via online learning. *Proc. of INFOCOM'22*, IEEE, pp. 1809 – 1818, 2022.

[38] Z. Xu, Z. Yuan, W. Liang, D. Liu, W. Xu, H. Dai, Q. Xia, and P. Zhou. Learning-driven algorithms for responsive AR offloading with non-deterministic rewards in Metaverse-enabled MEC. *IEEE/ACM Transactions on Networking*, vol. 32, no. 2, pp. 1556 –-1572, 2024.

[39] Z. Xu, L. Zhou, H. Dai, W. Liang, W. Zhou, P. Zhou, W. Xu, and G. Wu. Energy-aware collaborative service caching in a 5G-enabled MEC with uncertain payoffs. *IEEE Transactions on Communications*, vol. 70, no. 2, pp. 1058 – 1071, 2022.

[40] R. D. Yates, Y. Sun, D. R. Brown, S. K. Kaul, E. Modiano, and S. Ulukus. Age of information: an introduction and survey. *IEEE Journal on Selected Areas in Communications*, vol. 39, no. 5, pp. 1183 – 1210, 2021.

[41] D. Zeng, H. Geng, L. Gu, and Z. Li. Layered structure aware dependent microservice placement toward cost efficient edge clouds. *Proc of INFOCOM'23*, IEEE, 2023.

[42] R. Zhang, Z. Xie, D. Yu, W. Liang, and X. Chang. Digital twin-assisted federated learning service provisioning over mobile edge networks. *IEEE Transactions on Computers*, vol. 73, no. 2, pp. 586–598, 2024.

[43] S. Zhang, L. Wang, H. Luo, X. Ma, and S. Zhou. AoI-delay tradeoff in mobile edge caching with freshness-aware content refreshing. *IEEE Transactions on Wireless Communications*, vol. 20, no. 8, pp. 5329 – 5342, 2021.

[44] X. Zhou, I. Koprulu, A. Eryilmaz, and M. J. Neely. Efficient distributed MAC for dynamic demands: congestion and age based designs. *IEEE/ACM Transactions on Networking*, vol. 31, no. 1, pp. 74 – 87, 2023.
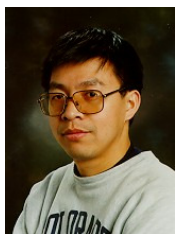
Jing Li received the PhD degree and the BSc degree with the first class Honours from The Australian National University in 2022 and 2018, respectively. He is currently a postdoctoral fellow at City University of Hong Kong. His research interests include edge computing, internet of things, digital twin, network function virtualization, and combinatorial optimization.

Song Guo (Fellow, IEEE) is a Full Professor in the Department of Computer Science and Engineering at the Hong Kong University of Science and Technology. He also holds a Changjiang Chair Professorship awarded by the Ministry of Education of China. His research interests are mainly in the areas of big data, edge AI, mobile computing, and distributed systems. With many impactful papers published in top venues in these areas, he has been recognized as a Highly Cited Researcher (Web of Science) and received over 12 Best Paper Awards from IEEE/ACM conferences, journals and technical committees. Prof. Guo is the Editor-in-Chief of IEEE Open Journal of the Computer Society. He has served on IEEE Communications Society Board of Governors, IEEE Computer Society Fellow Evaluation Committee, and editorial board of a number of prestigious international journals like IEEE Transactions on Parallel and Distributed Systems, IEEE Transactions on Cloud Computing, IEEE Internet of Things Journal, etc. He has also served as chair of organizing and technical committees of many international conferences. Prof. Guo is an IEEE Fellow and an ACM Distinguished Member.


Weifa Liang (Senior Member, IEEE) received the PhD degree from the Australian National University in 1998, the ME degree from the University of Science and Technology of China in 1989, and the BSc degree from Wuhan University, China in 1984, all in Computer Science. He is a Full Professor in the Department of Computer Science at City University of Hong Kong. Prior to joining City University of Hong Kong, he was a Full Professor in the Australian National University. His research interests include design and analysis of energy efficient routing protocols for wireless ad hoc and sensor networks, Mobile Edge Computing (MEC), Network Function Virtualization (NFV), Internet of Things and digital twins, design and analysis of parallel and distributed algorithms, approximation algorithms, and graph theory. He currently serves as an Editor of IEEE Transactions on Communications.

Jie Wu (Fellow, IEEE) received the Ph.D. degree in computer engineering from Florida Atlantic University, Boca Raton, FL, USA, in 1989. He is the Director of the Center for Networked Computing and Laura H. Carnell professor at Temple University. He also serves as the Director of International Affairs at College of Science and Technology. He served as Chair of Department of Computer and Information Sciences from the summer of 2009 to the summer of 2016 and Associate Vice Provost for International Affairs from the fall of 2015 to the summer of 2017. Prior to joining Temple University, he was a program director at the National Science Foundation and was a distinguished professor at Florida Atlantic University. His current research interests include mobile computing and wireless networks, routing protocols, cloud and green computing, network trust and security, and social network applications. He serves on several editorial boards, including IEEE Transactions on Mobile Computing, IEEE Transactions on Service Computing, Journal of Parallel and Distributed Computing, and Journal of Computer Science and Technology. Dr. Wu was general co-chair for IEEE MASS 2006, IEEE IPDPS 2008, IEEE ICDCS 2013, ACM MobiHoc 2014, ICPP 2016, and IEEE CNS 2016, as well as program co-chair for IEEE INFOCOM 2011 and CCF CNCC 2013. He was an IEEE Computer Society Distinguished Visitor, ACM Distinguished Speaker, and chair for the IEEE Technical Committee on Distributed Processing (TCDP). Dr. Wu is a Fellow of the AAAS and a Fellow of the IEEE. He is the recipient of the 2011 China Computer Federation (CCF) Overseas Outstanding Achievement Award.
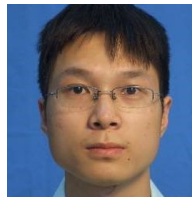
Quan Chen (Member, IEEE) received his BS, Master and PhD degrees in the School of Computer Science and Technology at Harbin Institute of Technology, China. He is currently an associate professor in the School of Computers at Guangdong University of Technology. He once worked as a postdoctoral research fellow in the Department of Computer Science at Georgia State University. His research interests include routing and scheduling algorithms in wireless networks and sensor networks.

Zichuan Xu (Member, IEEE) received his PhD degree from the Australian National University in 2016, ME degree and BSc degree from Dalian University of Technology in China in 2011 and 2008, all in Computer Science. From 2016 to 2017, he was a Research Associate at Department of Electronic and Electrical Engineering, University College London, UK. He is currently a full professor and PhD advisor in School of Software at Dalian University of Technology. His research interests include mobile edge computing, serverless computing, network function virtualization, algorithmic game theory, and optimization problems.

Wenzheng Xu (Member, IEEE) received the BSc, ME, and PhD degrees in computer science from Sun Yat-Sen University, Guangzhou, China, in 2008, 2010, and 2015, respectively. He currently is an associate professor at Sichuan University, China. Also, he was a visitor at both the Australian National University, Australia and the Chinese University of Hong Kong, Hong Kong. His research interests include wireless ad hoc and sensor networks, mobile computing, approximation algorithms, combinatorial optimization, online social networks, and graph theory.

Jianping Wang (Fellow, IEEE) received the B.S. and M.S. degrees in computer science from Nankai University, Tianjin, China, in 1996 and 1999, respectively, and the Ph.D. degree in computer science from the University of Texas at Dallas in 2003. She is currently a Professor with the Department of Computer Science, City University of Hong Kong. Her research interests include cloud computing, service oriented networking, edge computing, and network performance analysis.