

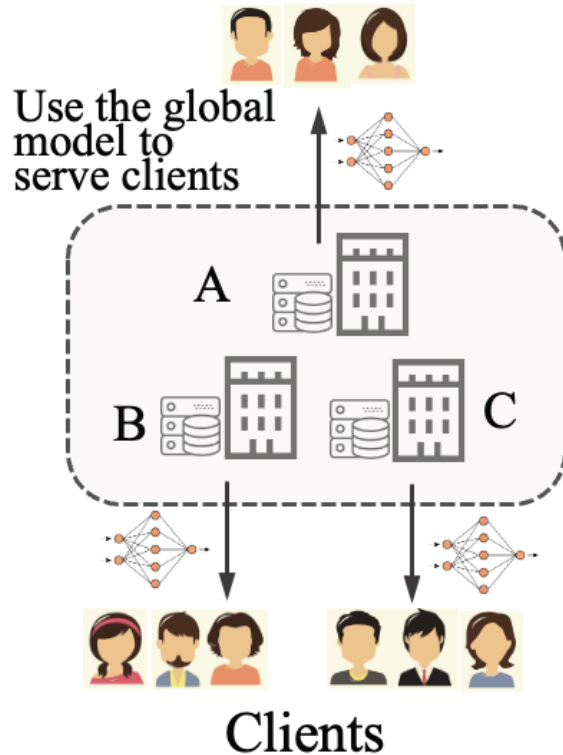
All Federated or Not: Optimizing Personal Model Performance in Cross-silo Federated Learning

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Outline

- Introduction
- Problem Formulation
- Personal Model Performance Improvement Estimation
- Design of Coalition Partition Algorithm
- Experimental Evaluation
- CONCLUSION

Background



In **cross-silo FL**, Organizations are participants performing local training. They own the global model and use it to serve their clients. Each organization cares most about its **personal model performance**.

the performance of the global model on its personal data distribution.

Motivations

One mode of Coalition

- {A,B} Distribution 1
- {C,D} Distribution 2

Organization	Local Accuracy	All Federated Accuracy	Coalition Accuracy
A	0.83	0.80 ↓	0.84 ↑
B	0.75	0.79 ↑	0.82 ↑
C	0.94	0.92 ↓	0.94 ↑
D	0.73	0.91 ↑	0.93 ↑

how to **arrange organizations into coalitions** to improve their **personal model performance**?

how to **arrange organizations into coalitions** to improve their **personal model performance**?

- Estimate **personal model performance improvement**



- Solve the coalition formation problem

Organizations' utility

social welfare

How to find a **stable** partition?

Personal Model Performance Improvement(utility):

The difference between the personal model performance obtained by **joining coalition C** and by training the model **alone** for an organization *i*.

Real value can only be known after FL is done!

Nash stable partition

No player **has an incentive** to change its coalition because it cannot get a higher utility

Individually stable partition

No player **can** change its coalition to coalition C for a higher utility with the agreement of all members of C

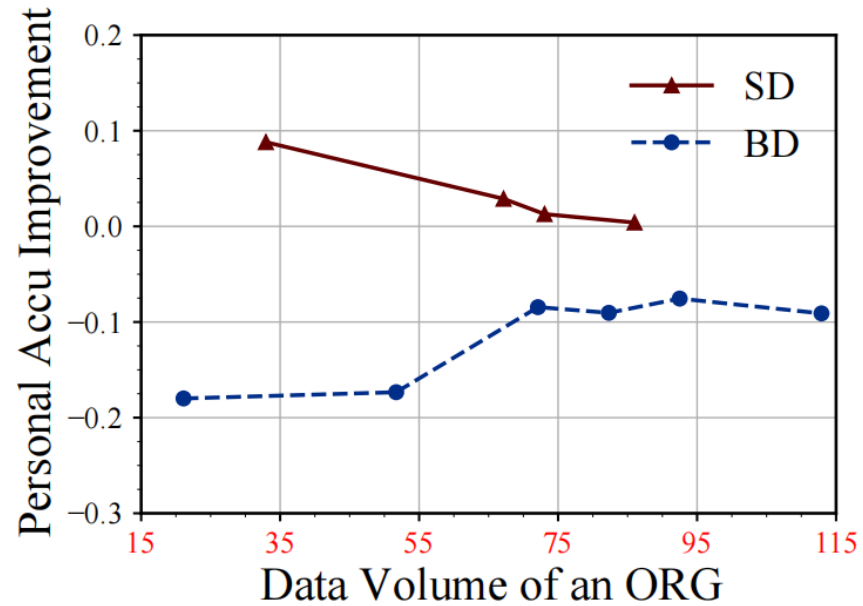
Critical Factors Influencing Utility

Experiment settings

Dataset: MNIST

BD: Bigger data Difference

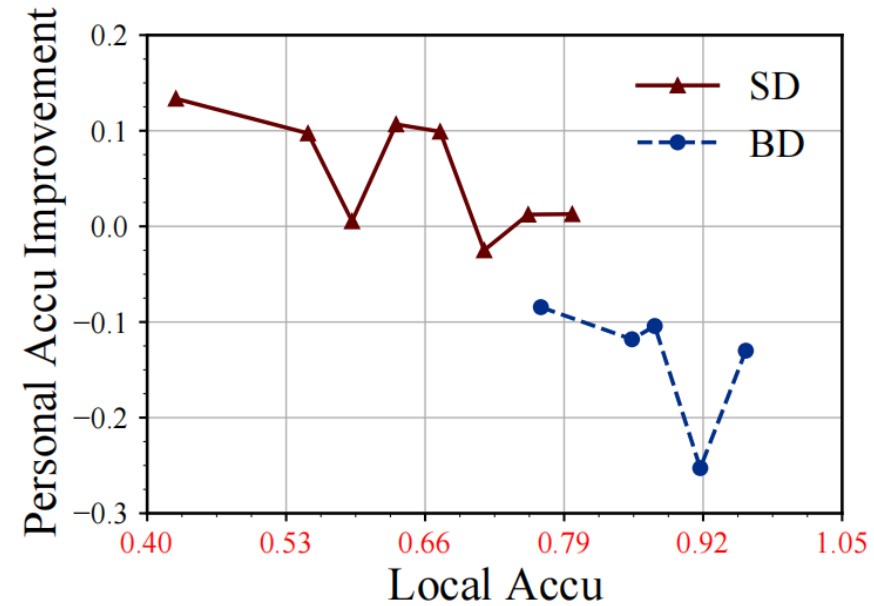
SD : Smaller Difference



Factors about organization i:

training data volume,

local model performance



Critical Factors Influencing Utility

Experiment settings

Dataset: MNIST

BD: Bigger data Difference

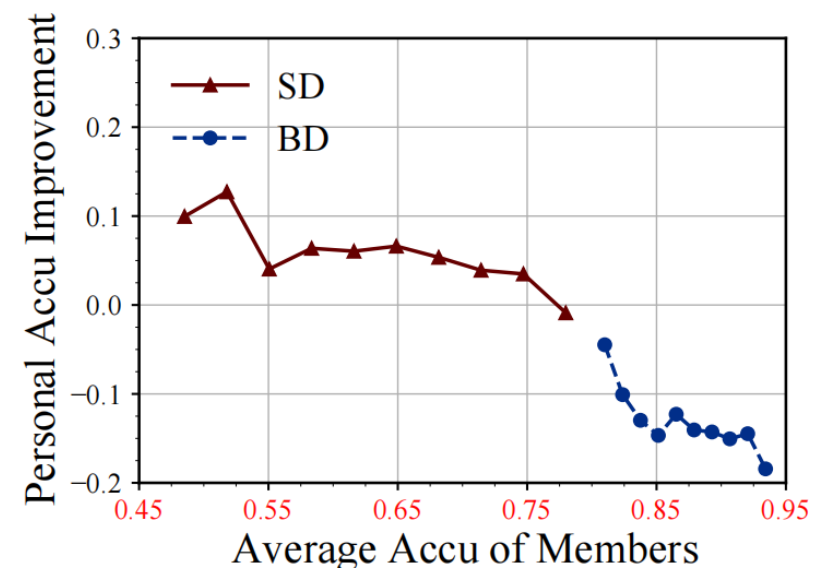
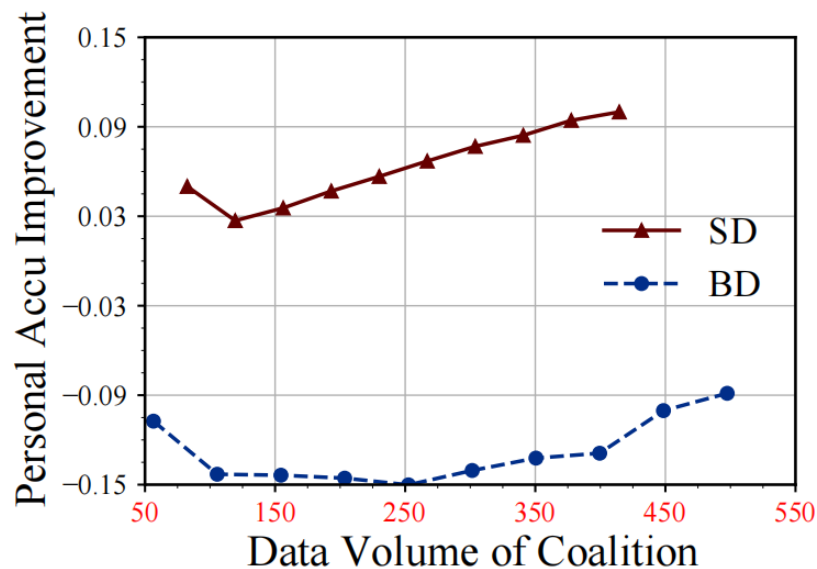
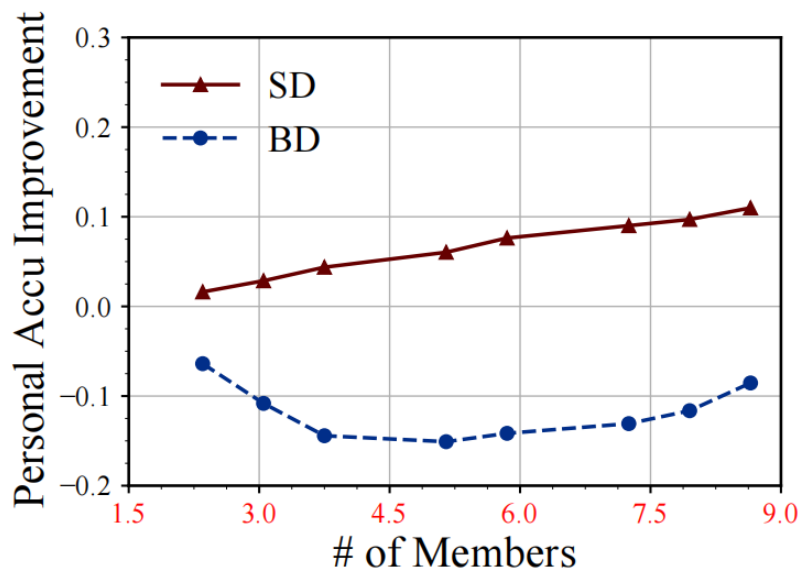
SD : Smaller Difference

Factors about coalition C:

the number of members of C,

the total data volume of C,

the average local accuracy of all members of C



Critical Factors Influencing Utility

Experiment settings

Dataset: MNIST

BD: Bigger data Difference

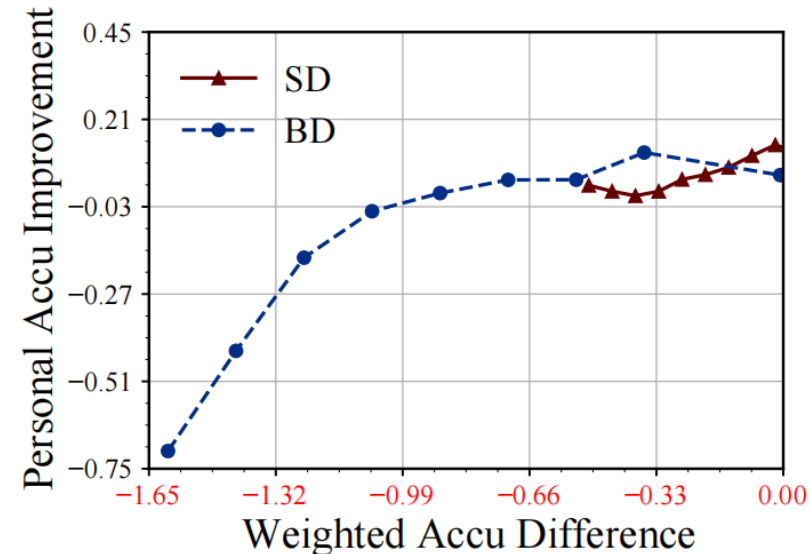
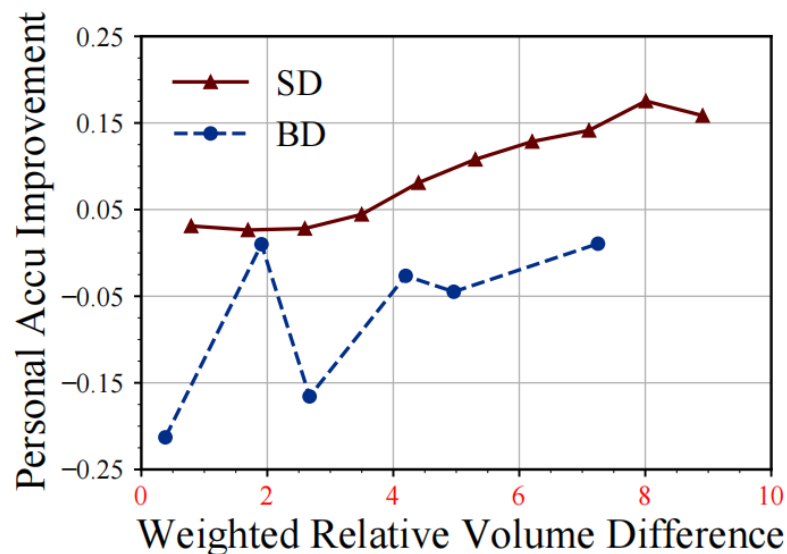
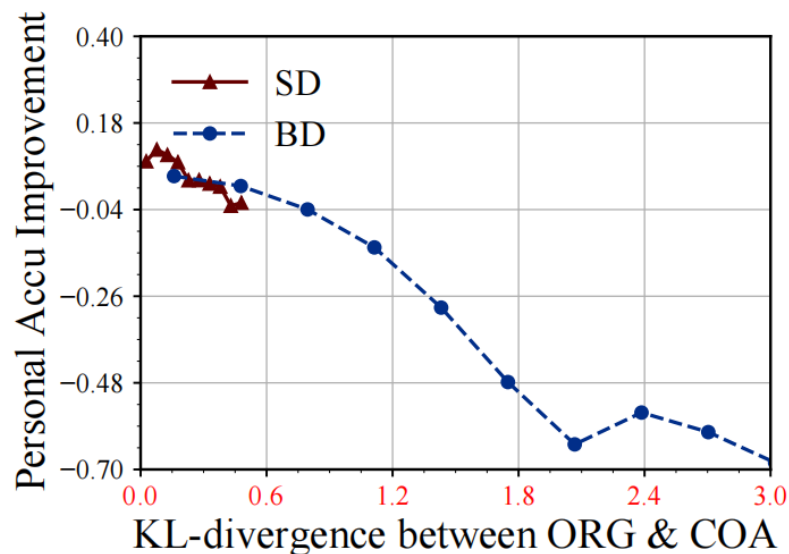
SD : Smaller Difference

Factors about difference between organization i and coalition C :

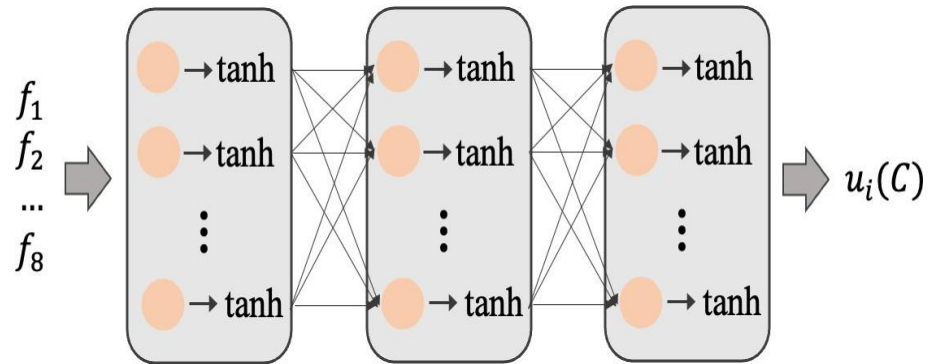
KL-divergence,

the weighted relative volume difference,

the weighted accuracy difference



Utility Fitting by Neutral Networks



Input: 8 critical factors $\{f_1, \dots, f_8\}$ we have selected.

Output: Estimated utility for organization i by joining coalition C .

Finding Individually Stable Partition

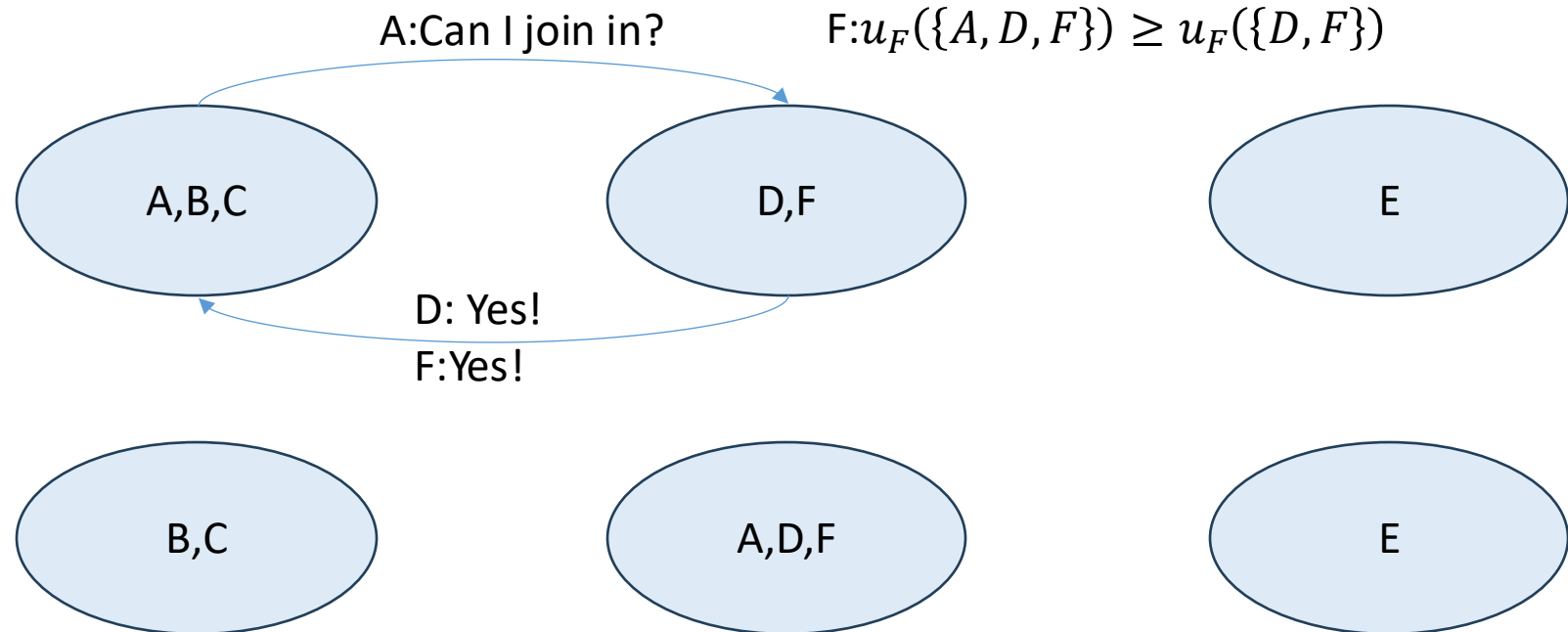
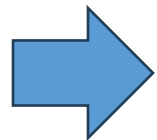
it is A's turn

A find its estimated utility

$$u_A(\{A, D, F\}) > u_A(\{A, B, C\})$$

$$D: u_D(\{A, D, F\}) \geq u_D(\{D, F\})$$

$$F: u_F(\{A, D, F\}) \geq u_F(\{D, F\})$$

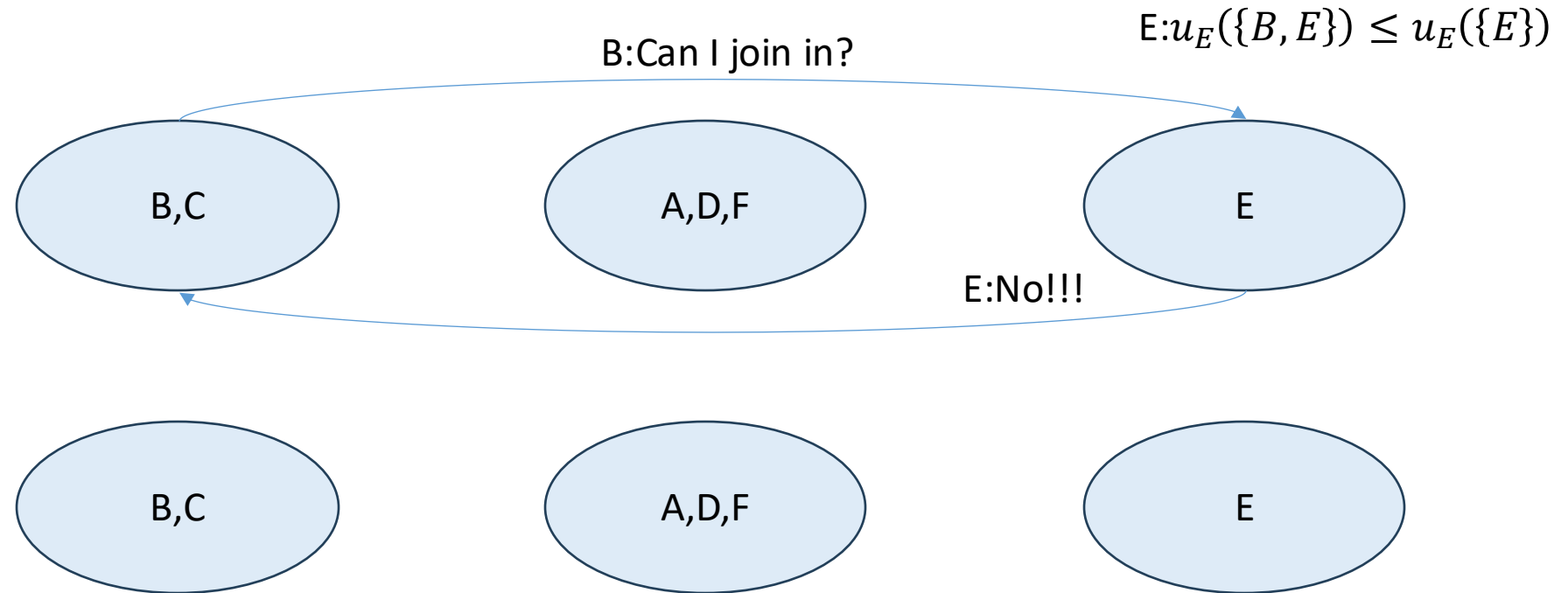


Finding Individually Stable Partition

it is B's turn

B find its estimated utility

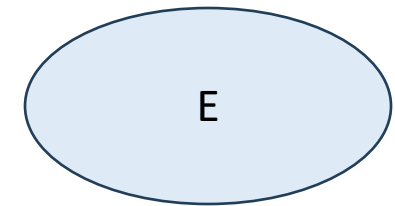
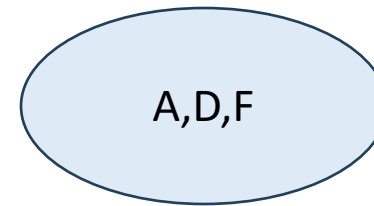
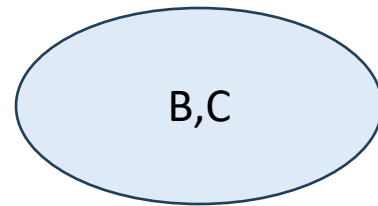
$$u_B(\{B, E\}) > u_B(\{B, C\})$$



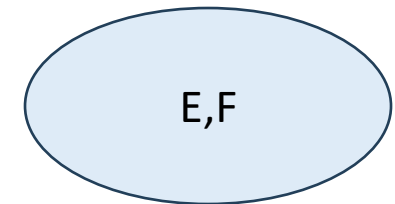
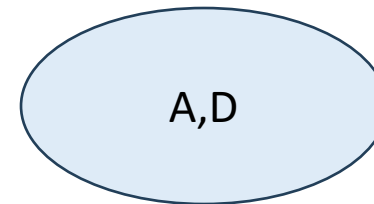
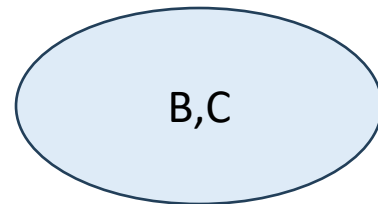
Finding Individually Stable Partition

it is C's turn
C find its estimated utility is max
when it remains still

C: Current is perfect!



.... After D,E,F made their choices in turns as well , **One round** has been completed, and the current partition is:



Now it's A's turn again.

A finds it wants to join {E,F}, and {E,F} agree.

So a new round begin, and the process above is **repeated until in one round no one moves.**

When finding Nash Stable Partition

Finding Nash Stable Partition

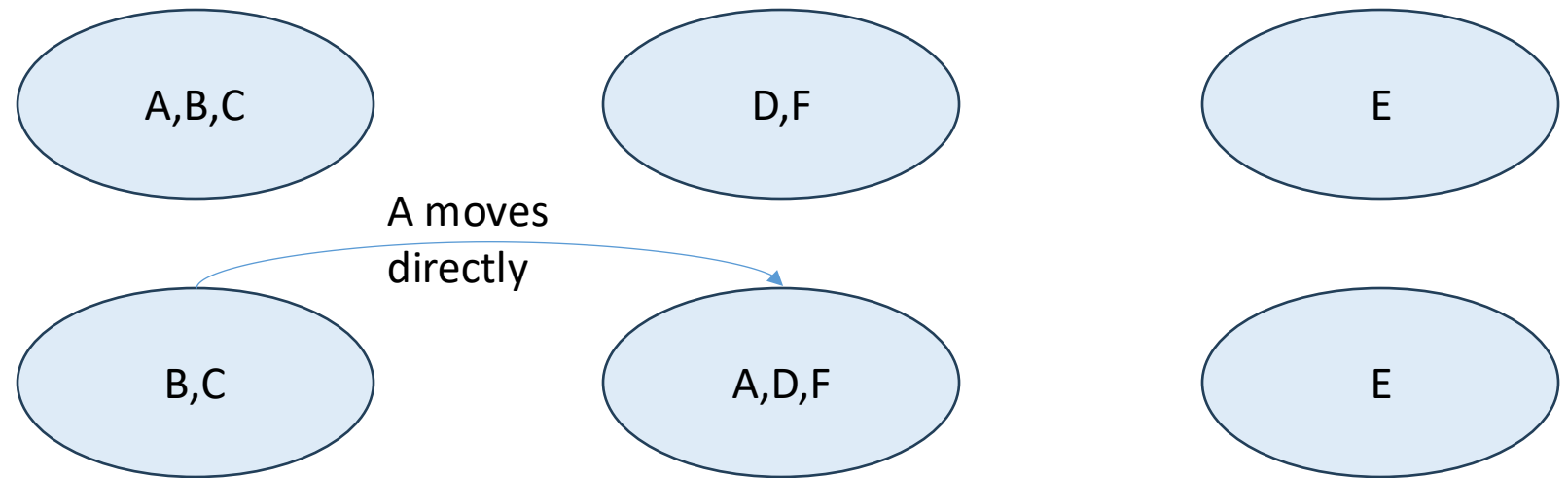
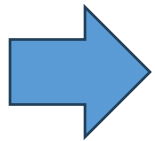
When finding Nash Stable Partition, An organization A joining a coalition **does not need to obtain the agreement** of other organizations in this coalition.

If members of the coalition find that they have a better choice after joining an organization, they can also move directly to the ideal coalition in its turn.

it is A's turn

A find its estimated utility

$$u_A(\{A, D, F\}) > u_A(\{A, B, C\})$$



It is a little difficult to find a **Nash Stable Partition** than find a **Individually Stable Partition**.

Improve Social Welfare of Stable Partitions



If there are multiple stable solutions which one is the **optimal**?
How to maximize the **social welfare**?



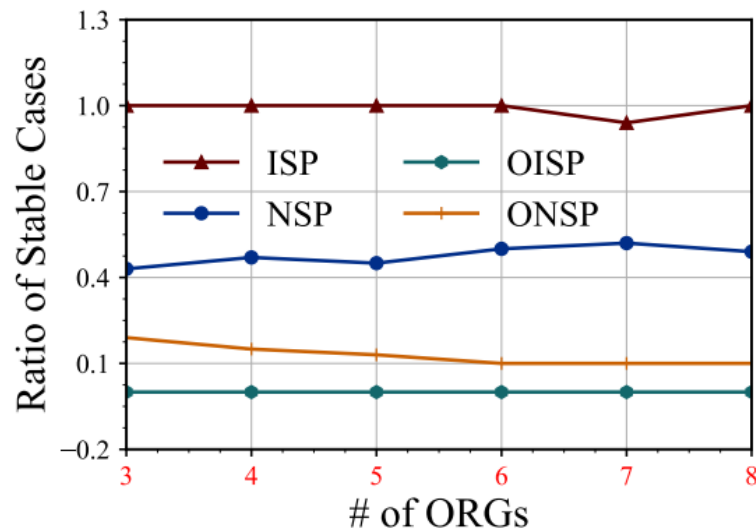
set the **initial coalition structure** as the optimal structure



We find the optimal partition with the highest social welfare based on dynamic programming.

The convergence performance

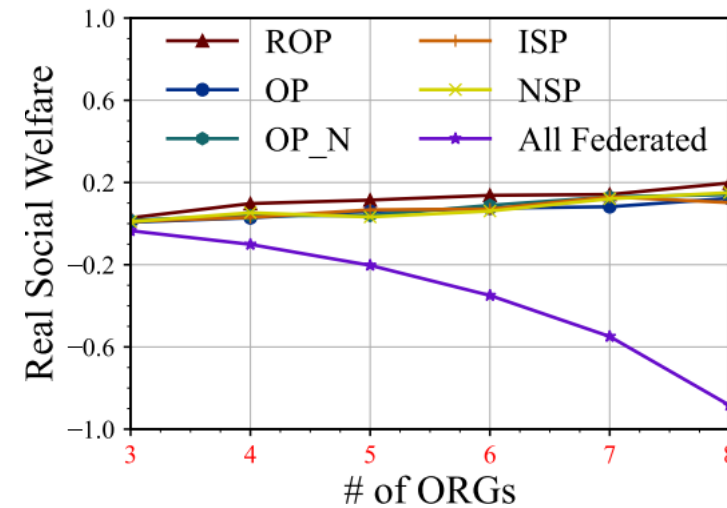
- **ISP** : Individually Stable Partitions
- **NSP**: Nash Stable Partitions
- **ONSP**: Other Nash Stable Partitions
- **OISP**: Other Individually Stable Partitions



It is better to pursue ISP as there exists one and only one ISP in most cases.

Social satisfaction

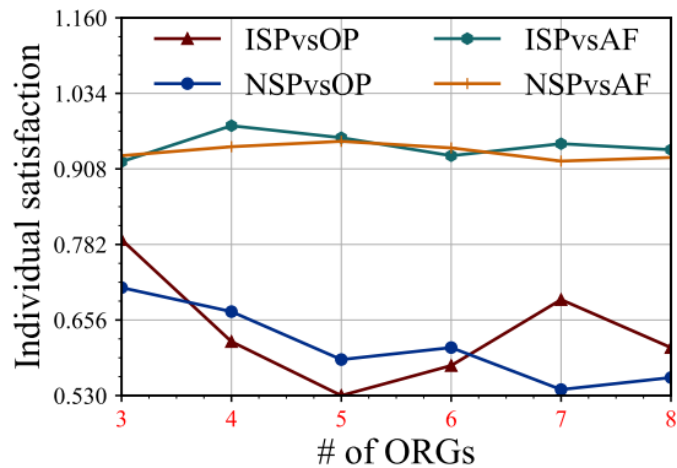
- **OP**: the Optimal Partitions found by us
- **OP_N**: the average social welfare of OPs when Nash stable partitions exist
- **ROP** :the Optimal Partition found according to [the Real individual utilities](#)
- **All Federated** :all organizations form one coalition



The social welfares of OP and ISP are close to ROP

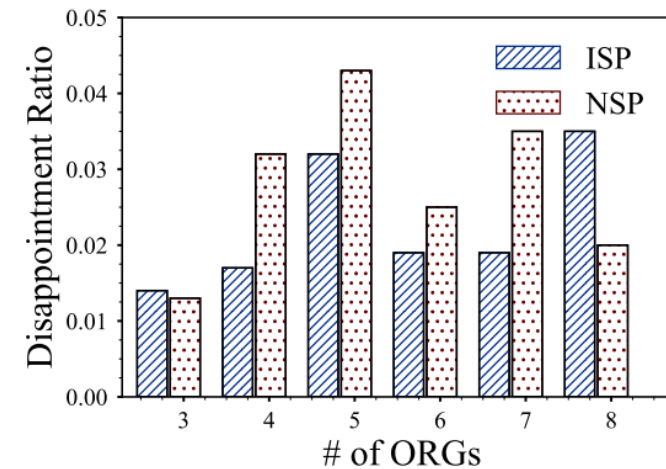
Individual satisfaction

Individual satisfaction of partition Π_1 vs Π_2 is defined as the ratio of the number of the organizations whose utility in partition Π_1 is more than its utility in partition Π_2 to the total number of the organizations.



ISP and NSP found by our algorithms are better than both OP and AF (All Federated together)

If an organization is told that it can get a positive utility as long as it follows the stable solution, **but it gets a negative utility** after FL is done, the organization would **be disappointed**.



The ratio of disappointed organizations is less than 5%.

- We solve a coalition formation problem in cross-silo federated learning to optimize the personal model performance for each organization.
- We first make use of previous FL results to train a neural network which estimates the utility function of each organization for the next time of FL.
- Based on the estimation results, we help organizations form stable coalitions by a distributed algorithm. The found stable coalition structure is close to the optimal one.
- The solution performs well with respect to both real social welfare and individual satisfaction.

Thank you!