User Requirements-aware Security Ranking in SSL Protocol

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Abstract The primary goal of the secure socket layer protocol (SSL) is to provide confidentiality and data integrity between two communicating entities. Since the most computationally expensive step in the SSL handshake protocol is the server's RSA decryption, it is introduced that the proposed secret exchange algorithm can be used to speed up the SSL session initialization. This paper first points out that the previous batch method is impractical since it requires multiple certificates, then it proposes a unique certificate scheme to overcome the problem. The optimization strategy, which is based on the constrained model considering the user requirements-aware security ranking, focuses on the optimal result in different public key sizes. It is also introduced that the parameter is optimized when integrating user requirements for Internet QoS, such as the stability of the system and the tolerable response time. Finally, the proposed algorithm is evaluated to be practical and efficient through both analysis and simulation studies.

Keywords Quality of Service (QoS) · SSL handshake · optimization strategy · security ranking

1 INTRODUCTION

The secure socket layer protocol (SSL) protects communications by encrypting messages with a secret key negotiated in the SSL handshake protocol [1]. How

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to offer some Quality of Service (QoS) that may be satisfied with Web users has become a new issue.

Web-based applications rely on the HTTPS protocol to guarantee security and privacy in transactions ranging from e-banking, e-commerce, and e-procurement to those that deal with sensitive data, such as career and identity information [2]. The SSL protocol allows the server and the client to authenticate each other and to negotiate an encryption algorithm and cryptographic keys before transmitting and receiving the first byte of data [3]. However, such a protocol needs intensive computational resources due to the cost of public-key operations [4].

In the Web context, one of the main factors is the direct consequence of expensive Public Key operations performed by servers as part of each SSL handshake. Since most SSL-enabled servers use RSA, the burden of performing many costly decryption operations can be very detrimental to the server performance.

For example, a typical Pentium server (running Linux and Apache) can handle about 322 HTTP connections per second at full capacity, but only 24 SSL connections per second; and a Sun 450 (running Solaris and Apache) fell from 500 to 3 connections per second [5]. To improve the performance of the SSL handshake protocol, there are several ways:

- 1. Hardware: Obviously, a specific circuit can improve the performance. This solution may not be a good solution to small or medium-sized servers [6].
- 2. Session Caching: The cache allows subsequent connections to resume an earlier TLS session, and thus, to reuse the result of an earlier computation. Research has suggested that, indeed, session caching helps to improve the web server performance[1]. However, the cache technology has no help to speed up the session setup.
- 3. Software: Many algorithmic approaches for speeding up SSL's performance on a web server are presented in literatures [7]-[13]. It is designed for heavily-loaded web servers handling many concurrent SSL sessions. However, these schemes ignore the satisfactory of the user requirements for QoS, such as the stability of the system and the tolerable response time.

Being aware of the computational imbalance between clients and server in the SSL handshake protocol, we proposed a secret exchange algorithm to overcome the problem. The starting point of the proposed scheme is a technique due to the batch RSA decryption [14] [15]. This paper adapts the certificate mechanism so as to provide the SSL setup with a unique certificate issued by the Certificate Authority (CA). This paper also proposes the constrained model integrating the user-perceived quality into secure web server design [16][17]. This paper also optimizes the batch size by the constrained model, which meets the user requirements-aware security ranking focusing on the optimal result in different public key sizes. In addition, the proposed scheme uses the approximate analytical solution of the mean response time to optimize the batch size of the server. It is designed for heavily-loaded web servers handling many concurrent SSL sessions. Notice that a preliminary version of this paper appeared in the paper [18].

The rest of the paper is organized as follows: Section II describes the secret exchange algorithm in the SSL handshake protocol. The proposed constrained model of the QoS-aware optimization strategy is presented in Section III. The QoS-aware optimization algorithm is presented in Section IV. Section V validates the proposed solutions through both analysis and simulation studies, and Section VI concludes the paper.

2 SECRET EXCHANGE ALGORITHM IN THE SSL HANDSHAKE PROTOCOL

The proposed scheme in this paper focuses on the parameter optimization-based technology, which is a software-only approach for speeding up SSL's performance on a web server. The starting-point of the proposed scheme is a technique due to using the batch RSA decryption. Being aware of the computational imbalance between clients and server in the SSL handshake protocol, we proposed algorithms to overcome the problem.

The following Algorithm 1 and Algorithm 2 are secret exchange algorithms of the SSL handshake at the server side and the client side, respectively. When using small public exponent e_1 and e_2 , it is possible to decrypt two cipher texts for approximately the price of one [14]. This technology facilitates more favorable load distribution by requiring the clients to perform more work (as part of encryption) and the server to perform commensurately less work, thus resulting in better SSL throughput at the server.

In the standard SSL protocol, each client encrypts a 48-byte pre-master secret as the encryption exponents, and the server decrypts the cipher text independently so as to get the *Pre-master secret*. Algorithm 1 obtains the *Pre-master secret* from multiple clients and hence, improves the performance significantly.

The parameter b is the size of multi-clients for aggregate decryption. The public key is made of two integers $\langle N, e \rangle$. The value e is called the encryption exponent. Given b distinct and pairwise relatively prime public keys e_1, \ldots, e_b , all sharing a common modulus N = pq. N is product of two large primes p and q. The security parameter n is the bit length of the public modulus N and k the bit length of the bigger of e_i at Steps 1-5 of Algorithm 1. Furthermore, we have b encrypted messages v_1, \ldots, v_b and further results v'_1, \ldots, v'_b , one encrypted with each key at Steps 3-8 of Algorithm 2. e'_i is defined as each client's brother's exponent. After we perform Step 10 of Algorithm 1, we call Algorithm 2 and receive the message including cipher text v_1, \ldots, v_b and v'_1, \ldots, v'_b from each client. At Step 19 of Algorithm 1, quantities subscripted by L or R refer to the corresponding value of the left or right child of the node, respectively.

At Steps 16-21 of Algorithm 1, we seek to combine the individual encrypted messages v_i to form, at the root of the batch tree, the value $v=\prod_{i=1}^b v_i^{e/e_i}$, where $e=\prod_{i=1}^b e_i$. At Steps 16-20, the first b/2 values of currentnode.ciphertext are computed by v_1',\ldots,v_b' because the left child and the

Algorithm 1 Secret exchange algorithm at the server side

```
1: Given b distinct and pairwise relatively prime public keys e_1, \ldots, e_b
 2: //all sharing a common modulus N = pq, relatively prime to \phi(N) = (p-1)(q-1).
 3: //n is the bit length of the public modulus N and k the bit length of the bigger of e_i.
 4: Construct a full binary tree T_d which is called the decryption tree with leaves labeled
 5: e_1, \ldots, e_h;
 6: Input: e_1, .
 7: Output: a full binary tree T_d, m_i 1 \le i \le b
 8: Construct a message including e_i and the information e'_i about brother's exponent for
 9: each client, where 1 \le i \le b;
10: call Algorithm 2; upon receiving the message including cipher text v_i and v_i' from each
11: client, where 1 \le i \le b;
12: //Compute two middle values such as exponent and ciphertext at each
13: //internal nodes of T_d repeating this computation recursively. The number of external
14: //nodes is equal to b-1. The computation phase is to generate the product
15: //v = \prod_{i=1}^{b} v_i^{e/e_i} \mod N, where e = \prod_{i=1}^{b} e_i.
16: \mathbf{for}(j = 1 \text{ to } b - 1)\mathbf{do}\{
     E_L \leftarrow leftchild.exponent; E_R \leftarrow rightchild.exponent; Currentnode.exponent \leftarrow E_L \times E_R; L \leftarrow leftchild.ciphertext; R \leftarrow rightchild.ciphertext;
18:
19: If (j \leq (b/2)) Current
node.exponent \leftarrow v'_{2j-1} \times v'_{2j}
       else Currentnode.ciphertext\leftarrow L^{E_R} \times R^{\tilde{E_L}};
       v \leftarrow \text{rootnode.ciphertext}; e \leftarrow \text{rootnode.exponent};
       //The value of v and e is simply the result associated with the root
23: Compute m \leftarrow v^{1/e} \mod N = \prod_{i=1}^b v_i^{1/e_i} \mod N; e \leftarrow \prod_{i=1}^b e_i 24: //m is the ciphertext of root node of T\_d. e is the exponent of root node of T\_d.
25: //The next step is to break up the product m to obtain the plaintexts m_i = v_i^{1/e_i} with
26: //repeating this computation recursively from the root node.
27: for(i = 1 \text{ to } b - 1) do{}
28:
        Compute X while ((X = 0 \mod E_L) \text{ and } (X = 1 \mod E_R) = = \text{true});
          X_L \leftarrow X/E_L; X_R \leftarrow (X-1)/E_R; \\ m_R \leftarrow m^X/(v_L^{X_L} \cdot v_R^{X_R}); m_L \leftarrow m/m_R; \}
29:
30:
         // The values of v_L and v_R are simply the results associated with the ciphertext of
31:
32:
         // node which have stored at Step 16
33: return m_i; 1 \le i \le b
```

right child of current node are leaves. The number of external nodes is equal to b-1.

Using the binary tree construction, working from the leaves to the root. At every internal node, each encrypted message v_i is placed (as v) in the leaf node labeled with its corresponding e_i . The root node v's value is percolated up the tree using the following recursive step, applied at each inner node at Steps 16-21 of Algorithm 1. E_L, E_R are the left child and the right child of each product of internal node at Step 17 of Algorithm 1.

The root node contains $v = \prod_{i=1}^b v_i^{e/e_i}$ at Step 21 of Algorithm 1. The eth root of this v is extracted. We store $v^{1/e} = \prod_{i=1}^b v_i^{1/e_i}$ as m in the root node at Step 23 of Algorithm 1. The Steps 27-34 are to break up the product m to obtain the plaintexts $m_i = v_i^{1/e_i}$ with repeating this computation recursively from the root node.

Algorithm 2 Secret exchange algorithm at the client side

```
1: Input: e_i, e'_i

2: Output: v'_i, v_i

3: Create plaintext m_i(0 < m_i < N);

4: //upon receiving the message including e_i;

5: Compute v_i = m^{e_i}_i \mod N \ 1 \le i \le b.

6: //upon receiving the message including e'_i which is the brother's exponent value of e_i;

7: Compute v'_i = v^{e'_i}_i \mod N;

8: Construct message including v'_i, v_i for server.

9: return
```

3 UNIQUE CERTIFICATE SCHEME IN THE SSL HANDSHAKE PROTOCOL

Our unique certificate method is to reuse the message *ServerHello* in the protocol. For simplicity, we only show the related processes and the modified information in the standard SSL handshake protocol (see Fig.1.).

The following procedure is the unique certificate scheme for the SSL handshake protocol: (1) Clients send a client hello massage that includes the cipherspects to the server and create random nonce r_c respectively. (2) Server responds with a server hello massage that includes server's public-key certificate and a random nonce r_s . In this improvement, e_i and e'_i are actually a part of ServerHello.random. Server only needs to send unique certificate to all the clients. (3) The clients choose a secret random 48-byte Pre-master secret m_1 and m_2 by inputting values m_1 , m_2 , r_c , r_s into hash function f(). It then encrypts m_i with e_i , which is different from server's public-key, and attaches the cipher text to a Client key exchange message that is sent to the server. (4) The Server decrypts the Pre-master secret m_1 and m_2 simultaneously using Algorithm 1, and uses it to compute the Sharedmastersecret s_1 and s_2 respectively. The client will verify the certificate as usual, but encrypt the Pre-master secret with received e_i , instead of the public exponent in the certificate. Therefore, no extra charge is required, and it is easy to manage the certificate. On the other hand, since the certificate is used to prove the owner who knows the factors of the RSA modules N only, this adaptation does not undermine the security strength of the SSL protocol.

4 CONSTRAINED MODEL OF QOS-AWARE OPTIMIZATION STRATEGY

The optimization strategy which is based on the constrained model considering the user requirements-aware security ranking focuses on the optimal result in different public key sizes.

Lemma 1 Algorithm 1 can generate the b decryption results in $O(\log_2 b(\sum_{i=1}^b \log_2 e_i) + \log_2 N)$ modular multiplications and O(b) modular divisions

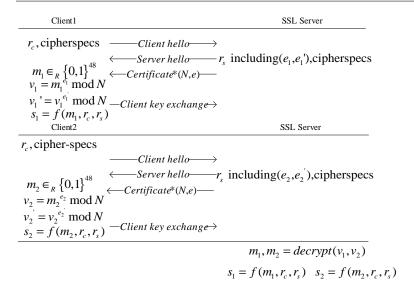


Fig. 1 Unique Certificate Scheme for a partial handshake

Proof According to Step 23 of Algorithm 1, $m \leftarrow v^{1/e} = \prod_{i=1}^b v_i^{1/e_i} \mod N$, with $e = \prod_{i=1}^b e_i$, the algorithm can get the result in $O(\log_2 N)$ modular multiplications, which is equivalent to one RSA decryption.

Using the full binary tree as a guide, working from the leaves to the root, for constructing the serial number for every exponent of the leaves, the binary length of the serial number is equal to $\lfloor \log_2 b \rfloor$. In other words, the depth of the leaves is equal to $\lfloor \log_2 b \rfloor$.

According to Step 27 of Algorithm 1, the algorithm takes the recursive result from left child and right child, and the result associated with this node is $m_R \leftarrow m^X/(v_L^{X_L} \cdot v_R^{X_R})$. The computation phase is to break up the product m to obtain the plaintexts $m_i = v_i^{1/e_i}$, which we wish to decrypt simultaneously.

Note that v_l and v_r have already been computed and stored, as the left and right branch values of the root, during the tree based computation of m at Steps 12-22 of Algorithm 1. By definition, X is the unique solution (($X = 0 \mod E_L$) and ($X = 1 \mod E_R$) == true). Note that $\log_2 X < \log_2 e$ and $X_L \leftarrow X/E_L$; $X_R \leftarrow (X-1)/E_R$, we can get $\log_2 X_L + \log_2 X_R < \log_2 X < \log_2 e$ with $e = \prod_{i=1}^b e_i[14]$.

Because the depth of the leaves is equal to $\lfloor \log_2 b \rfloor$, for every plaintext result $m_i = v_i^{1/e_i}$, every node contributes at most $\lfloor \log_2 b \rfloor$ bits to the appropriate exponents in the computation of m^X , $v_L^{X_L}$ and $v_R^{X_R}$ recursive result. Because the binary length of exponent e_i is $\lceil \log_2 e_i \rceil$, Steps 25-33 of Algo-

Because the binary length of exponent e_i is $\lceil \log_2 e_i \rceil$, Steps 25-33 of Algorithm 1 can generate the following b results in $O(\log_2 b(\sum_{i=1}^b \log_2 e_i))$ modular multiplications or $O(\log_2 b \log_2 e)$ modular multiplications with $e = \prod_{i=1}^b e_i$. To solve for $m_R \leftarrow m^X/(v_L^{X_L} \cdot v_R^{X_R})$, we divide $v_L^{X_L} \cdot v_R^{X_R}$ by m^X , the number of modular divisions required is O(b).

At all, Algorithm 1 can generate the b results $m_1^{1/e_1}(modN), \ m_2^{1/e_2}(modN), \ldots, \ m_b^{1/e_b}(modN)$

in $O(\log_2 b(\sum_{i=1}^b \log_2 e_i) + \log_2 N)$ modular multiplications and O(b) modular divisions.

Then, Lemma 1 is proved.

Theorem 1 Choosing the batch size b, which satisfied $2 \le b \le \frac{n}{(\log_2 n)^2}$, and choosing the e_i exponents to be polynomial in n we get $O((\log_2 n)^2 + n)$ modular multiplications and $O(\frac{n}{(\log_2 n)^2})$ modular divisions. n is defined as the binary length of modules N.

Proof We can easily get $\lfloor \log_2 N = n \rfloor$, where n is defined as the binary length of modules N.

We can easily get $\frac{n}{(\log_2 n)^2} < n$, because n is a positive number and n > 2. Also because the function $\log_2 x$ increases with x, we can get $\log_2 \frac{n}{(\log_2 n)^2} < \log_2 n$. Because of choosing the batch size b which satisfies $2 \le b \le \frac{n}{(\log_2 n)^2}$, we can derive $\log_2 b \le \log_2 \frac{n}{(\log_2 n)^2}$ and $\log_2 b(\sum_{i=1}^b \log_2 e_i) + \log_2 N \le \log_2 \frac{n}{(\log_2 n)^2} (\sum_{i=1}^b \log_2 e_i + \log_2 N)$.

Due to Lemma 1, where $\sum_{i=1}^{b} \log_2 e_i = \log_2 e$ and $\log_2 N = n$, it can be described as

 $O(\log_2 \frac{n}{(\log_2 n)^2} (\sum_{i=1}^b \log_2 e_i + \log_2 N)) < O(\log_2 e(\log_2 n) + n).$

By choosing the e_i exponents to be polynomial in n,

Thus, e < n, the following equation is derived as

 $O(\log_2 e(\log_2 n) + n) < O((\log_2 n)^2 + n)$

Then, Theorem 1 is proved.

Constrained model considering the user requirements-aware security ranking is proposed based on Theorem 1. We optimize the batch size b for a specific modulus size, and obtain better results for smaller batches if the modulus is relatively small. According to Theorem 1, the batch size is optimized as $\log_2 \frac{n}{(\log_2 n)^2}$ in this constrained model.

5 QOS-AWARE OPTIMIZATION ALGORITHM

Let the decryption time of Algorithm 1 in the SSL handshake time be T_b .

The performance analysis of Algorithm 1 can be divided as multiplication at Steps 16-20, exponentiation at Steps 21-24 and division computation phases at Steps 27-33.

We can estimate the cost of $e = \prod_{i=1}^{b} e_i$ is $(b-1)n^2$. The cost of computing 1/e is $(b-1)n^2$. The main computation cost is exponentiation costs $(3k-2)n^2 + o(n^2)$ with the exponent e_i where the bit length of e_i is k. The whole cost in the multiplication phase is $b((3k/2) + 3) + o(n^2)$.

In the exponentiation computation phase, the Steps 21-24 costs $3n^3 + n^2 + o(n^2)$.

In the division phase, the Step 31 mainly includes one exponentiation cost $b(3bk-2)n^2+o(n^2)$ and two exponentiations cost $(3(b-1)k-2)n^2+o(n^2)$. The Step 31 also includes one inversion of n-bit integers. Inversion of n-bit integers is equivalent to 20 modular multiplications. The cost of modular multiplication of two n-bit integers can be estimated as $2n^2+2n$ [15][18].

The whole cost in Algorithm 1 is estimated as $3n^3+n^2(44b+3b^3-1)+o(n^2)$. As a result, the decryption time of Algorithm 1 T_b is estimated as:

$$\left(\frac{3n^3 + n^2(44b + 3b^3 - 1)}{b(3n^3 + n^2)}\right)bT_{rsa} = \left(\frac{3n + (44b + 3b^3k - 1)}{b(3n + 1)}\right)bT_{rsa}$$
(1)

Since T_b is the majority of the service time, the batching service time of the server τ is T_b roughly.

Lemma 2 To satisfy the client's requirement for the stability of the system, the decryption time in SSL handshake T_b is less than the batch size multiplied by the mean Poisson distributed arrival time interval when the time in the Batch Queue Model M/D/1, thus:

$$\tau \approx T_b < b/\lambda \tag{2}$$

Proof Let X_i ($i = 1, 2, \ldots$) be the arrival time interval of two consecutive requests, and Y be the time interval of b consecutive requests. Batch Queue Model M/D/1 has been described in our previous work [18].

If the system achieves the stability when the time $t \to \infty$ for the M/D/1 queue model, $T_b < E(Y)$, where E(Y) is the expected value of Y. Because X_i is a random variable with independent identical distribution, the average arrival time interval of b consecutive requests is:

$$E(Y) = E(\sum_{i=1}^{b} X_i) = bE(X_i) = b/\lambda$$
 (3)

Then, Lemma 2 is proved.

Lemma 3 In the Batch Queue Model M/D/1, to satisfy the client's requirement for the stability of the system, thus, $T_q < b/2\lambda$.

Proof In the Batch Queue Model M/D/1, the value of T_q is derived following the equation:

$$T_{q} = \left(\frac{1 - e^{-\lambda \tau}}{1 - e^{-\lambda \tau} + e^{-1.5\lambda \tau}}\right) T_{r} = \left(\frac{e^{\lambda \tau} - 1}{e^{-\lambda \tau} - 1 + e^{-0.5\lambda \tau}}\right) T_{r} = \left(\frac{1}{1 + \frac{1}{(e^{\lambda \tau} - 1)e^{0.5\lambda \tau}}}\right) T_{r}$$
(4)

Where $T_r = 0.5\tau$, due to Lemma 2, it can be easily described as

$$T_q = \left(\frac{0.5\tau}{1 + \frac{1}{(e^{\lambda\tau} - 1)e^{0.5\lambda\tau}}}\right) < \left(\frac{1}{1 + \frac{1}{(e^b - 1)e^{0.5b}}}\right) \left(\frac{b}{2\lambda}\right)$$
 (5)

It can be easily described as when $b \leq 2$,

$$0.944 \approx 1 + \frac{1}{(e^2 - 1)e^{0.5*2}} \le 1 + \frac{1}{(e^b - 1)e^{0.5b}} < 1$$
 (6)

Then, the value bound of the upper limit of T_q is estimated as $[0.944b/2\lambda, b/2\lambda]$. Then, Lemma 3 is proved.

Tolerable response time (TRT) is defined as the delay time a client can tolerate between a request for a secure web page and receiving the page [16]-[19]. The real response time (RRT) is the interval between the receipt of the end of transmission of an SSL-based inquiry message and the beginning of the transmission of a response message to the station originating the SSL handshake.

Theorem 2 In the Batch Queue Model M/D/1, to satisfy the client's requirement for tolerable response time, RRT < TRT, thus, $\Rightarrow b < 0.4(\lambda \times TRT + 1)$

Proof The mean real response time (RRT) is denoted as the sum of T_q , T_c and the T_b .

In the Batch Queue Model M/D/1, the value bound of the upper limit of T_q is estimated as $b/2\lambda$ derived from Lemma 3 (refer to Eq. 6).

The value bound of the upper limit of T_b is estimated as b/λ derived from Lemma 2 (refer to Eq. 2).

 T_c is the mean time for waiting other client in the same batching which is easily derived that the max value of T_c is $(b-1/\lambda)$.

On the other hand, it is supposed that the solution of b should satisfy the approximate bound, which is derived from Lemma 2, Lemma 3 and described as the following equation:

$$RRT = T_q + T_c + T_b < \frac{b}{2\lambda} + \frac{(b-1)}{\lambda} + \frac{b}{\lambda} < TRT \Rightarrow b < 0.4(\lambda \times TRT + 1)$$
 (7)

Then theorem 2 is proved.

Combining the user requirements for QoS such as security ranking, the stability of the system and tolerable response time, these strategies aim to optimize the parameter b, which means the size of multi-clients for aggregate decryption in Algorithm 1. QoS-aware optimization algorithm satisfies these strategies in this paper.

According to Theorem 2, the initial value of b is estimated at Step 4 of Algorithm 3 with TRT and λ as input values. According to Theorem 1, b is estimated at Step 5 with PKS as input value. If the condition of optimal batch can not be satisfied, the algorithm has the ability to fall back on conventional_RSA_decryption() which means the decryption with plain RSA, which is described at Step 9 and Step 18. The computation of T_b is performed using Eq. 1 at Step 12. Step 11 sorts b to satisfy max solution of $T_b < b/\lambda$ according

Algorithm 3 QoS-aware optimization algorithm

```
1: Input: \lambda, TRT, PKS
 2: Output: Optimal_b, T_b, T_b_real, Speedup, Speedup_real
 3: // Compute the initial value of b
 4: initial_b \leftarrow \int (0.4(\lambda \times TRT + 1)); (refer to Eq. 7)
 5: n \leftarrow PKS; estimate\_b \leftarrow \lfloor \frac{n}{(\log_2 n)^2} \rfloor
 6: if (estimate\_b < initial\_b)
 7: then\{initial\_b \leftarrow estimate\_b; Successfind \leftarrow false;\}
 8: if (initial\_b \le 1)
 9: then{do conventional_RSA_decryption(); return;}
10: b \leftarrow initial\_b;
11: while (b! = 1) do{
      T_b = \left(\frac{3n + (44b + 3b^3k - 1)}{b(3n + 1)}\right)bT_{rsa} (refer to Eq. 1)
12:
13:
         if (T_b \leq b/\lambda)
14:
         then\{Optimal\_b \leftarrow b; Successfind \leftarrow true; break; \}
15:
         elseif(T_b > b/\lambda)
         then b \leftarrow b - 1; }
17: if (initial_{-}b <= 1)
18: then {do conventional_RSA_decryption(); return; }
19: call Algorithm1; Compute T_b_real
20: Speedup \leftarrow \frac{b(3n+1)}{3n+(44b+3b^3k-1)}; (refer to Eq. 1)
21: Speedup\_real \leftarrow bT_{rsa}/T_b\_real;
22: return;
```

to Lemma 2 in the descending order from the upper limit computing at Step 7 to two. The computation of T_b -real is performed by executing the Algorithm 1

6 VALIDATION OF ANALYTICAL MODELS AND PERFORMANCE EVALUATION STUDY

6.1 Validation of analytical models

The analytical results and simulation results are executed on a machine with a Dell Intel Pentium IV processor clocked at 3.20GHz and 1GB RAM. Specifically, this paper performs the simulation of the SSL handshake secret exchange algorithm with very small public exponents, namely, e=3,5,7,11,13,17, etc. It is assumed that the value (TRT) is equal to 1 second and 8 seconds as examples both in the analytical model and simulation. It is assumed that the values of the public key sizes (PKS) are equal to 512, 1024 and 2048 bits length as examples both in the analytical model and simulation.

Table 1 validates the result of *Optimal_b*, described by the constrained model of QoS-aware optimization strategy. It is assumed that TRT is equal to 1s in the analytical model and simulation. Due to small arrival rates, b is almost uniformly calculated by our analytical model (Table 1). Since arrival rates are small (i.e., $\lambda < 2$), there is very little opportunity to batch, and therefore, the solution of b is relatively small (Table 1). Even at a higher arrival

Table 1 Optimal batch size in constrained model validation

λ/PKS	$ig Optimal_b$							
	analytical model			simulation results				
	512	1024	2048	512	1024	2048		
1	-	_	_	-	_	_		
2	2	2	2	2	2	2		
3	2	2	2	2	2	2		
4	3	3	3	3	3	3		
5	4	4	4	4	4	4		
10	8	8	6	8	8	6		
20	8	10	6	8	10	6		
30	8	10	6	8	10	6		
40	8	10	-	8	10	-		
50	8	10	-	8	10	-		
60	8	6	-	8	6	-		
70	8	6	-	8	6	-		
80	8	6	-	8	6	-		
90	6	5	-	6	5	-		
100	6	5	-	6	5	-		

rate, the analytical result and simulation result are very close. The solution of the optimal batch size is increased with λ , both in the analytical model and simulation when $\lambda < 30$ (i.e., PKS=1024bits), approximately. Otherwise, the RRT is not increased, obviously. The solution of b is decreased with λ when $\lambda > 60$ (i.e., PKS=1024bits) approximately. The solution of b can not satisfy the user requirements for the stability of the system, in other words, the solution of b can not satisfy $T_b \leq b/\lambda$ according to Lemma 3 when $\lambda > 37.5$, approximately (i.e., PKS=2048bits).

But, with a non-batching system, it becomes unstable when $\lambda > 1/T_{rsa} = 1/0.16 = 6.25$ for 2048 bits keys due to the fact that a non-batching system becomes unstable when $\lambda > \tau$.

6.2 Performance evaluation

The simulation result of the RSA decryption time T_{rsa} with a larger public exponent, namely e=65537 is about 16 ms, 32ms and 130ms with public modulus N that is 512 bits in length, 1024 bits in length, and 2048 bits in length respectively, which is tested using reiterative results.

The multi-factor RSA [12] can expect the theoretical speed up of around 2.25 with n=pqr and 3.38 for $n=p^2q$. Experiments show the real speed up to be around 1.73 and 2.3, respectively. Rebalanced RSA offers theoretical speed up of 3.6, but the actual speedup is 3.2 for 1024 bits keys. Specifically, d is chosen to be close to n such that both $d \mod (p-1)$ and $d \mod (q-1)$ are small integers [12]. The resulting public exponent e also becomes close to n, which is much larger than typical values (i.e., e=3,17, or 65537). It is in fact so large that Microsoft Internet Explorer (IE) cannot accept it; SB (Shacham

Table 2 Speed up of decryption time validation

b/PKS	Speedup of decryption time								
	Speedup			$Speedup_real$					
	512	1024	2048	512	1024	2048			
2	1.81	1.90	1.95	1.78	1.83	1.90			
4	3.68	3.05	3.42	3.21	2.93	3.39			
6	2.10	2.80	3.82	2.01	2.76	3.80			
8	1.28	2.18	3.47	1.14	2.09	3.39			

and Boneh) scheme [10] offers a speed up factor of 2.5 for 1024bits keys. The downside is obvious because CAs charge per certificate regardless of whether the certificate is for the same site or not. It also ignores the satisfaction of the user requirements for QoS, where the batch size is equal to four.

Our algorithm offers the speedup factor of 2.76 (Table 2) for a 1024 bits key which is used in the SSL handshake protocol frequently. Typically, b is equal to 6 for optimal performance when $60 < \lambda < 80$ approximately (Table 1). Obviously, our scheme not only achieves a better speedup factor, but overcomes these disadvantages of the previous schemes. All the methods are backward compatible with standard RSA. Also, all speedup methods discussed are based on 1024-bit RSA and is relative to the cost of performing plain RSA decryptions.

It is assumed that TRT is equal to 8 seconds in Figure 2. These figures show that RRT is almost linear when λ is relatively small. This is due to the fact that $RRT = T_q + T_c + T_b$ (refer to Eq. 7). When λ is relatively small, the main contribution to RRT is made by T_c (i.e., $\lambda = 10$, PKS=1024bits). It is evident that the time T_c is increased linearly with b. T_b is also increased with b. Therefore, RRT is also increased with b when λ is relatively large (i.e., $\lambda = 80$, PKS=1024bits).

Figure 3 illustrates the analytical mean response time RRT, our simulation results and that of the SB (Shacham and Boneh) scheme (i.e. TRT=1PKS=1024bits). When λ is approximately equal to 30, RRT reaches Maximum which is equal to 828ms approximately, whereas the value is less than 1 second and decreased with λ when using optimal batch size b (see Fig.3). In the SB scheme, RRT behaves poorly especially when λ does not exceed 10 requests/sec (see Fig.3). When λ is larger than 10 and less than 100 approximately, the performance of our scheme and the SB scheme are all satisfied with the clients' requirement of tolerable response time. However, it is showen that the solutions of b (Table 1) are larger than four. That means the optimal scheme can submit more decryption requests once to decryption device than the SB scheme. The analytical and simulation results of RRT showed our scheme behaves nicely.

A non-batching system becomes unstable when $\lambda > 1/T_{rsa} = 1/0.032 = 31.25$ for 1024bits keys. When the non-batching system is stable, the mean response time T' can be estimated as Eq. 8 [18]. The mean service time τ'

is deterministic in the non-batching in the M/D/1 queue model. Since T_{rsa} is the majority of the service time, the mean service time τ' of the server is roughly T_{rsa} .

$$T' = \tau' + \tau'(\frac{\tau'\lambda}{2(1 - \tau'\lambda)} \approx T_{rsa} + T_{rsa}(\frac{T_{rsa}\lambda}{2(1 - T_{rsa}\lambda)}))$$
(8)

Fig. 4 (TRT=8) illustrates the comparison of the mean response time of our scheme with non-batching. The vertical axis in each graph is the mean response time over the batch size divided by the mean response time with non-batching. The optimal batch size in our scheme is equal to 10 when $\lambda=30$. The speedup of the mean response time is an optimal one that equals to 6.69 approximately. The optimal batch size in our scheme is equal to 2 when $\lambda=2$. The speed up of the mean response time is an optimal one that equals to 1.94 approximately. It is clear that with the optimal batch size, our scheme has significant advantages and while costing less.

7 CONCLUSION

In conclusion, this paper proposes the secret exchange algorithm in the SSL handshake protocol. This paper also proposes a method of assigning the set of public exponents e_i only using the unique certificate in the SSL handshake protocol. Combining the user requirements for Quality of Service (QoS) such as security ranking, the stability of the system, and the tolerable response time, these strategies aim to optimize the parameter b, which is the size of multiclients for aggregate decryption. The parameter optimization-based SSL handshake is a viable option for secure communications. Currently, we mainly investigated this work based on the Internet with a high speed client/server computing paradigm. This paper also proposes the optimization strategy, which is based on the constrained model considering the user requirements-aware security ranking. Other optimization strategies are based on the constrained model considering the users' requirements for the stability of the system and the the client's requirement for the tolerable time. These optimal strategies focus on the optimal result in different public key sizes. Combining the users' requirements for Quality of Service (QoS), there are many factors which should be considered in the real Web application development. The evaluation criterion of Web service's performance is not only restricted to the response time and the throughput when the server handles SSL requests. In our future work, we consider establishing more evaluation criterion of Web service's performance and propose optimal strategies combing more users' requirements for Quality of Service.

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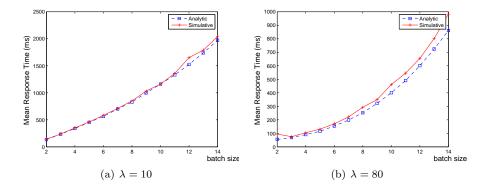
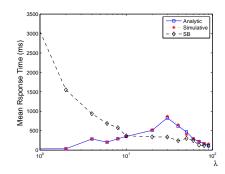
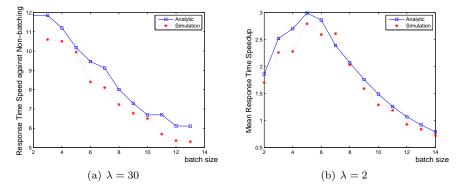


Fig. 2 Mean response time validation over batch size.



 ${\bf Fig.~3~~Mean~response~time~validation~over~client's~tolerable~response~time}$



 ${\bf Fig.~4}~{\rm Mean~Response~Time~Speed~Against~Non-batching~Scheme}.$

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