# Geometric Robot Mapping 

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#### Abstract

The purpose of this paper is to present a technique to create a global map of a robot's surrounding by converting the raw data acquired from a scanning sensor to a compact map composed of just a few generalized polylines (polygonal curves). To merge a new scan with a previously computed map of the surrounding we use an approach that is composed of a local geometric process of merging similar line segments (termed Discrete Segment Evolution) of map and scan with a global statistical control process. The merging process is applied to a dataset gained from a real robot to show its ability to incrementally build a map showing the environment the robot has traveled through.


Keywords: Robot Mapping, Polygon Merging, Polygon Simplification, Perceptual Grouping

## 1 Introduction

Imagine a scenario where a robot explores an unknown terrain. The goal is to acquire in real time a global overview map integrating all measurements collected by the robot. Here we deal with measurements obtained by 2D range sensors, called scans, that represent partial top views of the robots environment. Building a global overview map from scans is a typical scenario for rescue robots, where the overview knowledge, in the form of a global map, is particularly important to localize victims in catastrophe scenarios (e.g., in collapsed buildings) and to ensure that the whole target region has been searched [4]. Since odometry information under such conditions is very unreliable, we assume that it is not available. Also landmarks are ambiguous.

The whole process from reception of raw scanning data to the final map refers to the problem of simultaneous localization and mapping (SLAM) in robotics. The proposed approach addresses two main problems in SLAM stated in [10].

1. The measurement errors are statistically dependent, since errors in control accumulate over time, and they affect the way future sensor measurements are interpreted.
2. The second complicating aspect of the robot mapping problem arises from the high dimensionality of the entities that are being mapped, which leads to serious runtime and storage problems.

We address the problem of measurement errors being statistically dependent with a new process of map merging that is based on geometric local process of line segment merging with a global statistical control.

The second problem arises from the fact that in most mapping approaches the objects of which maps are built are simply points. These are either directly scan reflection points or point landmarks, e.g., [2] and [10]. In some approaches simple geometric features, especially line segments $[7,9,1]$ are used. However, the maps are still composed of a huge numbers of them, since these approaches do not provide any mechanisms to incrementally reduce the number of building blocks, which can be line segments of simply points. Consequently, the obtained maps are composed of thousands or even millions of points or line segments. An example of such a map is shown in Fig. 1(a). It is composed of 144400 points and obtained by alignment of 400 scans. It is then clear that such maps lead to serious runtime and storage problems, e.g., it is impossible to map larger environments and to perform loop closing in real time. In our map representation, we simply do not run into the second problem. Our representation is built of higher level objects, which are line segments and generalized polylines, and we have an explicit process, called Discrete Segment Evolution, that reduces the number of line segments to a minimal number required to represent the mapped environment. An example map obtained by our approach is shown in Fig. 1(b). This map was obtained from the same scan data as the map in (a), and it is composed of only about 50 line segments (which amounts to about 100 endpoints). Videos illustrating our incremental mapping results can be viewed on http://knight.cis.temple.edu/~shape/robot/.

A nice probabilistic framework to construct a global map from scan data is presented in [8]. However, this framework is based on the assumption that the uncertainty of scan points' positions is known. Due to the dependence of laser scan measurements on surface characteristics of scanned objects, e.g., glass-like surface, brick wall, and metal surface, this assumption is not satisfied in our example of rescue robots. We approach the problem of constructing a global map using the principles of perceptual grouping, which look for geometric structures in the data without any assumptions about the error characteristics [6].

## 2 Robot Mapping

In this section we introduce some notation regarding the system used by a robot to create its global map of its surroundings, and we summarize the main steps performed at each iteration of the algorithm, i.e., on the arrival of a new scan. The output is a global map that represents a top view of the environment using a small number of polylines. Fig. 1(b) illustrates such a map. For comparison, a global map obtained by alignment only is shown in Fig. 1(a).


Fig. 1. (a) A global map obtained by alignment of 400 scans is composed of 144400 points. (b) A global map obtained by the proposed map merging algorithm is composed of about 50 line segments ( 100 endpoints). Both maps are obtained from the same laser range data set showing a hallway at the Univ. of Bremen.

The proposed algorithm merges the newest laser range scan $S_{t}$ at time $t$ with a global map $G_{t-1}$ built from previous scans 0 to $t-1$. The global map is produced incrementally, which means that at every time $t$ we have a ready to use and a very simple global map of the environment. This is very important for all navigation and mapping tasks. Both global map $G_{t}$ and scan $S_{t}$ are composed of generalized polylines.

A generalized polyline is a set of line segments, having a specific ordering, whose vertices may or may not be connected. Observe that a classical definition of a polyline (polygonal curve) requires that the endpoints of consecutive segments coincide. Generalized polylines result naturally when scan points are approximated with line segments, which is our first processing step of the input range data. By dropping the constraint that a polyline be composed of line segments whose vertices are connected, we do not introduce additional noise that would result from connecting these vertices. The usage of generalized polylines is particularly important in the polyline merging and shape similarity algorithms described below.

Our first processing step (approximation of scan points with line segments) is followed by the segment grouping step. We form an ordered list of segments by minimizing the sum of the distances of their endpoints. Finally, if the endpoints of consecutive segments are too far apart, we split the list into sublists. Thus, generalized polylines are sublists of this list.

To create a global map $G$, we start with the first global map $G_{1}$ being equal to the first scan $S_{1}$. Henceforth, assuming we have created the global map $G_{t-1}$
at time $t-1$ and a new scan $S_{t}$ has arrived, $G_{t}$ is created in the following three steps:
Correspondence: We use a very simple and common approach to establish correspondence between global map $G_{t-1}$ and a new scan $S_{t}$. We position the new scan $S_{t}$ at the pose of the previous scan $S_{t-1}$ that has been aligned to the previous global map $G_{t-2}$ (in the process of construction of the actual global map $G_{t-1}$ ). The pose is the position and rotation angle in the coordinates of the global map. Then the correspondence is establish by mapping each segment endpoint of $S_{t}$ to a closest point in $G_{t-1}$ and the same with roles of $S_{t}$ and $G_{t-1}$ interchanged.

This process of correspondence computation works fine if there is continuity in the robot pose, i.e., robot pose changes only slightly from scan to scan. If the continuity assumption is not satisfied, we use shape similarity to establish the correspondence [5] and [11]. However, this approach is outside the scope of this paper.
Alignment: The current scan $S_{t}$ is rotated and translated until a minimum distance is found between the corresponding points. Then the closest points are found again, and the whole process is repeated until it stabilized. This algorithm to align scan $S_{t}$ and map $G_{t-1}$ is called Iterative Closest Point (ICP), and is described in [3].
Merging: This is the main contribution of this paper and its detailed discussion follows in Section 2.1. The output of alignment overlays the actual scan on the global map, but the surfaces of the same objects are still represented by separate polylines. The goal of merging is to represent surfaces of the same objects by single polylines.

### 2.1 Merging

Merging is the task of combining similar segments taken from two aligned maps to form new segments in a joint map. The similarity between pairs of segments is modeled following principles of perceptual grouping. In the case of incremental building of a global map, the task of merging is to combine similar line segments of the new scan, $S_{t}$, and the previous global map, $G_{t-1}$, to form new segments that define a new and current global map $G_{t}$. We assume that $S_{t}$ has been aligned to $G_{t-1}$. Merging consists of two steps, which integrate the new information contained in $S_{t}$ with the previous global map to produce $G_{t}$. The two steps are restrictive pairing and simplification.
Restrictive Pairing: The result of pairing can intuitively be understood as visual average of $S_{t}$ and $G_{t-1}$. Since our goal is to combine the information from both maps, we allow only pairing of segments from different maps. Therefore, we define two classes of line segments, class $C_{1}$ is a list consisting of segments from $G_{t-1}$ and class $C_{2}$ is a list consisting of segments of $S_{t}$.

Although the final task of merging is to decrease the number of line segments by combination, the pairing step goes into the opposite direction: it might create many new segments, which will be simplified in the second step called simplification. Pairing can be compared to a pencil drawing technique known as sketching,
e.g., used for cartoon drawings: to find the final outline of an object, it is first approximated by a larger number of light strokes, giving the eye the opportunity to imagine and select the correct position.

The process creates all possible pairs of line segments that are sufficiently similar, taking one segment from $C_{1}$ and one from $C_{2}$. Pairing of two segments from the same class is not allowed.

The similarity of line segments $L_{1}$ and $L_{2}$ is measured with the cost function $C\left(L_{1}, L_{2}, a d\right)$ (defined below), where $a d$ is an angular direction given by global statistics (defined below). If $C\left(L_{1}, L_{2}, a d\right)$ is below a given threshold, we create a new line segment $m s\left(L_{1}, L_{2}, a d\right)$ (defined below) that is visually close to $L_{1}$ and $L_{2}$. Figure 2 shows an example of restricted pairing. The newly created segments must follow the main directions, i.e., they are only allowed to have angles of $0^{\circ},+60^{\circ},-60^{\circ}$ with the $x$ axis.

A single line segment $L_{1}$ can create many children line segments $m s\left(L_{1}, L_{2}^{i}, a d\right)$ by pairing with segments $L_{2}^{i}$ for $i=1, \ldots, n$. We need to allow a single segment to pair with more than one segment from the other class, since we do not know the exact segment correspondence. It might be that the correct shape feature is created by the pairing with a second partner. However, to limit the computational complexity, each line segment is allowed to create only a small number of segments (at most 3 children segments are allowed in our implementation).

We remove all line segments from $C_{1}$ and $C_{2}$ that were parents of at least one new segment. We denote the resulting lists by $C_{1}^{\prime}$ and $C_{2}^{\prime}$. We denote with $A_{t}$ a list of all resulting children together with $C_{1}^{\prime}$ and $C_{2}^{\prime}$. Formally, the output of restricted pairing is defined as ( $T_{p}$ is a pairing cost threshold):

$$
A_{t}=C_{1}^{\prime} \cup C_{2}^{\prime} \cup\left\{m s\left(L_{1}, L_{2}, a d\right): C\left(L_{1}, L_{2}, a d\right)<T_{p}, L_{1} \in C_{1}, L_{2} \in C_{2}\right\}
$$



Fig. 2. The figure (b) is obtained from (a) by the proposed pair creation process. The index pairs in (b) refer to parent segments in (a). (c) shows the final result obtained by simplification of (b). The newly created segments in (b) and (c) must follow the main directions of $0^{\circ},+60^{\circ},-60^{\circ}$ with the $x$ axis.

Restrictive pairing may create some small artifacts in addition to features present in the reality, such as parallel segments in Fig. 2(b). The artifacts may
be introduced, since we do not know the exact correspondence of line segments, and therefore, must allow a single line segment to pair with many line segments in the other class. We therefore need a cleaning process to remove these artifacts, or, in analogy to the sketching example mentioned above, a process that selects or creates an appropriate precise set of strokes based on the approximation. This process is called simplification and it is the second step in the merging process. Its result is illustrated in Fig. 2(c).
Simplification: The input is the joint map $A_{t}$ created by restrictive pairing. Simplification can be viewed as cleaning process after pair creation to create a smaller set of possibly new segments, being the final merging result. To use the sketch analogy again, the simplification process creates a single line by visually averaging the approximating bundle of strokes. Pairs of line segments are merged together to form new segments using the same merging process $m s$ and cost function $C$ but with different constraints. Simplification is done without any class restriction, i.e., a line segment in $A_{t}$ can pair with any other segment in $A_{t}$.

The main difference is that the simplification process has a global control mechanism: We iteratively merge a pair whose merging cost $C$ is the lowest at each pass. More precisely, the segment pair $L_{1}, L_{2}$ with lowest cost $C\left(L_{1}, L_{2}, a d\right)$, for one of the main angular directions $a d$, is merged in each pass. This means that $m s\left(L_{1}, L_{2}, a d\right)$ is inserted to list $A_{t}$, and $L_{1}, L_{2}$ are removed from $A_{t}$. Thus, each line segment can have at most one child. The process stops when the lowest cost is above a threshold $T_{s}$. The resulting simplified version of $A_{t}$ is the new global map $G_{t}$. Fig. 3(c) shows the simplified version of line segments in (b). Observe that both merged shape features from (a) are preserved (the straight line and the tent). This is acceptable, since given the input as in Fig. 3(a), we cannot decide which feature is the right one. This decision can be, however, made after merging several consecutive scans.

The main angular directions for simplification are computed with the same global statistics as in pairing process. This allows us to cope with accumulative errors. Section 2.2 gives more details on global statistics.

### 2.2 Main directions

The main directions $a d$ are obtained as significant peaks in the direction histogram of line segments (angles with the $x$ axis) in $G_{t-1}(t m)$, where $G_{t-1}(t m)$ is a global map $G_{t-1}$ restricted to line segments created in at most tm time steps ago. tm is a time memory factor. This restriction implies that only part of global map recently created determines the main directions. Therefore, the choice of directions is dynamic: the set of main directions ad is created with respect to the most recent part of the global map. This dynamic process assures the robustness of the algorithm with respect to main directions, e.g., for indoor environments, while simultaneously being flexible enough to react to changing or even non present main directions, e.g., outdoor or natural environments.


Fig. 3. The figure (b) is obtained from (a) by the proposed pair creation process. The index pairs in (b) refer to parent segments in (a). (c) shows the result simplification of (b). The newly created segments in (b) and (c) have to follow the main directions of $0^{\circ},+60^{\circ},-60^{\circ}$ with the $x$ axis.

Each line segment in the restricted global map $G_{t-1}(t m)$ contributes to the bin representing its direction with the weight given by its length. This histogram is cyclic, e.g., a window of size 5 around bin 1 contains bins $179,180,1,2,3$.

An important feature of our approach is the interaction between main directions and merging: Let us assume we have a significant number of segments in $S_{t}$, all having a similar direction that is significantly different from main directions present in $G_{t-1}(t m)$, i.e., these segments do not define a main direction yet. For example, this is the case if the robot starts to perceive a new surface.

Since the new segments follow a significantly different direction, the cost function $C$ assures that they create no children, because the pairing cost is above the threshold $T_{p}$, i.e., the transformation of the parent segments to child segments is too expensive. Thus, the original segments will remain in $A_{t}$. Since $A_{t}$, after simplification, becomes the new global map $G_{t}$, the new segments will lead to a peak, and will open a new main direction in the direction histogram. Consequently, pairing and simplification in the new direction will be allowed. A real example will be given in Section 3.

The direction histogram represents the statistical distribution of line segment directions. This statistical control provides a solution to the problem of cumulative errors (Problem 1 in the introduction). Cumulative errors introduce systematic distortions in the directions of line segments that accumulate slowly. The main issue is that accumulative errors do not lead to peaks in the direction histogram, and consequently, appearing line segments are correctly mapped to the existing main directions. On the other hand, as we have just described, if a surface of a new object is oriented into a new direction, it will lead to a peak in the direction histogram after a few scans of the surface have been acquired. This solution is based on quantization of the angular directions. Thus, a new main direction is created in the direction of the new surface if the difference between the new direction and the existing main directions is larger then the quantization factor, which is determined by the thresholds $T_{p}$ and $T_{s}$. The fact that the direction histogram provides a solution to the problem of cumulative errors is also true for other histogram-based approaches, e.g., [9].

### 2.3 New Line Segment Creation and Cost function

This section will describe the merging function $m s$ and the associated cost function $C$ used for the pairing and simplification process. The merging function is the most important module in the merging system, since it is responsible for the creation of the segments finally seen in the new map. Given a pair of line segments, $L_{1}$ and $L_{2}$, and the angular direction $a d$, it computes a merged segment $m s\left(L_{1}, L_{2}, a d\right)$ with the angular direction $a d$. The cost function $C\left(L_{1}, L_{2}, a d\right)$ is responsible for the filtering step: it produces the basic values for the decision if a created segment will be accepted or rejected as a member of the approximated $\operatorname{map} A_{t}$ or the new global map $G_{t}$. It measures the similarity of $L_{1}$ and $L_{2}$ in the context of the main direction $a d$.

The geometric intuition of the presented merging process and, in particular, the definition of merging cost $C\left(L_{1}, L_{2}, a d\right)$ is based on cognitively motivated principles of perceptual grouping. We followed the approach presented in [6] on grouping line segments to form longer line segments. It states that proximity of endpoints, parallelism, and collinearity are the main geometric relations that influence the perceptual grouping of line segments. Our setting is slightly different, since we merge two line segments only with respect to a given main direction $a d$. Therefore, we developed a new cost function. As mentioned above, the usage of main directions is necessary to cope with cumulative errors.

Before we explain the meaning of the perceptual grouping principles in our setting, we need to introduce one more concept of a straight line $l d$ that follows one of the main directions ad. Let two line segments $L_{1}$ and $L_{2}$ and a main angular direction $a d$ be given. A first step in our cost computation is to position a line following direction $a d$ between two line segments $L_{1}$ and $L_{2}$. The straight line $l d$ with direction $a d$ is positioned between $L_{1}$ and $L_{2}$ so that the equation

$$
d_{1} \cdot l_{1}=d_{2} \cdot l_{2}
$$

is satisfied (see Figure 4), where $l_{i}$ is the length of segment $L_{i}$ and $d_{i}$ is the distance of the midpoint of $L_{i}$ to line $l d$ for $i=1,2$. The merged segment $m s\left(L_{1}, L_{2}, a d\right)$ is defined by the convex hull of the projections of $L_{1}$ and $L_{2}$ on line $l d$. It is the segment from $P_{1}^{\prime}$ to $P_{4}^{\prime}$ in Figure 4.

Now we can explain the meaning of the perceptual grouping principles in our setting.

- Parallelism: The greater the angles between $L_{1}$ and $L_{2}$, and between $L_{1}$ and $L_{2}$ and $m s\left(L_{1}, L_{2}, a d\right)$, the greater the cost of merging them together. Likewise, the angle difference of longer segments have more weight than shorter ones.
- Collinearity: The greater the distance of the endpoints of $L_{1}$ and $L_{2}$ from the target line $l d$, the higher the value of the cost function.
- Proximity: The greater the distance between the projections of $L_{1}$ and $L_{2}$ on line $l d$, the higher the value of the cost function.

Finally we can define the new cost function that integrates the three perceptual grouping principles. Given the line $l d$, the cost of merging $L_{1}$ and $L_{2}$ to
$m s\left(L_{1}, L_{2}, a d\right)$ is defined by the following measure that incorporates our realization of the perceptual grouping principles (see Figure 4):

$$
\begin{aligned}
& C\left(L_{1}, L_{2}, a d\right)= \\
& \frac{\operatorname{lr}\left(\left(l_{1}+1\right) \frac{d\left(P_{1}, l d\right)+d\left(P_{2}, l d\right)}{1+K \cos \left(a_{1}\right)}-l_{1} \frac{d\left(P_{1}, l d\right)+d\left(P_{2}, l d\right)}{1+K}\right)}{1+K \cos \left(a_{12}\right)}+ \\
& \frac{\operatorname{lr}\left(\left(l_{2}+1\right) \frac{d\left(P_{3}, l d\right)+d\left(P_{4}, l d\right)}{1+K \cos \left(a_{2}\right)}-l_{2} \frac{d\left(P_{3}, l d\right)+d\left(P_{4}, l d\right)}{1+K}\right)}{1+K \cos \left(a_{12}\right)}
\end{aligned}
$$

where $a_{1}$ is the angle between $L_{1}$ and $l d, a_{2}$ is the angle between $L_{2}$ and $l d, a_{12}$ is the angle between $L_{1}$ and $L_{2}, P_{1}, P_{2}$ are endpoints of $L_{1}, P_{3}, P_{4}$ are endpoints of $L_{2}, d\left(P_{i}, l d\right)$ is the distance between point $P_{i}$ and line $l d$. The constant $K$ depends on the metric units used, and need s to be adjusted to obtain a balance between angular and metric units. The length ratio

$$
l r=\frac{l\left(m s\left(L_{1}, L_{2}, a d\right)\right)}{l\left(p\left(L_{1}\right)\right)+l\left(p\left(L_{2}\right)\right)}
$$

is the quotient of the length of the merged line segment $m s\left(L_{1}, L_{2}, a d\right)$ to the sum of the length of the projections $p\left(L_{1}\right)$ and $p\left(L_{2}\right)$ of line segments of $L_{1}$ and $L_{2}$ on line $l d$.


Fig. 4. Geometric illustration of the cost function $C\left(L_{1}, L_{2}, a d\right)$.

## 3 Implementation Details

### 3.1 Merging

Pairing: As described in Section 2.1, the merging consists of pairing followed by simplification. The pairing step creates a rough approximation of the new map, and it must take into account features in both the scan and the global map, even if a certain feature is only present in one of them. An example is given in Fig. 5, where the triangle feature is only present in the global map $G$. To permit appropriate combinations with segments of this feature, the straight segment of
the scan $S$ is split up to create segments corresponding to the feature segments of the global map. In order to do so a correspondence between endpoints of line segments is established. For every endpoint $E$ in $G$, we find a closest point $p(E)$ in $S$. If distance from $E$ to $p(E)$ is below a predefined threshold and $p(E)$ is not an existing end point in $S$, then $p(E)$ is inserted to $S$, splitting an existing line segment in $S$ into two collinear line segments (that meet at $p(E)$ ). We perform the same for every endpoint $E$ in $S$. The maps modified this way are the input to pair building.


Fig. 5. New vertices are inserted in $S$ in (a) as projections of vertices in $G$. The vertex insertion is necessary to make the correspondence of line segments possible.

The creation of descendants in the pairing process is dependent on the pairing threshold $T_{p}$. Fig. 6 shows the output of the pairing with global direction control of the input shown in Fig. 5 with different thresholds $T_{p}$, leading to different constellations: The leftmost map consists of newly created segments only. In the second figure the triangle segments could only pair once. The rightmost figure finally did not change the input; the threshold was too low to create any new segments.


Fig. 6. Input map is from Figure 5(b). Pairing with different threshold $T_{p}$ and global direction control with main directions of $0,+62^{\circ},-62^{\circ}$. From left to right we have $T_{p}$ $=0.05,0.04,0.03,0.01$.

### 3.2 Main Directions

The following section shows an example for the interaction between the merging process and the dynamic detection of main directions. The basic idea is not to merge segments with a cost above $T_{p}$ or $T_{s}$ respectively, but to keep them in their original position/direction Such segments can be described as outliers with respect to the current main directions $a d$. If these outliers become dominant, they will open a new main direction and will be merged. This process can be observed in Fig. 7 showing a section of an experiment with real laser finder data collected in a hallway at the University of Bremen. The robots' position is in the upper left corner, the robot moves up right and scans backward, i.e., down left.

In the left figure the robot approaches a $45^{\circ}$ corner, the current main directions consist of $0^{\circ}$ and $90^{\circ}$ angles with the $x$-axis. New $45^{\circ}$ segments are not simplified but transferred unchanged into the new global map. New $45^{\circ}$ segments still do not have enough weight to create a new direction in the center figure. Additionally the $0^{\circ}$ walls are out of sight, and therefore, the histogram loses this entry (which does not effect any segments in this situation). The only main direction remaining is $90^{\circ}$. In the right figure, new $45^{\circ}$ segments finally create a peak in the direction histogram. Hence the new main directions are now $90^{\circ}$ and $45^{\circ}$. Consequently, the new segments are merged together and simplified following the new $45^{\circ}$ direction.


Fig. 7. Bremen hallway experiment: a new main direction is detected in the right figure and used for merging.

## 4 Conclusions and Future Work

We presented a novel approach to robot mapping, based on an iterative process that merges similar line segments of subsequent scans. The process is locally
controlled by a similarity of line segments, which is motivated by principles of perceptual grouping. Additionally the process is controlled by global statistics, giving emphasis to the main directions present in the map to eliminate effects of accumulated errors of local scans. The experiments performed on real robot data show that the interaction between local and global control is able to successfully adapt to changes in directions without any pre-knowledge of the environment to build the environmental map given by subsequent scans. The merging process can be useful for any application where (visual) simplification of sets of line segments is needed; further experiments will include simplification of images gained by edge detection and hand drawn sketches for stroke recognition.

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